

Matter-Antimatter asymmetry of the Universe and Leptogenesis

Koichi Hamaguchi (Tokyo U.)

@TGSW 2021, September 11, 2021.

Mostly review

+ partially based on
K. Asai, KH, N. Nagata, S. Tseng [[arXiv:2005.01039](https://arxiv.org/abs/2005.01039)], JCAP **11** (2020) 013.

Plan

90% of the talk
= review



- Leptogenesis
 - ▶ Baryon Asymmetry of the Universe
 - ▶ Why "Lepto"genesis?
 - ▶ Seesaw and Leptogenesis in a "big picture"
- Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.
- Summary

Plan

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- Leptogenesis

- ▶ Baryon Asymmetry of the Universe

- ▶ Why "Lepto"genesis?

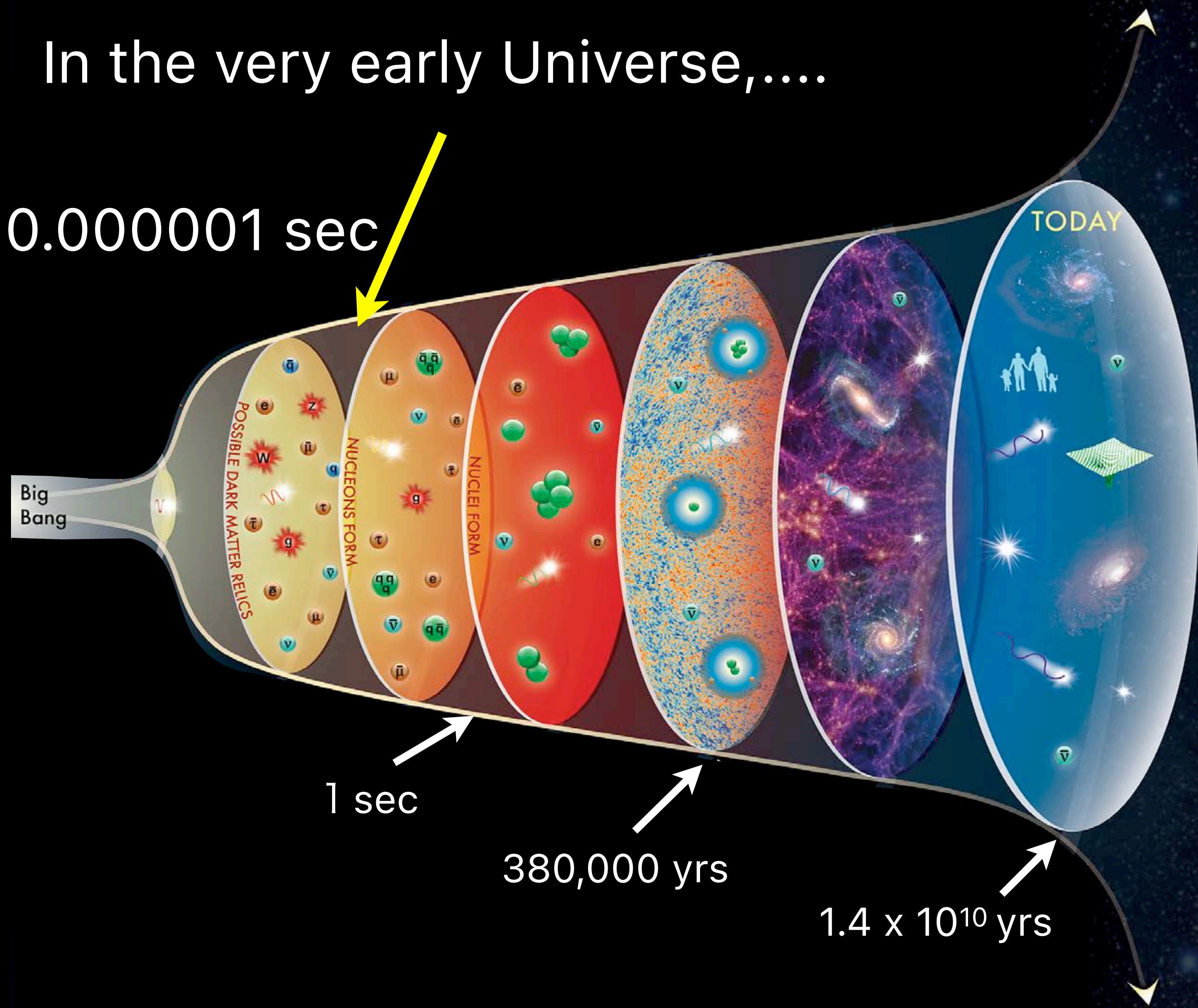
- ▶ Seesaw and Leptogenesis in a "big picture"

- Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

- Summary

In the very early Universe,....

0.000001 sec



1 sec

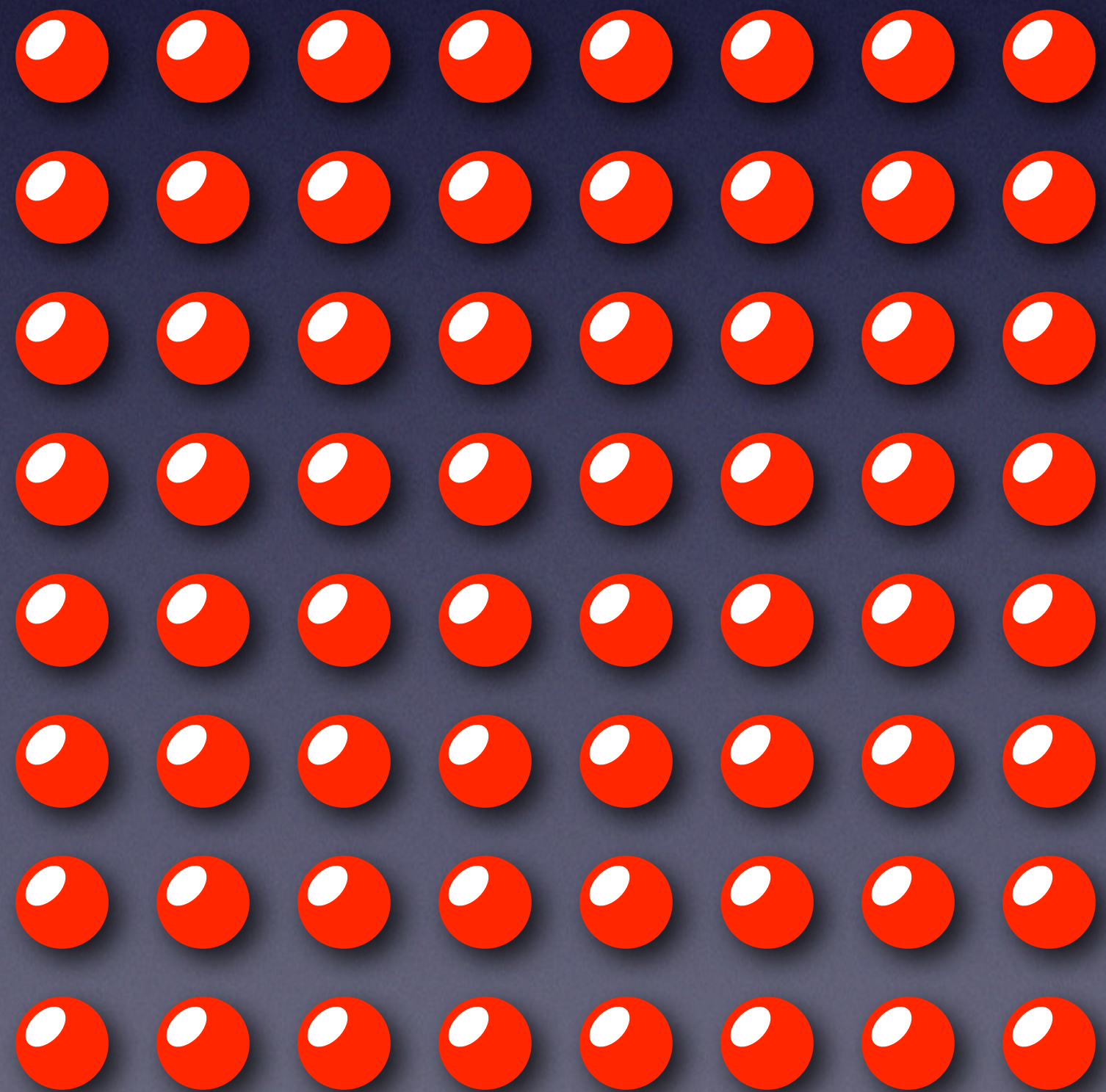
380,000 yrs

1.4×10^{10} yrs

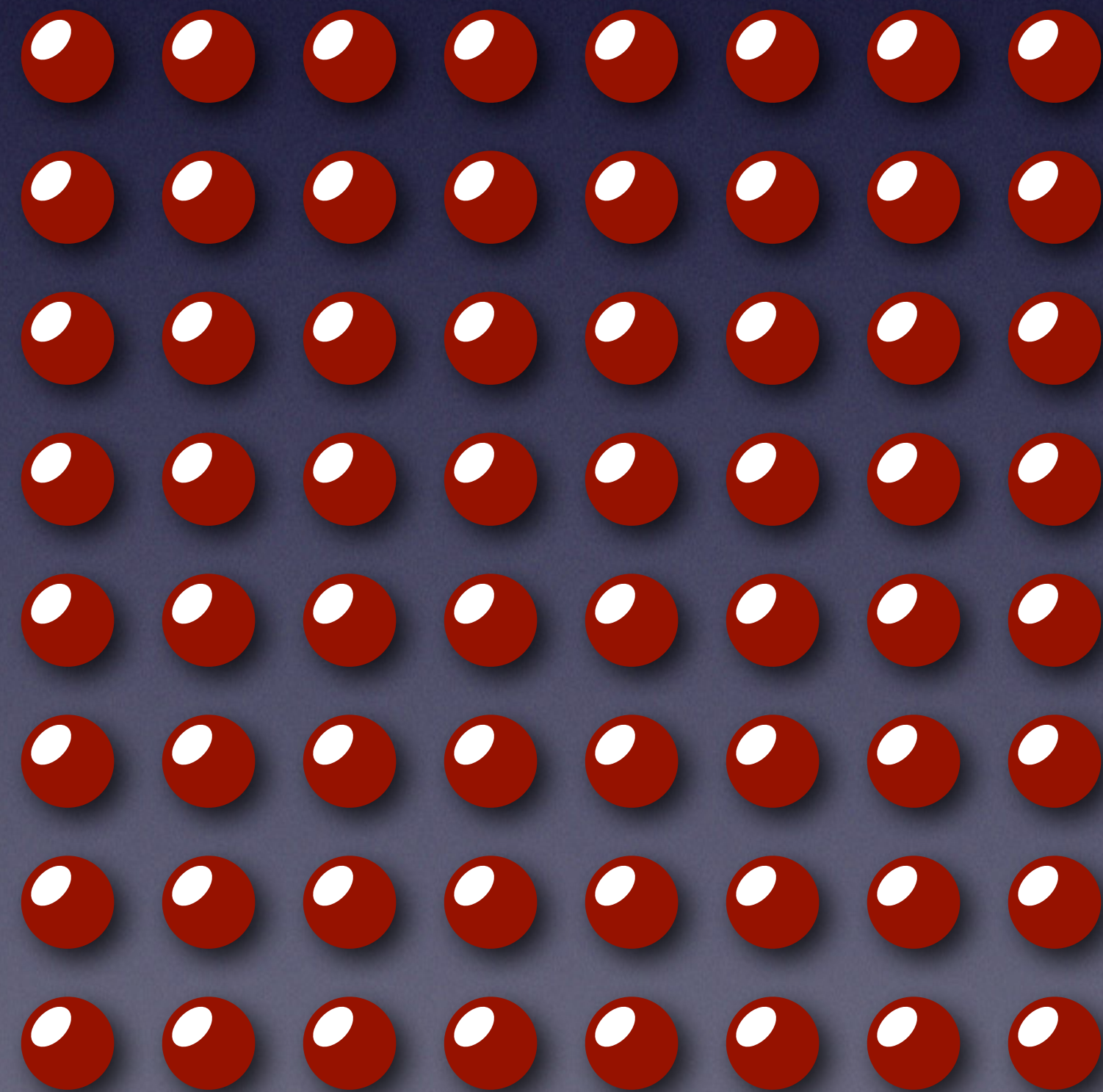
In the very early Universe,....

The number of particles and anti-particles were almost the same.

matter



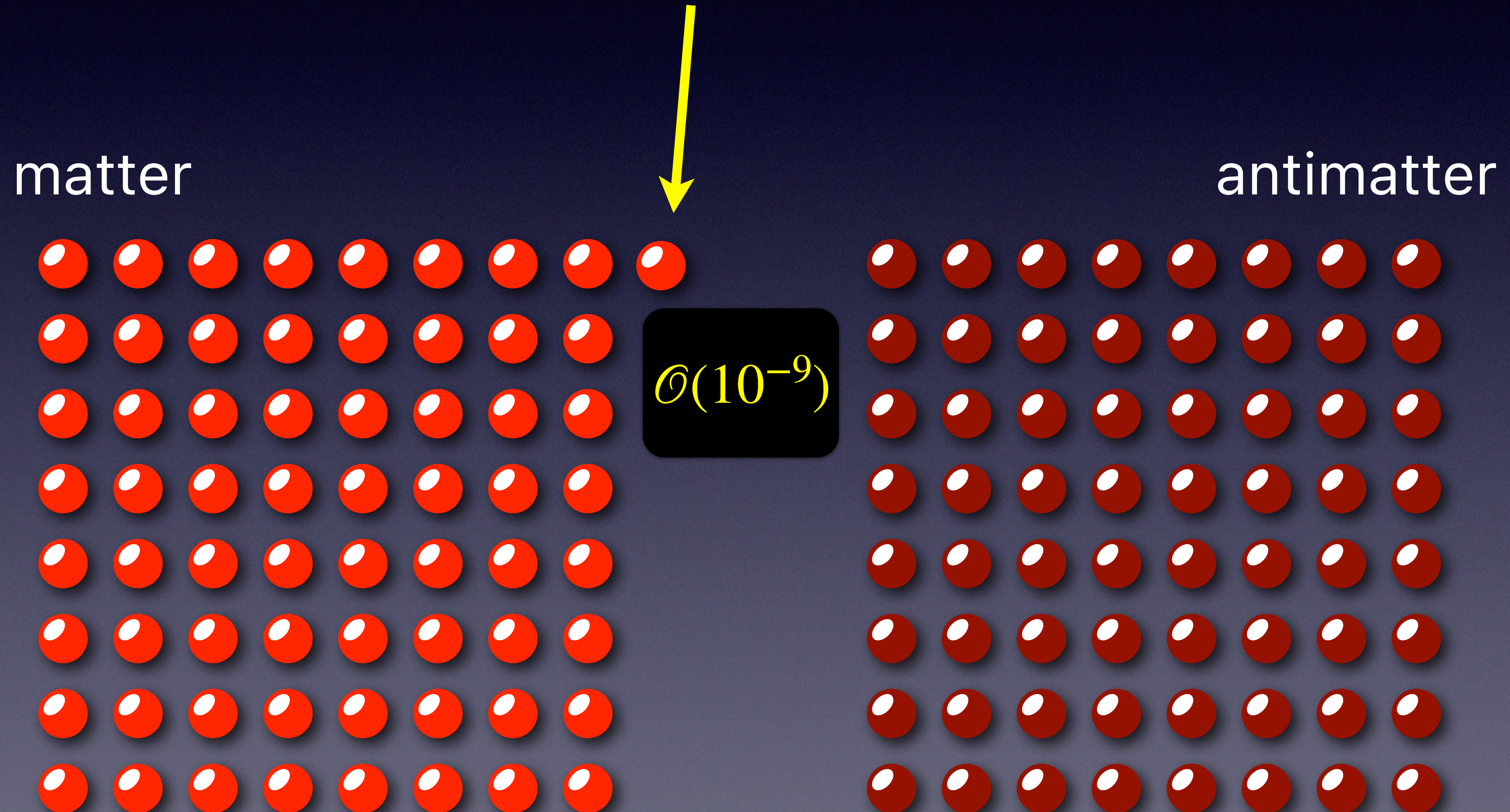
antimatter



In the very early Universe,....

The number of particles and anti-particles were almost the same.

But there was tiny excess of matter over anti-matter.

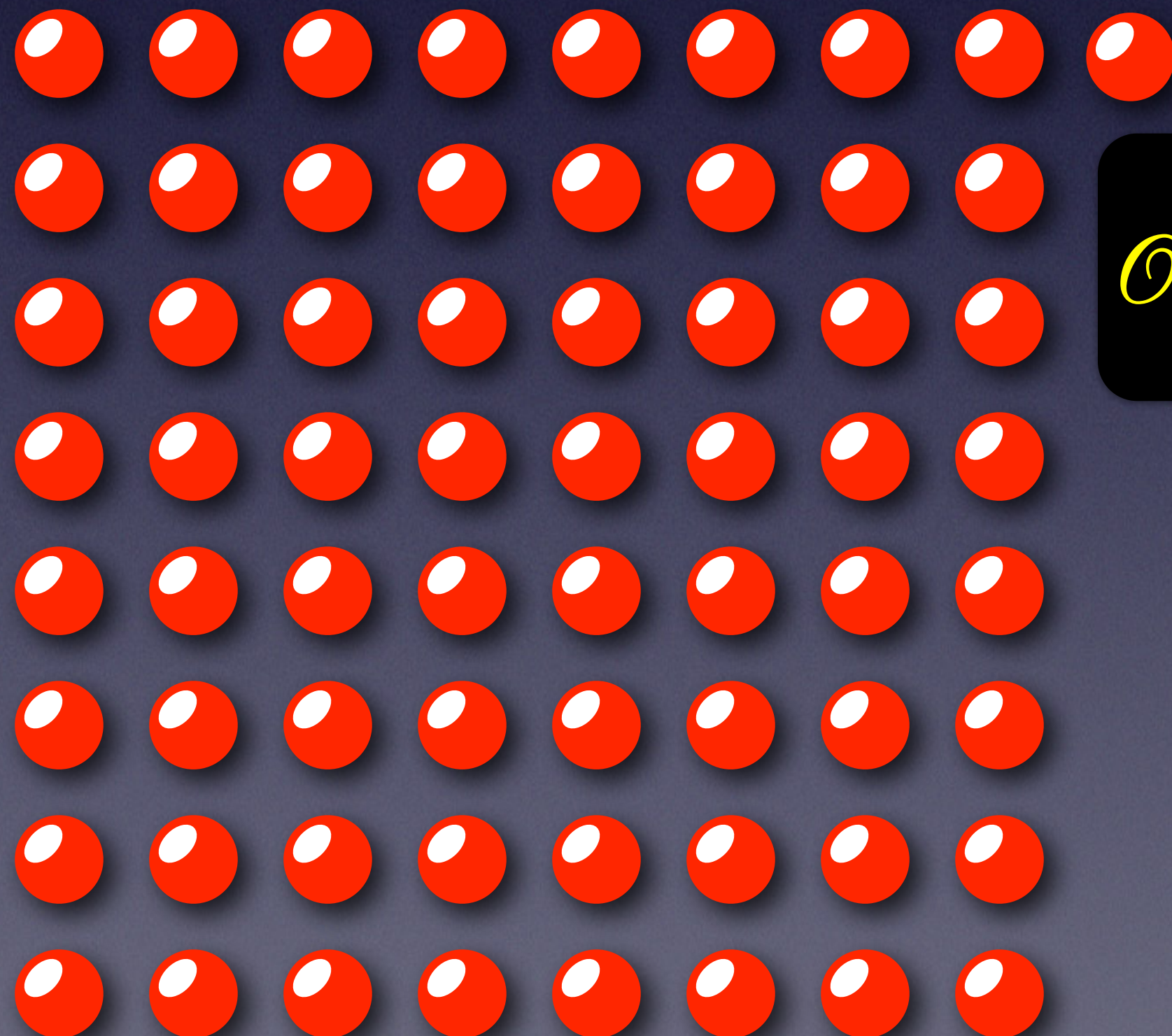


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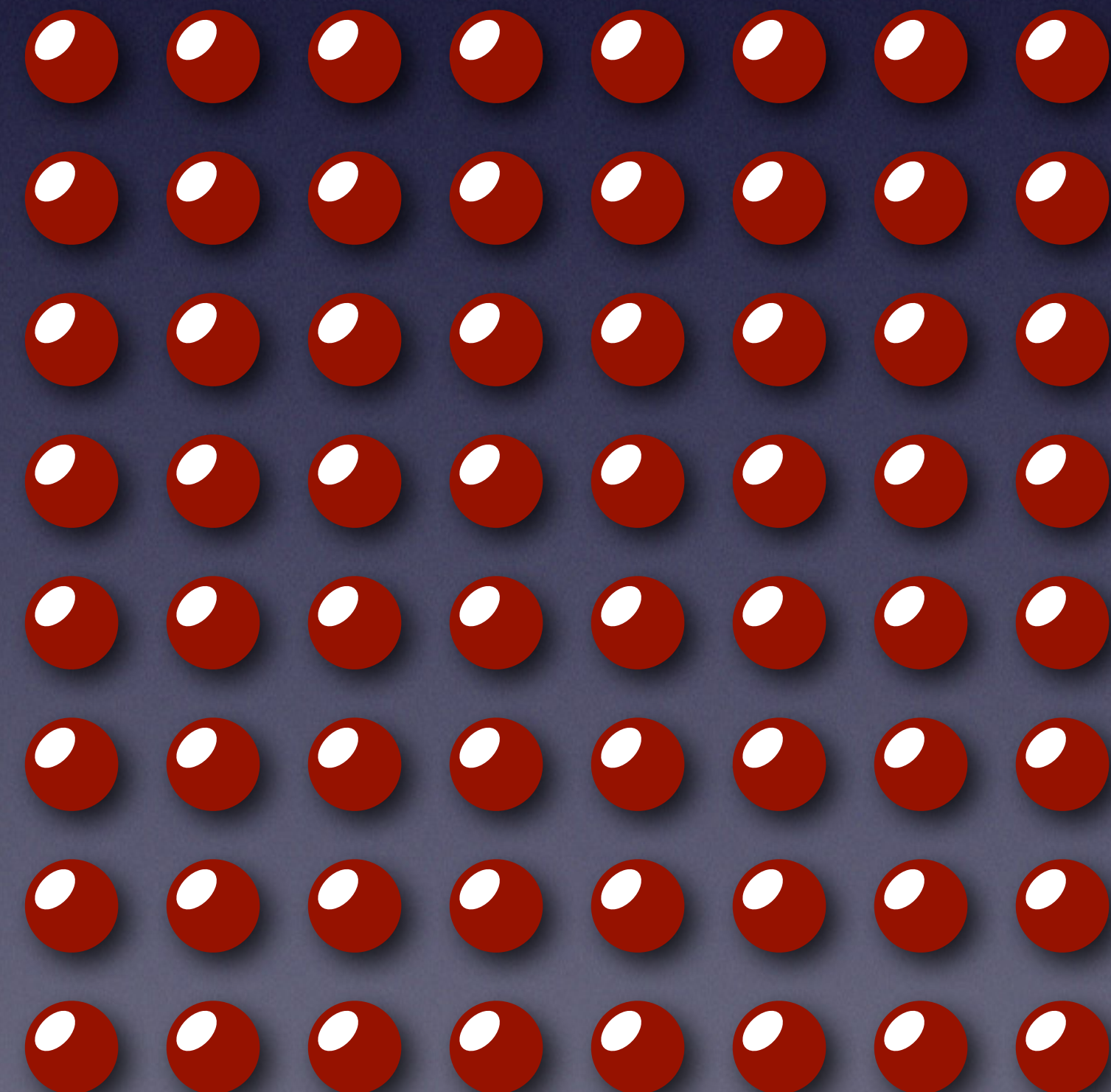
When the Universe got cooler, they **pair-annihilated**,..

matter



$\mathcal{O}(10^{-9})$

antimatter



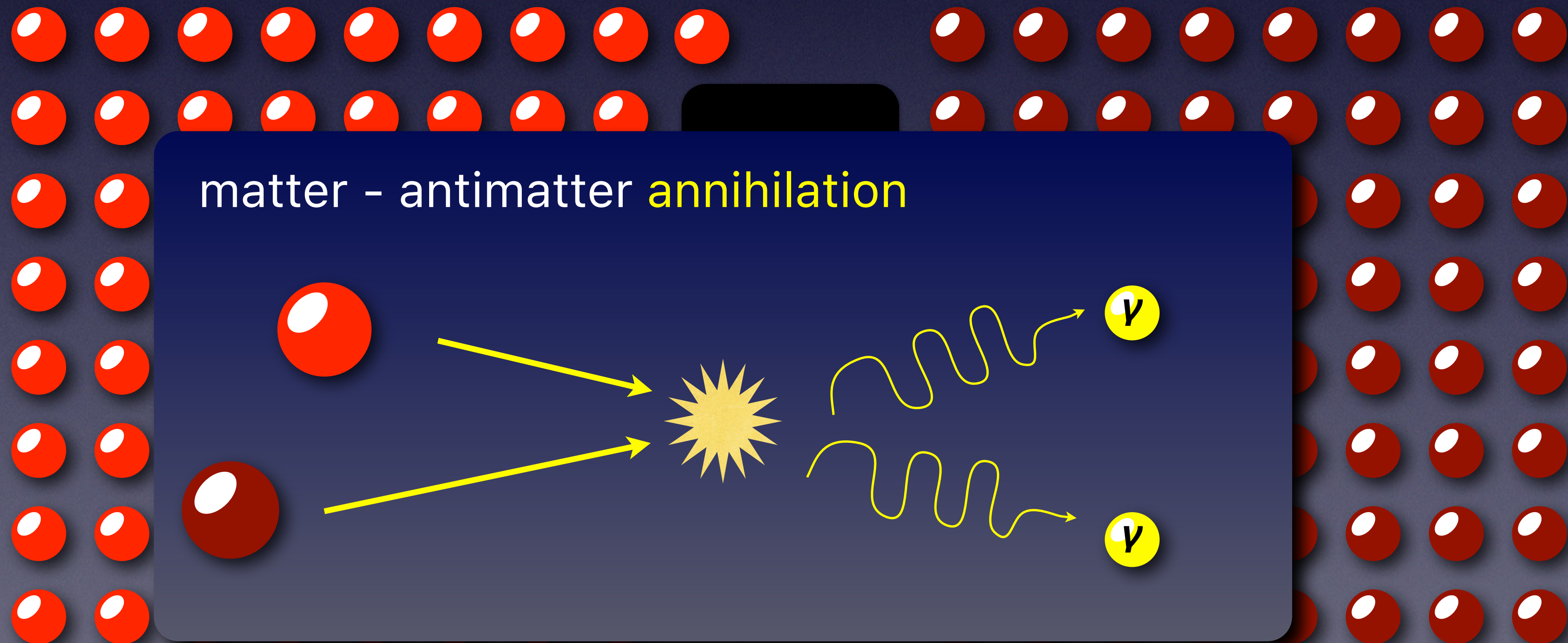
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matter

antimatter



In the very early Universe,....

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When the Universe got cooler, they **pair-annihilated**,..

matter

antimatter



$\mathcal{O}(10^{-9})$

In the very early Universe,....

The number of particles and anti-particles were almost the same.

When the Universe got cooler, they **pair-annihilated**,..

only matter remains



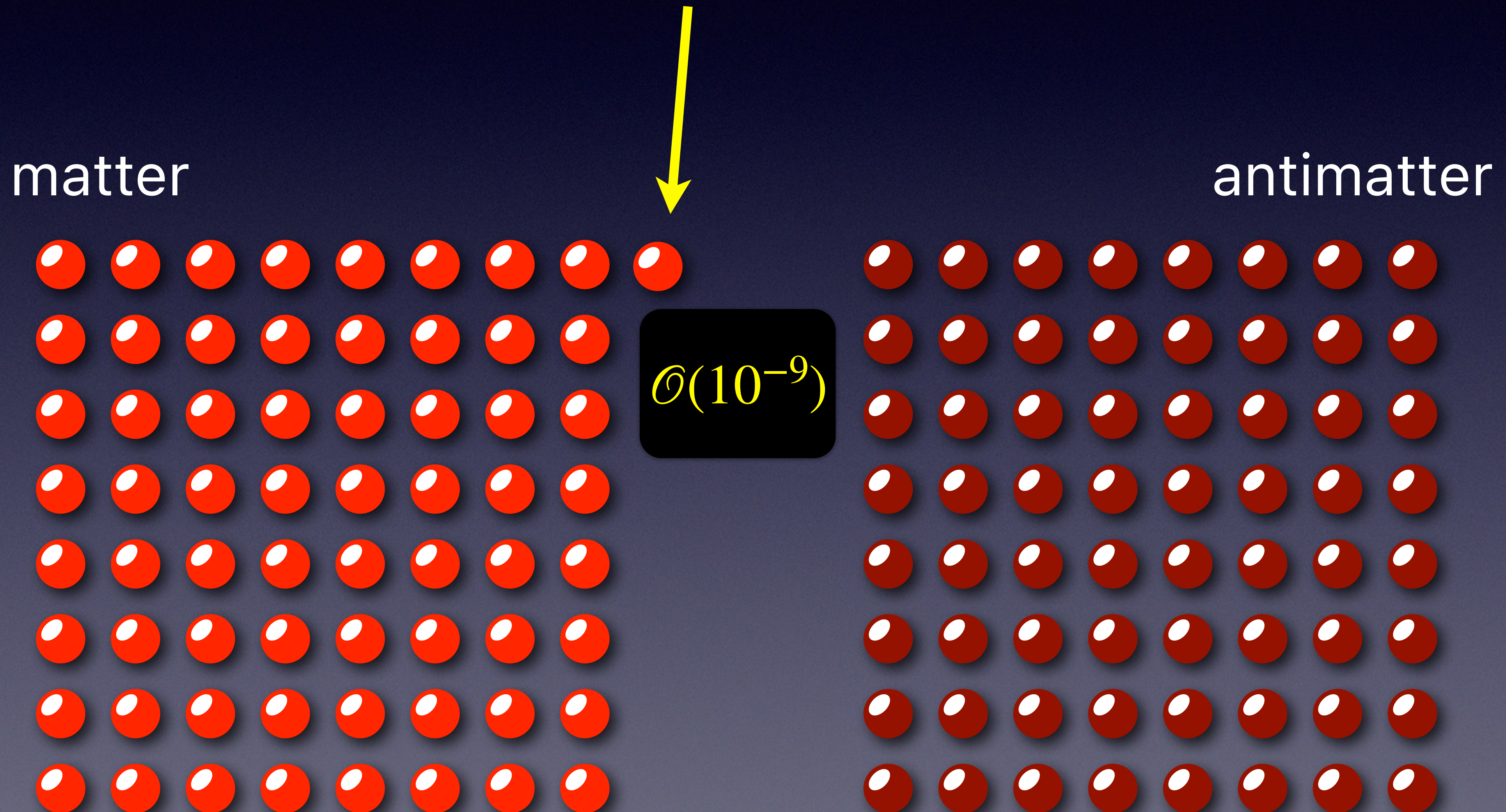
(no antimatter)



All of us (Galaxy, the Earth, the human beings,...)
are made from this leftover matter.

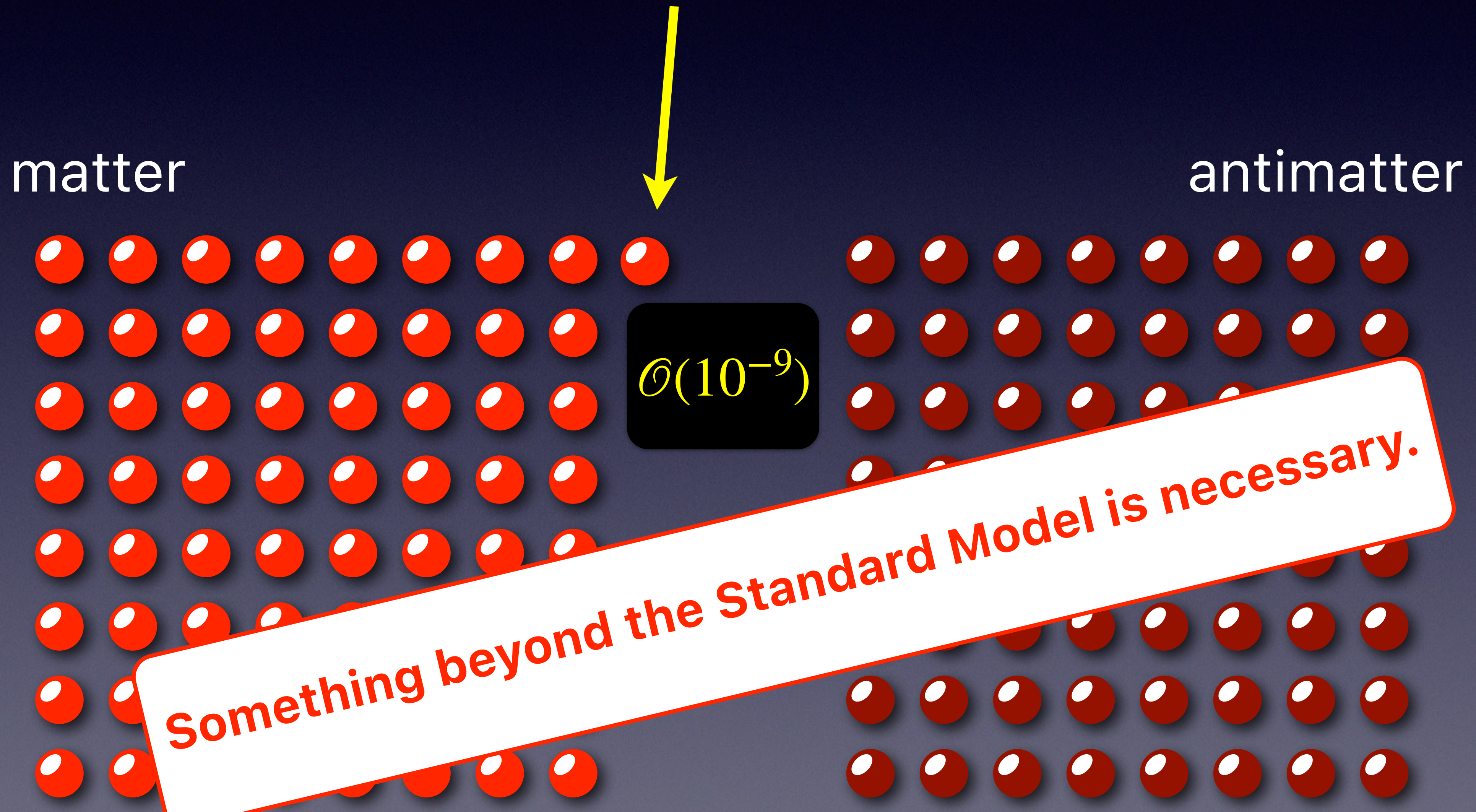
Puzzle

How was the initial excess of matter created ?

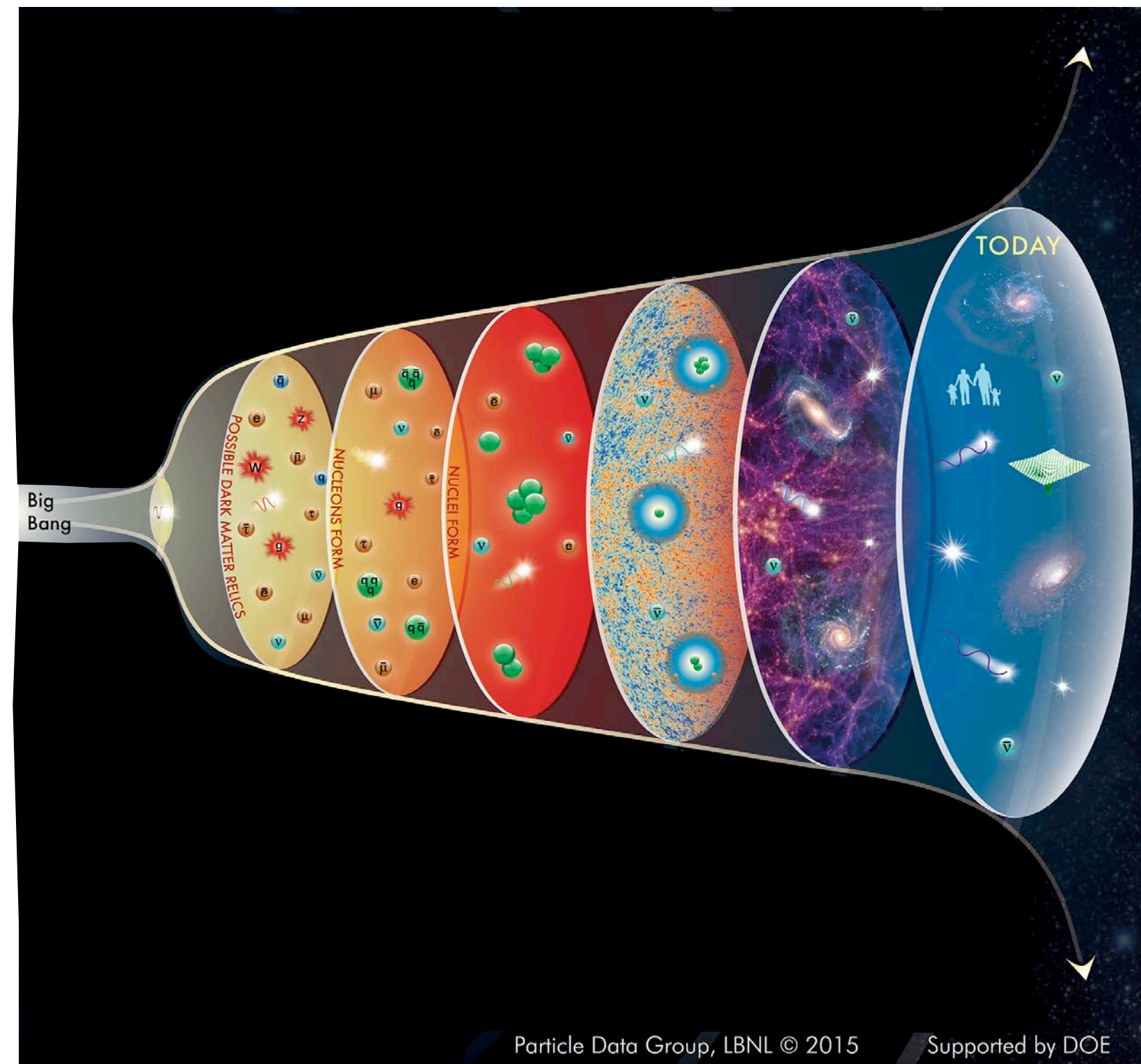


Puzzle

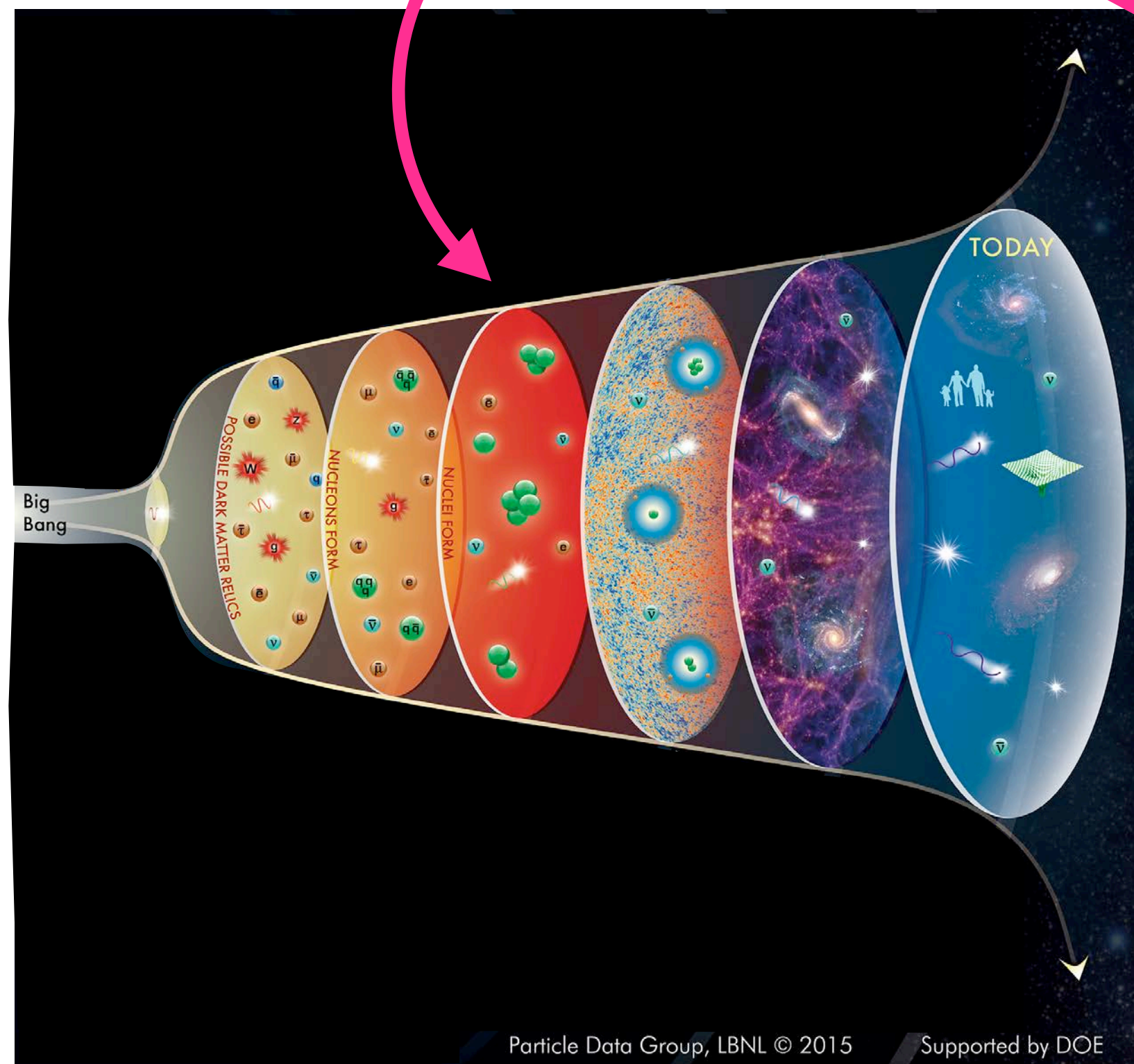
How was the initial excess of matter created ?



Observations (two independent evidences)



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(1) Big Bang Nucleosynthesis (BBN) (cosmic time about 1 sec)

$$5.8 \leq \eta_{10} \leq 6.6 \text{ (95\% CL).}$$

$$\longleftrightarrow 0.021 \leq \Omega_b h^2 \leq 0.024 \text{ (95\% CL).}$$

24. Big-Bang nucleosynthesis 3

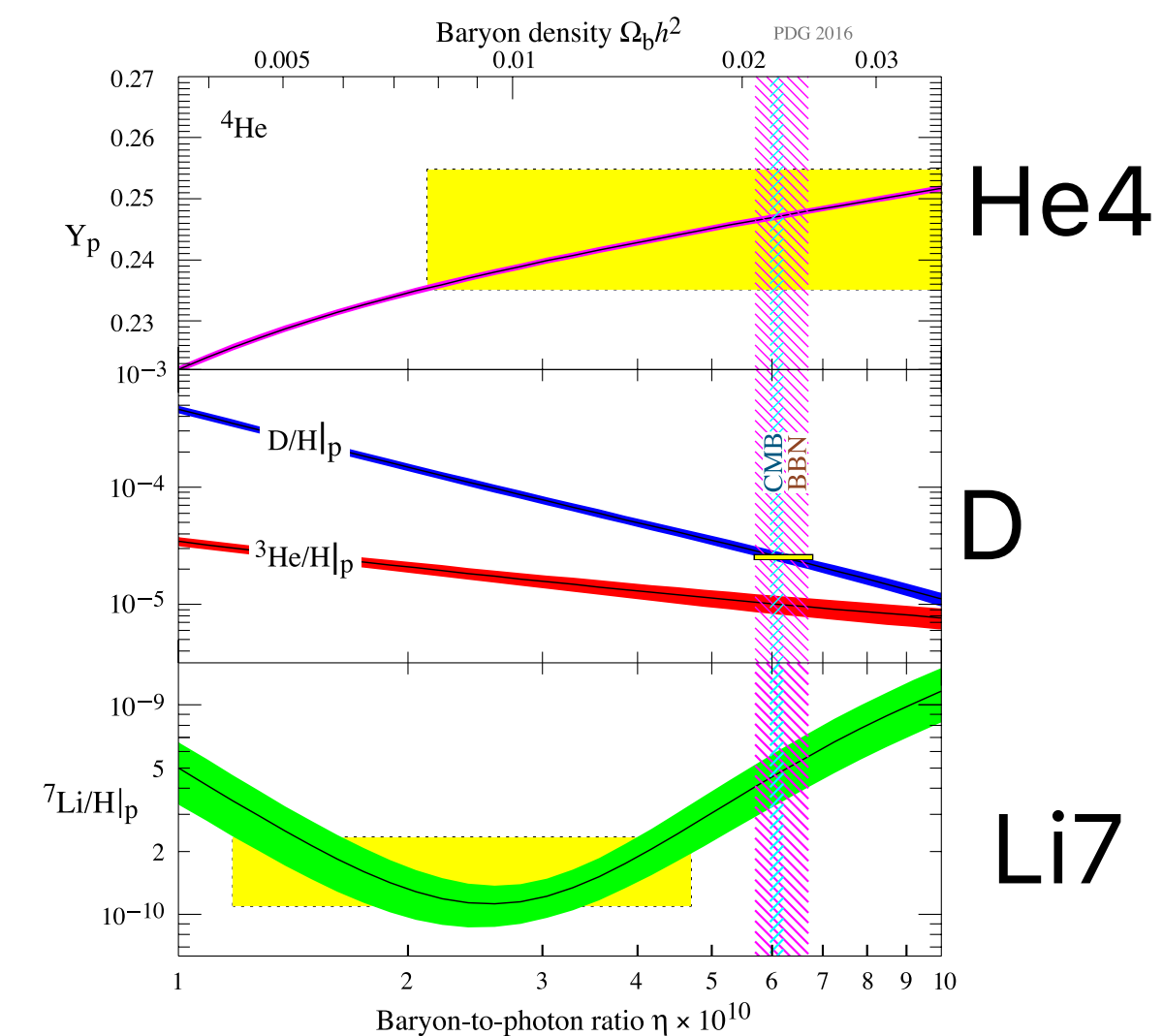
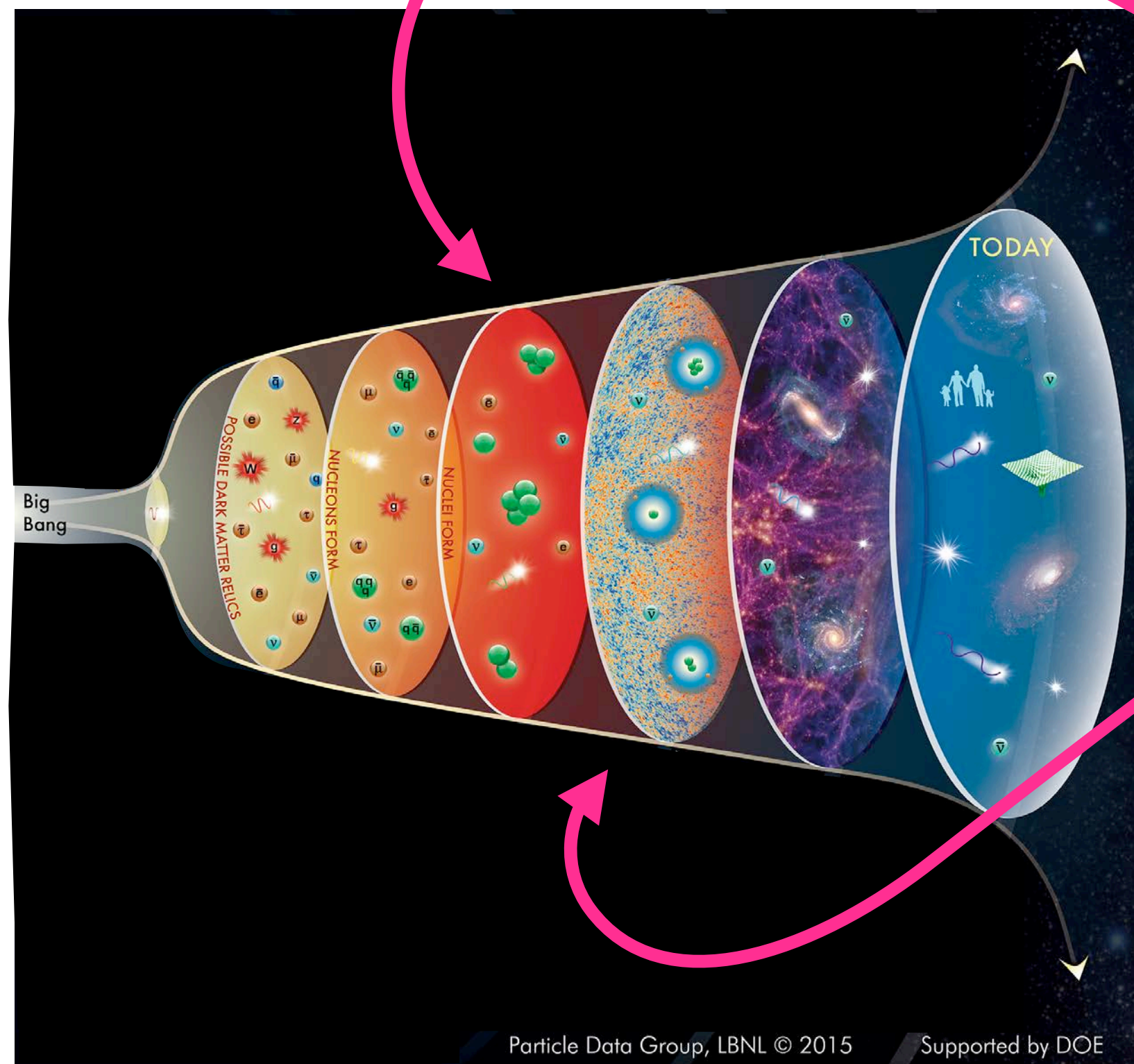


Figure 24.1: The primordial abundances of ${}^4\text{He}$, D , ${}^3\text{He}$, and ${}^7\text{Li}$ as predicted by the standard model of Big-Bang nucleosynthesis—the bands show the 95% CL range [5]. Boxes indicate the observed light element abundances. The narrow vertical band indicates the CMB measure of the cosmic baryon density, while the wider band indicates the BBN concordance range (both at 95% CL).

[Particle Data Group]

Observations (two independent evidences)



(1) Big Bang Nucleosynthesis (BBN)

(cosmic time about 1 sec)

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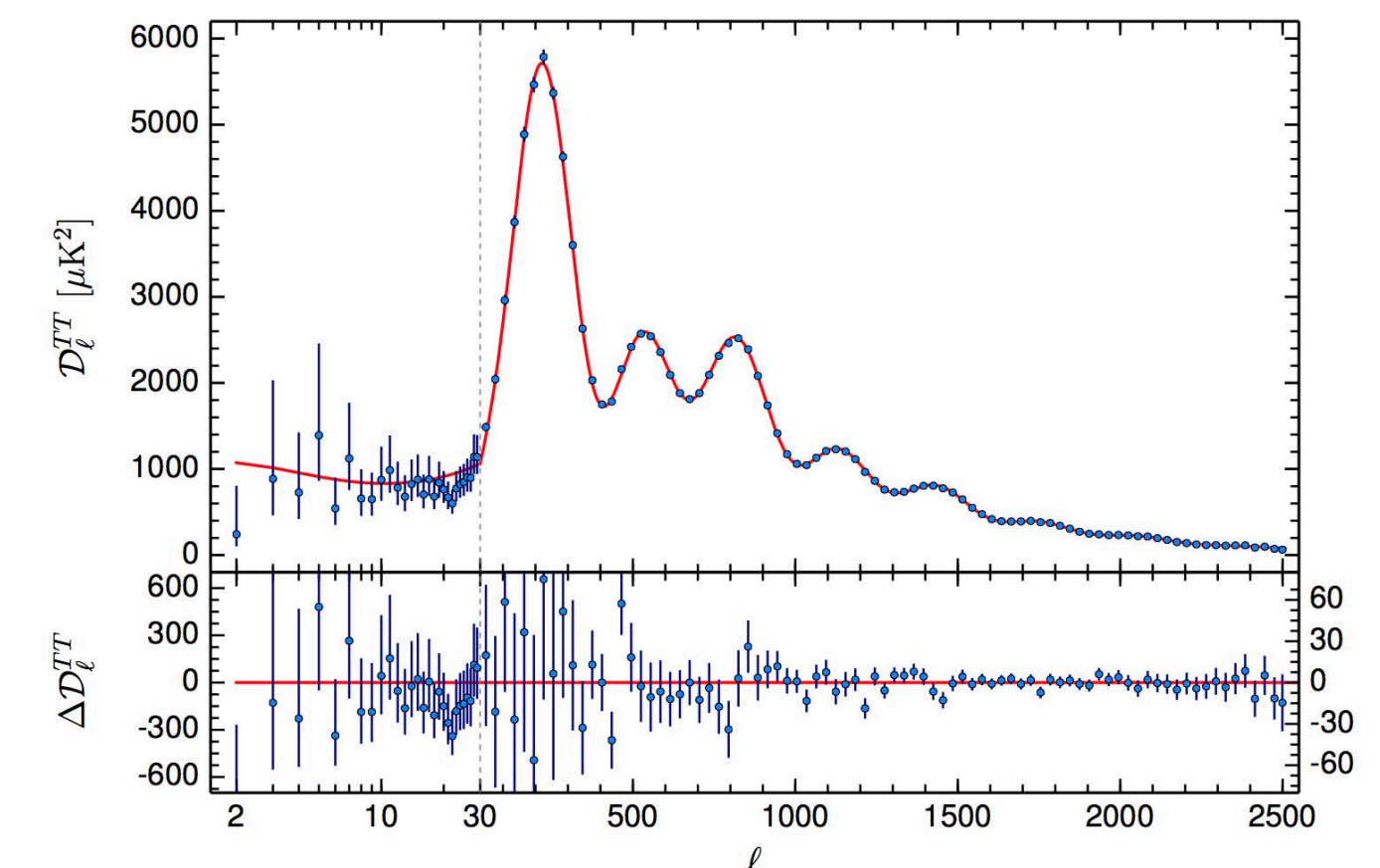
(2) Cosmic Microwave background

(cosmic time about 400,000 yrs)

$$\Omega_b h^2 \dots 0.02222 \pm 0.00023 \text{ (68\%)}$$

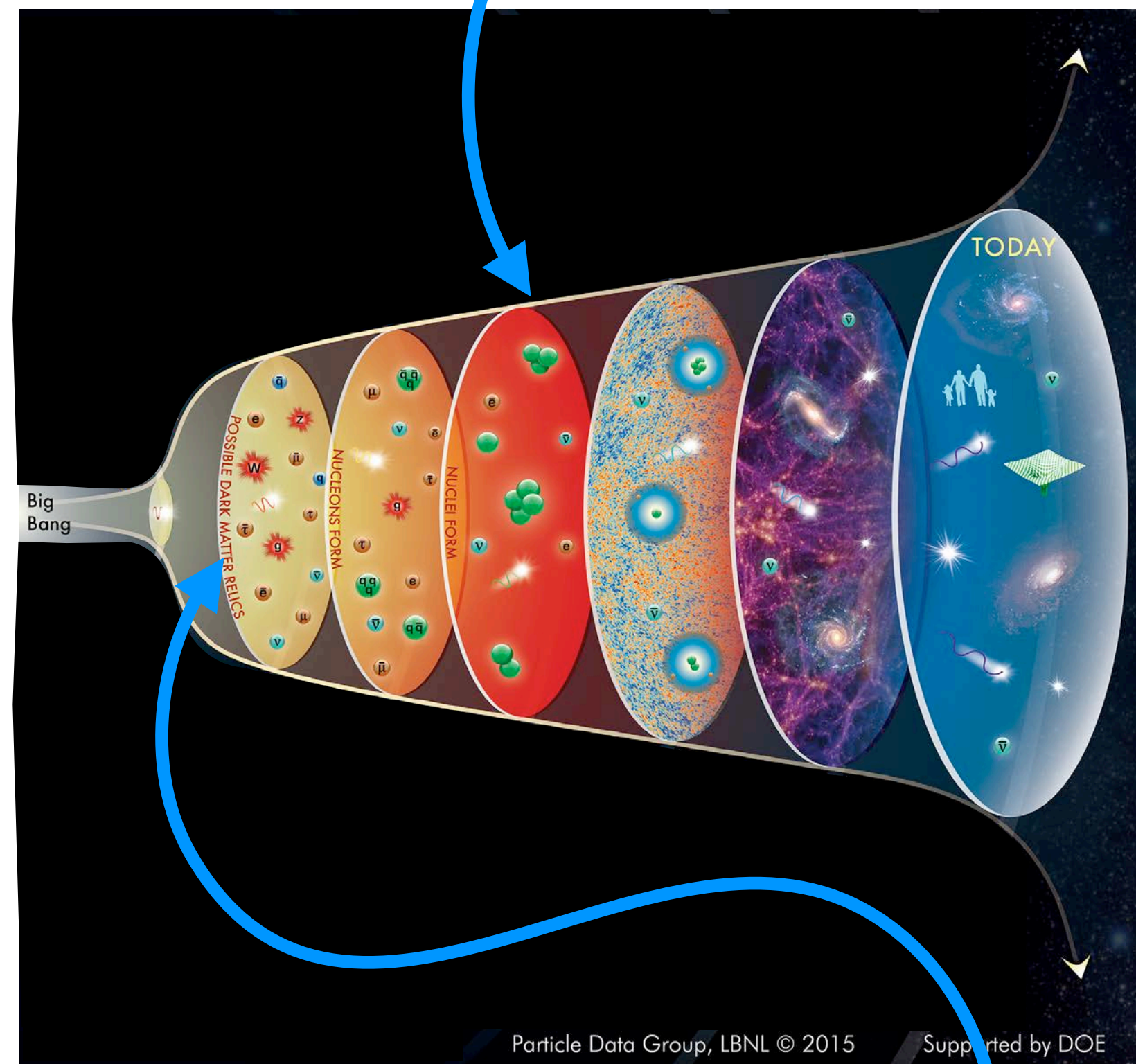
They are consistent.
(2) has better precision.

[Planck 2015]



When was the **Baryon Asymmetry of the Universe** generated?

When was the **Baryon Asymmetry of the Universe** generated?



At latest, before the BBN

(before 1 sec, temperature > 1 MeV.)

It is difficult to generate the BAU just before the BBN, so usually much earlier time (much higher temperature) is considered.

(An example at a relatively low temperature:
Electroweak Baryogenesis, @ $T \sim 100$ GeV.)

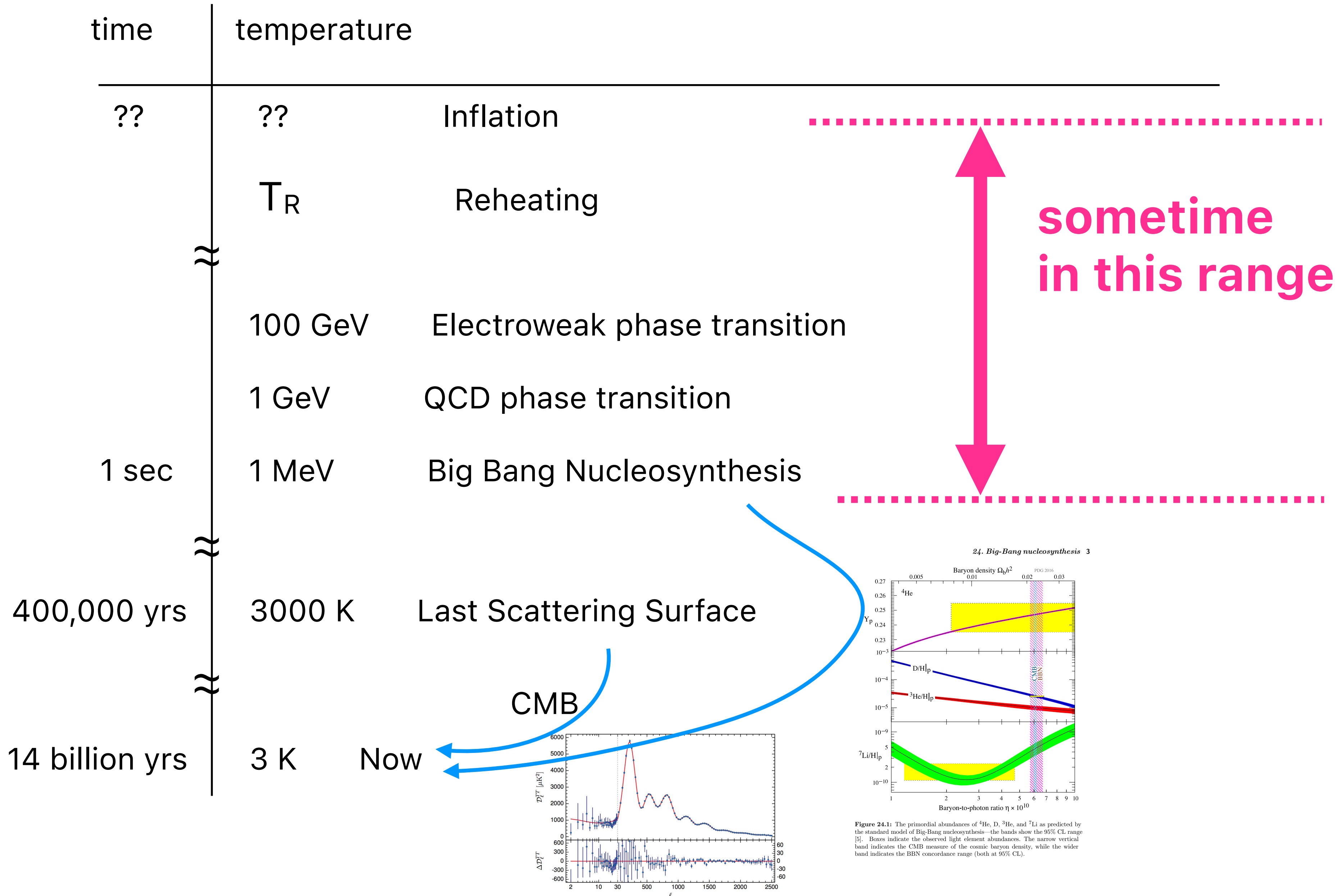
At earliest, after the Inflation

because the inflation dilutes everything.

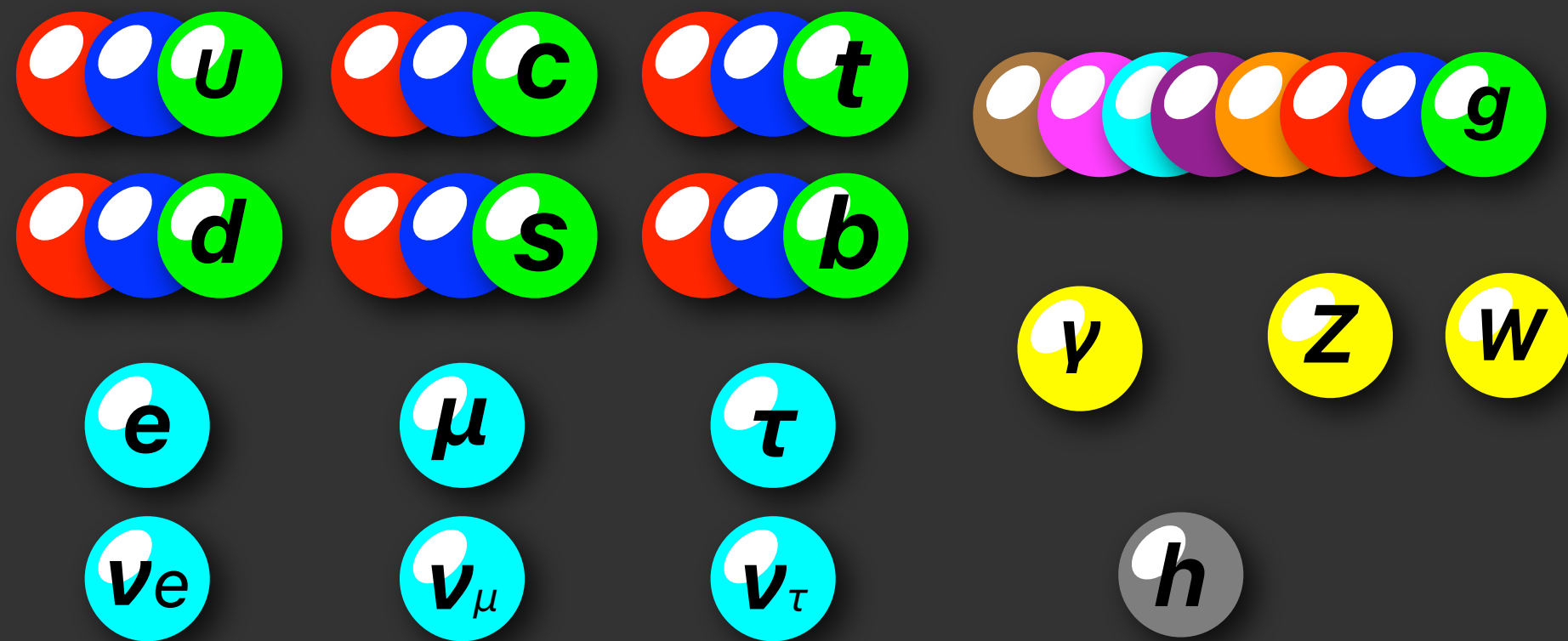
(An example just after the inflation: Non-thermal Leptogenesis.

The inflaton decays into right-handed neutrinos, which then lead to Leptogenesis.)

When was the Baryon Asymmetry of the Universe generated?



Standard Model



... does not work.

Sakharov's 3 conditions [[Sakharov 1967](#)]

- Baryon number violation
- CP-violation ... (but too small)
- out-of-equilibrium

Something beyond the Standard Model is necessary.

Plan

- Leptogenesis

- ▶ Baryon Asymmetry of the Universe

- ▶ Why "Lepto"genesis?

- ▶ Seesaw and Leptogenesis in a "big picture"

- Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

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Why "Lepto"genesis?

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Within the Standard Model,...

Both Baryon # (B) and Lepton # (L) are conserved at classical level.

$$\partial_\mu J_B^\mu = \partial_\mu J_L^\mu = 0$$

However, B and L are violated at quantum level! ['t Hooft, '76]

$$\partial_\mu J_B^\mu = \partial_\mu J_L^\mu = N_f \frac{g_2^2}{32\pi^2} \epsilon_{\mu\nu\rho\sigma} \text{Tr} F^{\mu\nu} F^{\rho\sigma} \neq 0$$

Note: B-L is conserved

$$\partial_\mu (J_B^\mu - J_L^\mu) = 0$$

Although there is essentially no effect at low energy,...

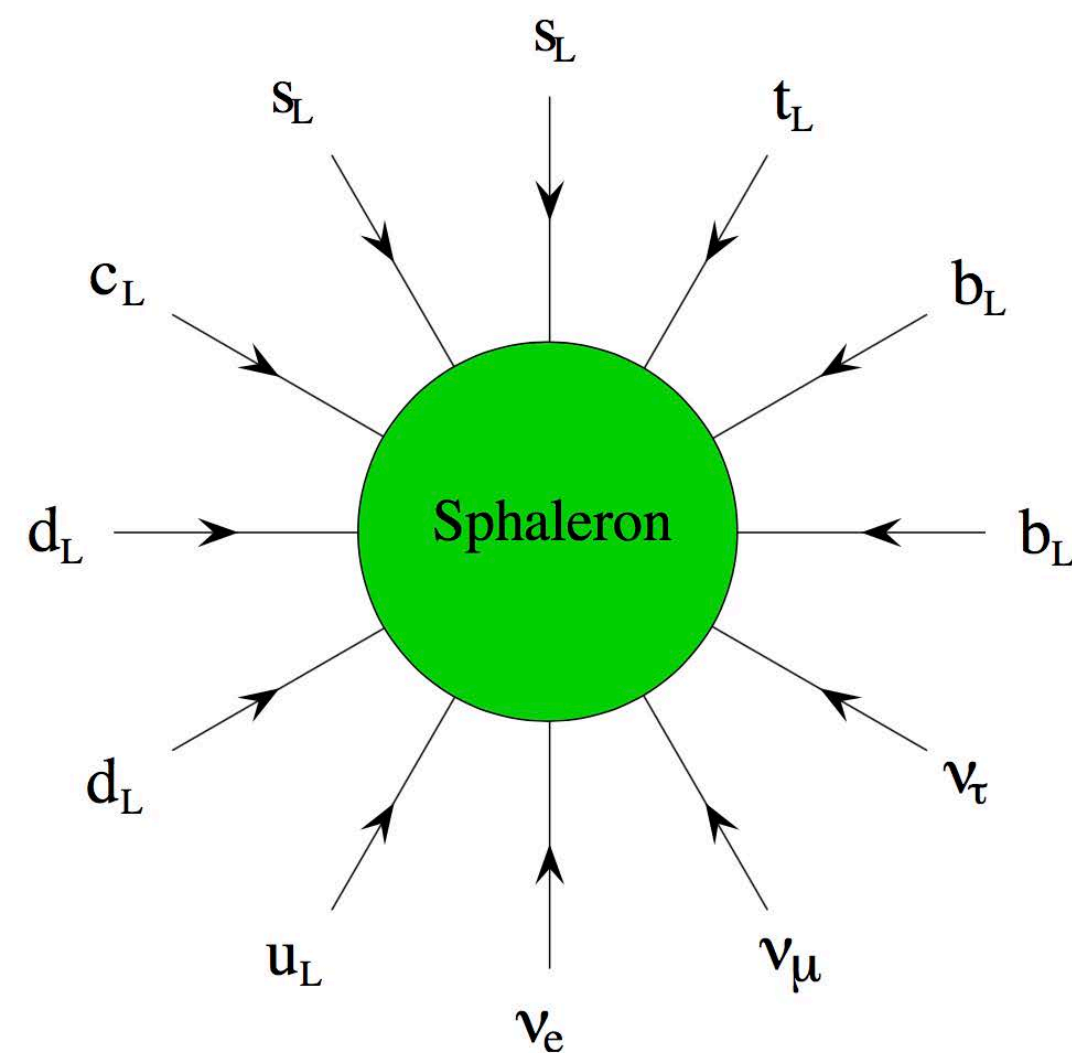
$$\Gamma_{B,L} \sim e^{-16\pi^2/g_2^2} \sim 10^{-170}$$

Why "Lepto"genesis?

Within the Standard Model,...

At high temperature, $T \gg 100 \text{ GeV}$,
B and L violating processes (sphaleron)
become very rapid, and in thermal equilibrium!

[Kuzmin, Rubakov, Shaposhnikov,'85]



Sphaleron process

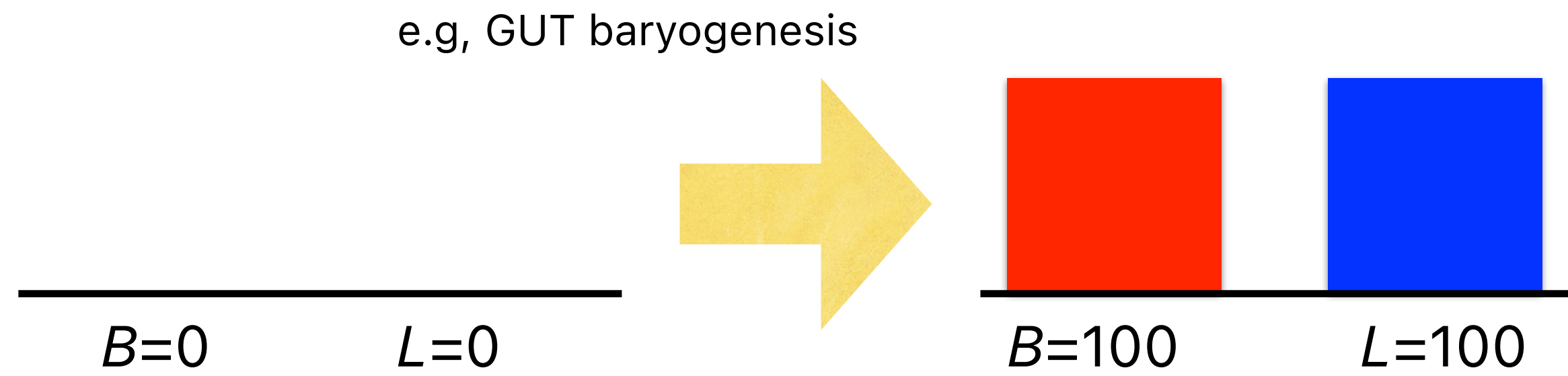
processes involving 9 quarks ($B=3$)
and 3 leptons ($L=3$).

Note that $B-L$ is conserved.

Figure 1: One of the 12-fermion processes which are in thermal equilibrium in the high-temperature phase of the Standard Model.

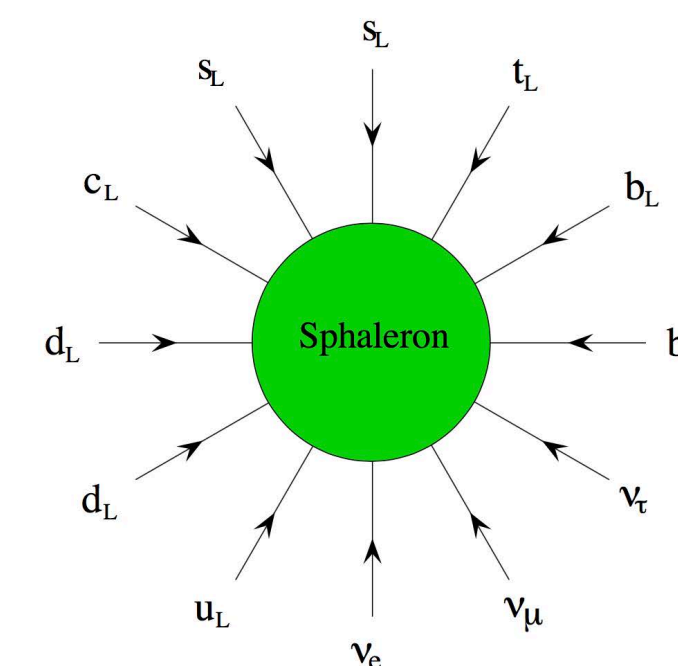
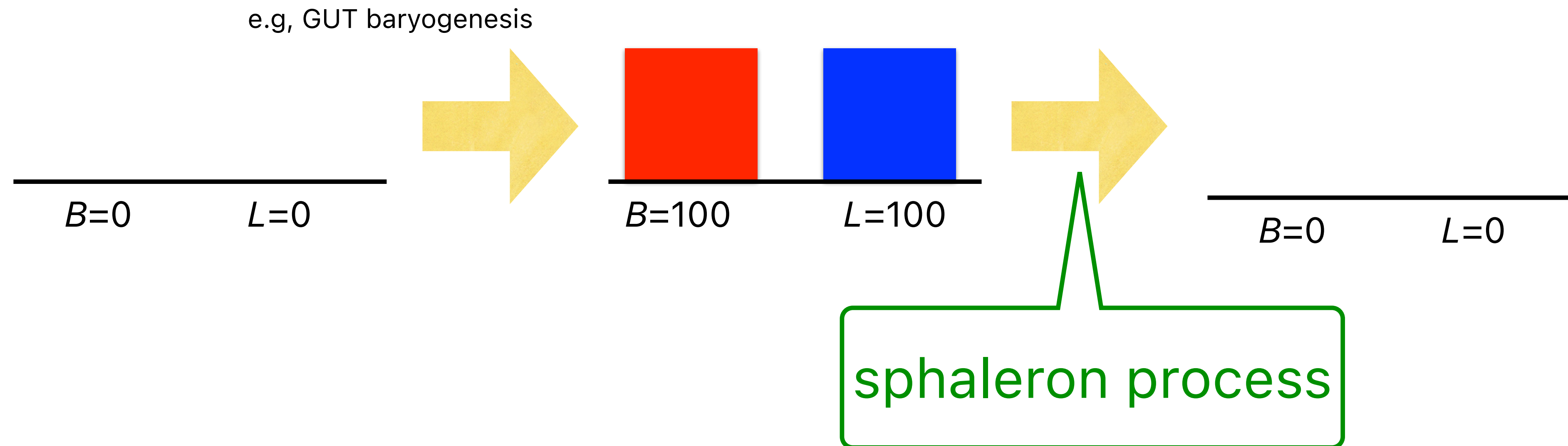
[fig. from W.Buchmuller, 1210.7758]

Therefore, if the Baryon asymmetry is generated via a ***B-L conserving process***,...



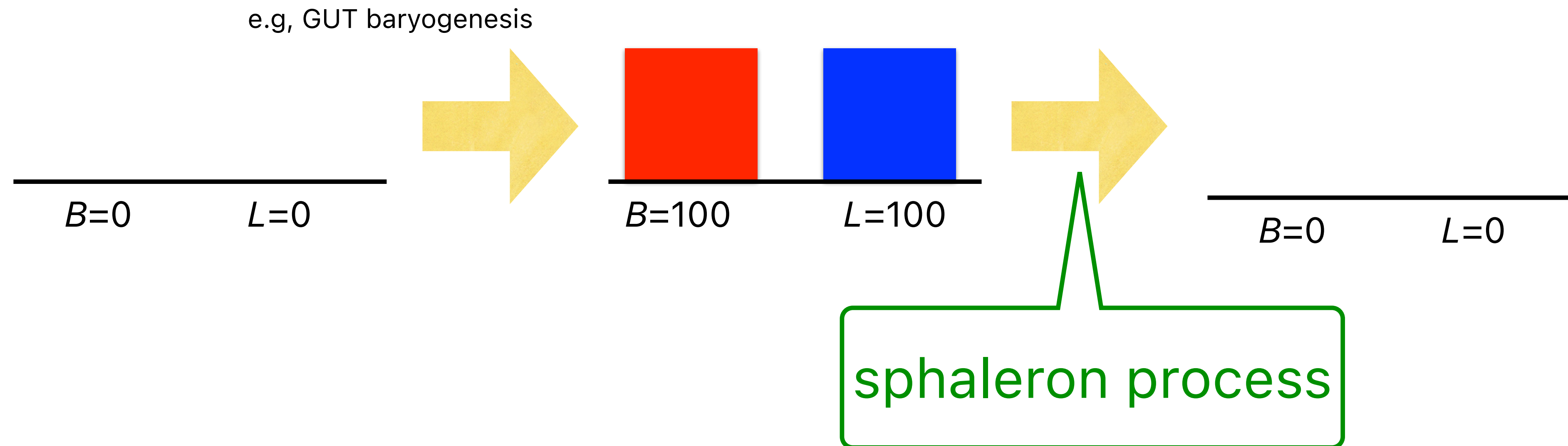
Therefore, if the Baryon asymmetry is generated via a ***B-L conserving process***,...

Finally $B=0$ at equilibrium.

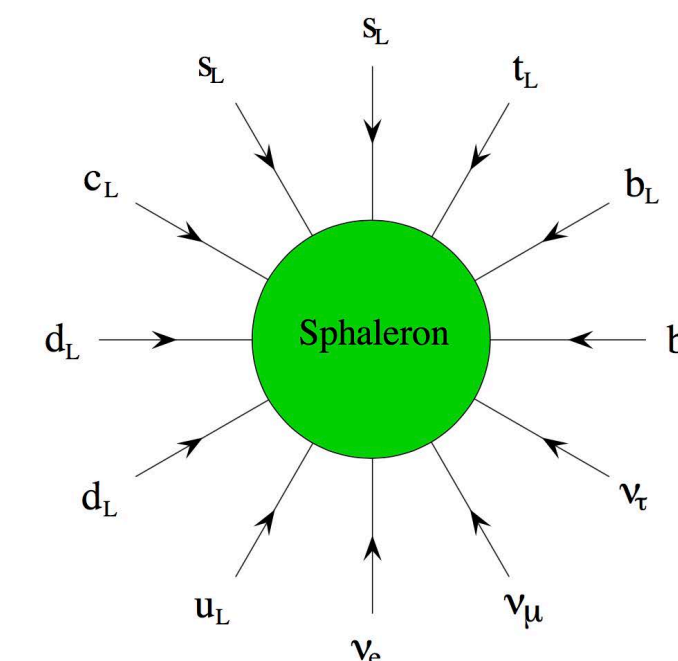


Therefore, if the Baryon asymmetry is generated via a ***B-L conserving process***,...

Finally **$B=0$** at equilibrium.



B-L violating process is necessary.



Sakharov's 3 conditions

- ~~Baryon number (B) violation~~
 - C and CP violation
 - Out-of-equilibrium
- B-L violation***

Sakharov's 3 conditions

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On the other hand, this means that...

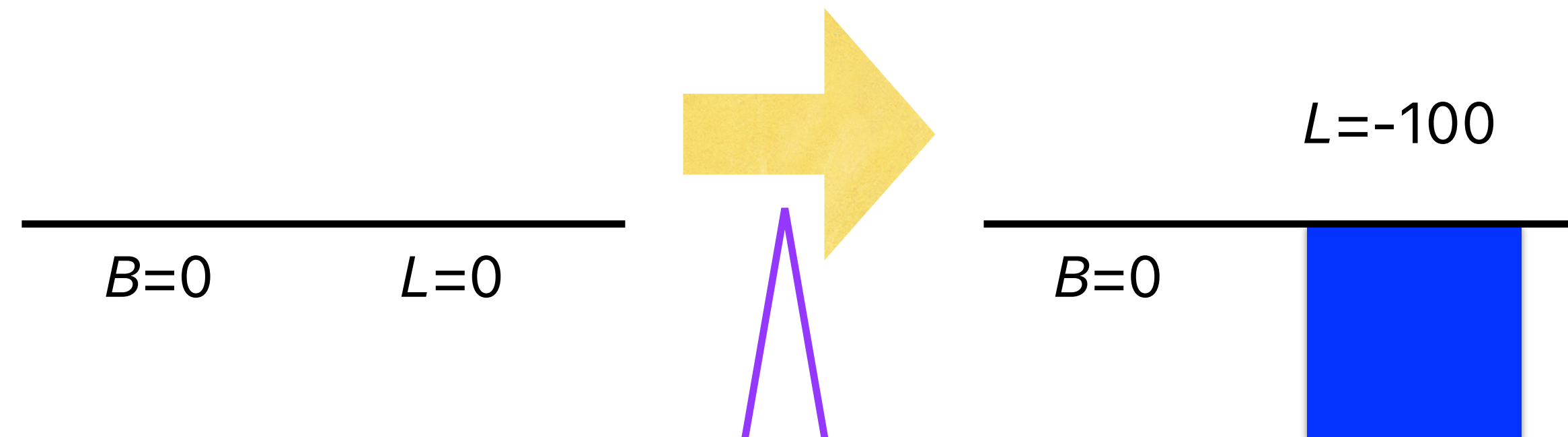
Baryogenesis can work, not only via B-violation, but also via **L-violation**.

and L-violation implies **Majorana neutrino (and $0\nu\beta\beta$ decay)**.

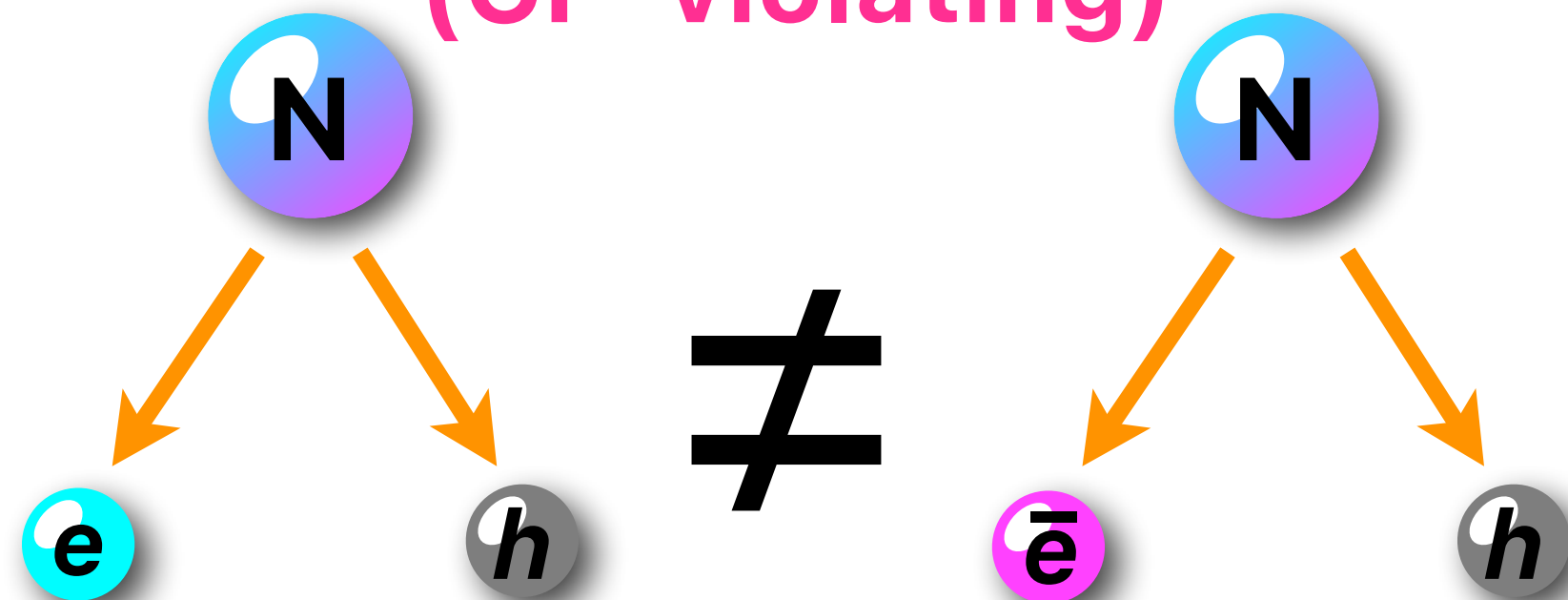
Leptogenesis

[Fukugita, Yanagida, '86]

generate Lepton asymmetry



right-handed neutrino decay
(CP-violating)

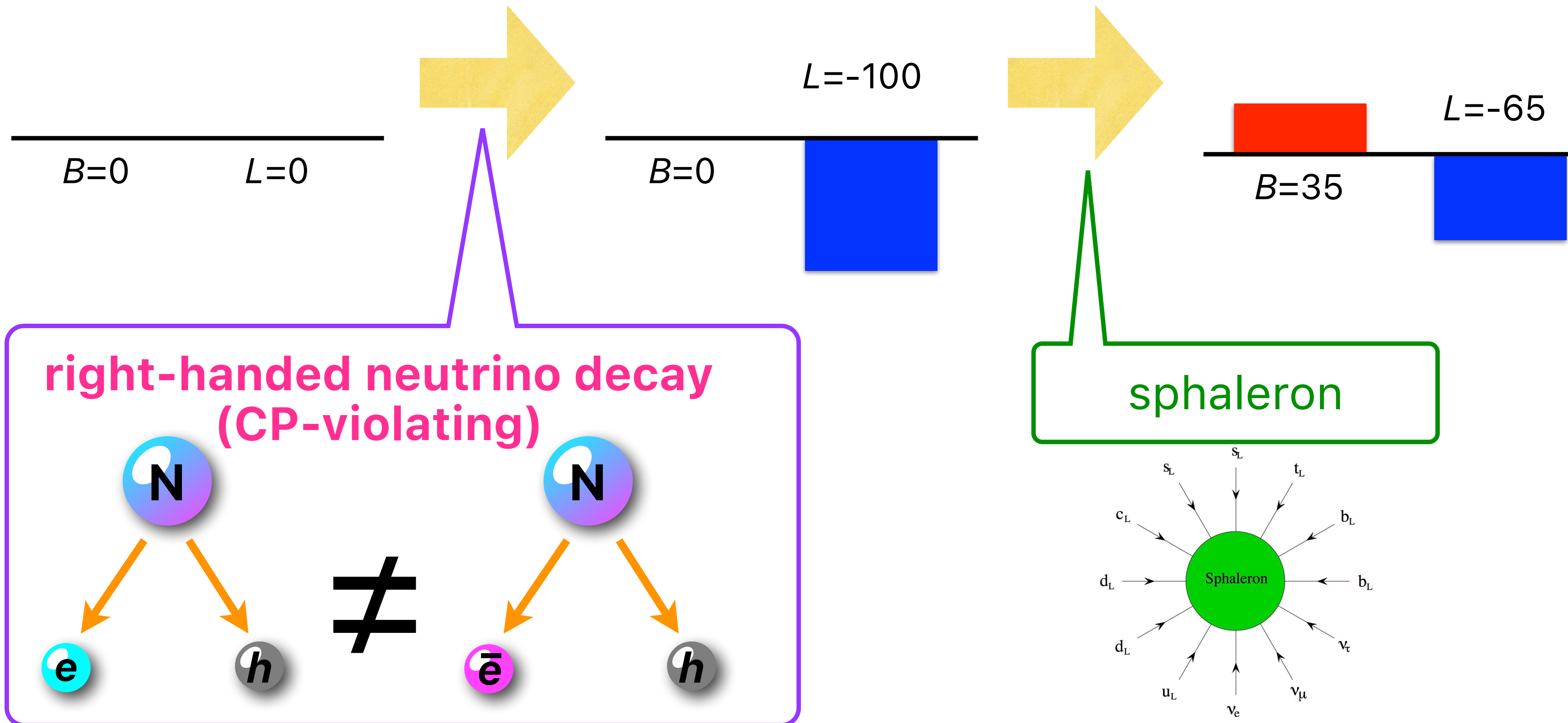


Leptogenesis

[Fukugita, Yanagida, '86]

generate Lepton asymmetry

Then, $B \neq 0$ remains at equilibrium!



Leptogenesis

[Fukugita, Yanagida, '86]

There are various versions...

- Thermal Leptogenesis

[Fukugita, Yanagida,'86, Buchmuller, Plumacher, Di Bari,.....]

- Leptogenesis from Inflaton Decay

[..... Asaka, KH, Kawasaki, Yanagida,'99.....]

- Leptogenesis from R.H.Sneutrino dominated Universe

[Murayama, Yanagida,'93, KH, Murayama, Yanagida,'01.....]

[Murayama, Suzuki, Yanagida, Yokoyama,'93,... ...]

- Affleck-Dine Leptogenesis

[Murayama, Yanagida,'93, Asaka, Fujii, KH, Yanagida,'00, Fujii, KH, Yanagida,'01,]

- via R.H.N oscillation (ν_{MSM})

[Akhmedov, Rubakov, Smirnov,'98, Asaka, Shasposhnikov,'05.....]

(+ many others ...)

For reviews, see e.g., arXiv:1711.02861~ 1711.02866.

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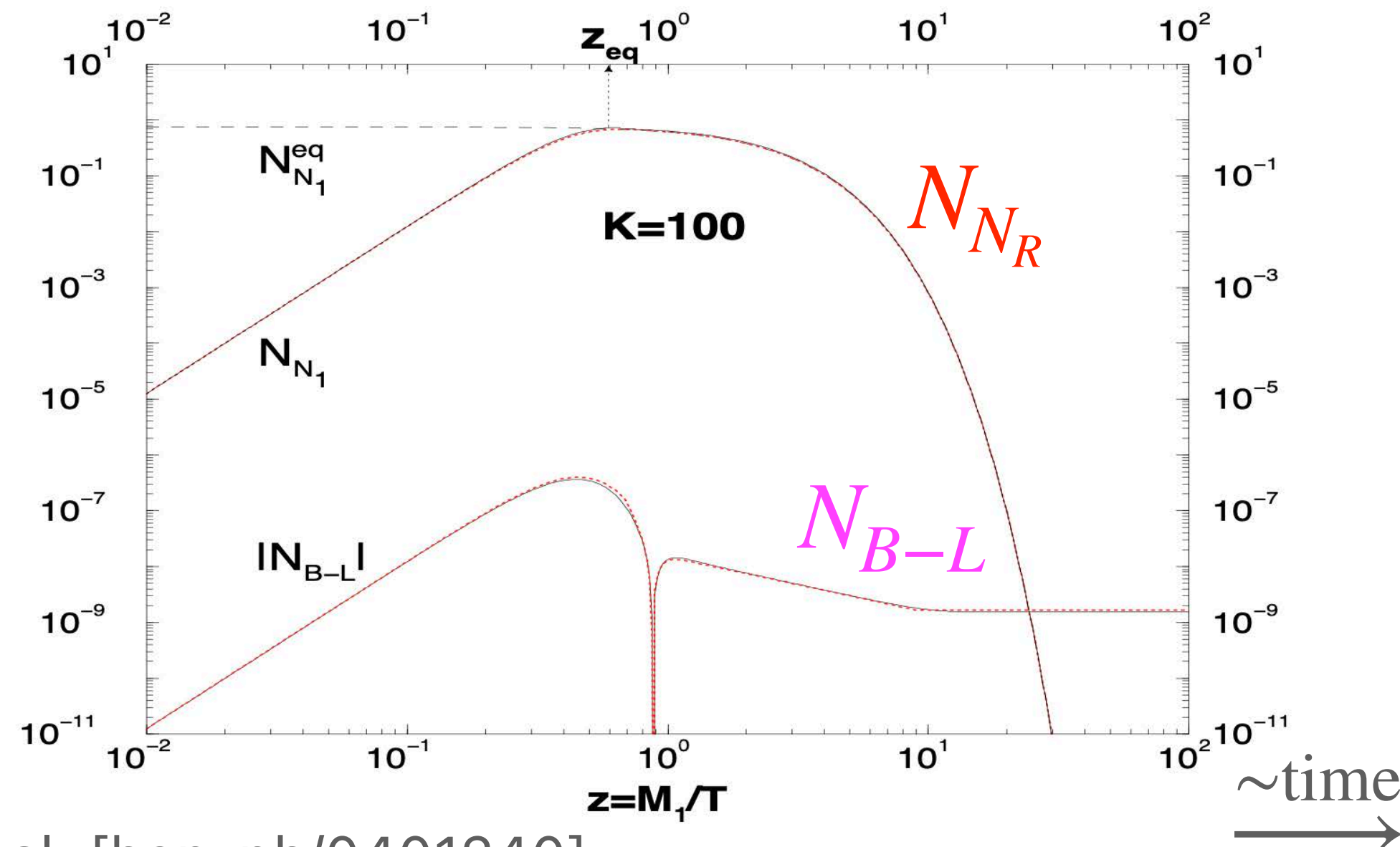
- **Model:** Standard Model + Right-handed neutrino (**very simple!**)

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \bar{N}_R (i\gamma^\mu \partial_\mu + M_{N_R}) N_R + y_\nu \bar{N}_R \ell_L H + h.c.$$

- **Boltzmann eqs.**

$$\frac{dN_{N_R}}{dz} = -D \left(N_{N_R} - N_{N_R}^{\text{eq}} \right)$$

$$\frac{dN_{B-L}}{dz} = \epsilon D \left(N_{N_R} - N_{N_R}^{\text{eq}} \right) - W N_{B-L}$$



- The observed baryon asymmetry can be explained if

$$M_{N_R} \gtrsim \mathcal{O}(10^9) \text{ GeV.}$$

• Fig. from Buchmuller et.al. [hep-ph/0401240]

Leptogenesis

[Fukugita, Yanagida, '86]

There are various versions...

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(+ many others ...)

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✧ All of them require L-number violation and predict **$0\nu\beta\beta$ decay**.
cf. **talk by Umehara-san** in the previous session.

Exception: "Dirac leptogenesis".
[Dick, Lindner, Ratz, Wright, 99,
Murayama, Pierce, 02]

Plan

- Leptogenesis

- ▶ Baryon Asymmetry of the Universe

- ▶ Why "Lepto"genesis?

- ▶ Seesaw and Leptogenesis in a "big picture"

- Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

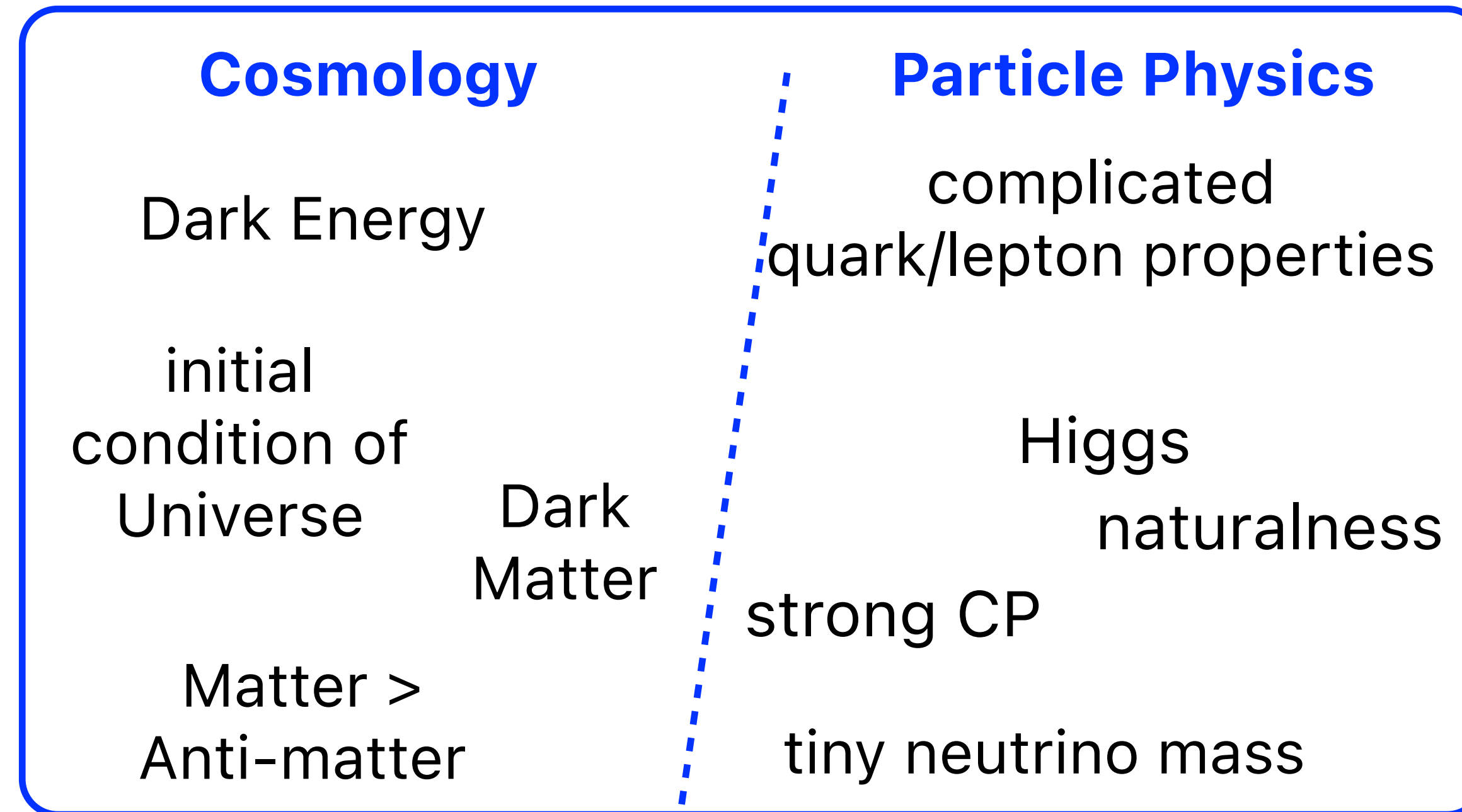
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Seesaw and Leptogenesis in a “big picture”

Seesaw and Leptogenesis in a “big picture”

Puzzles in the Standard Model

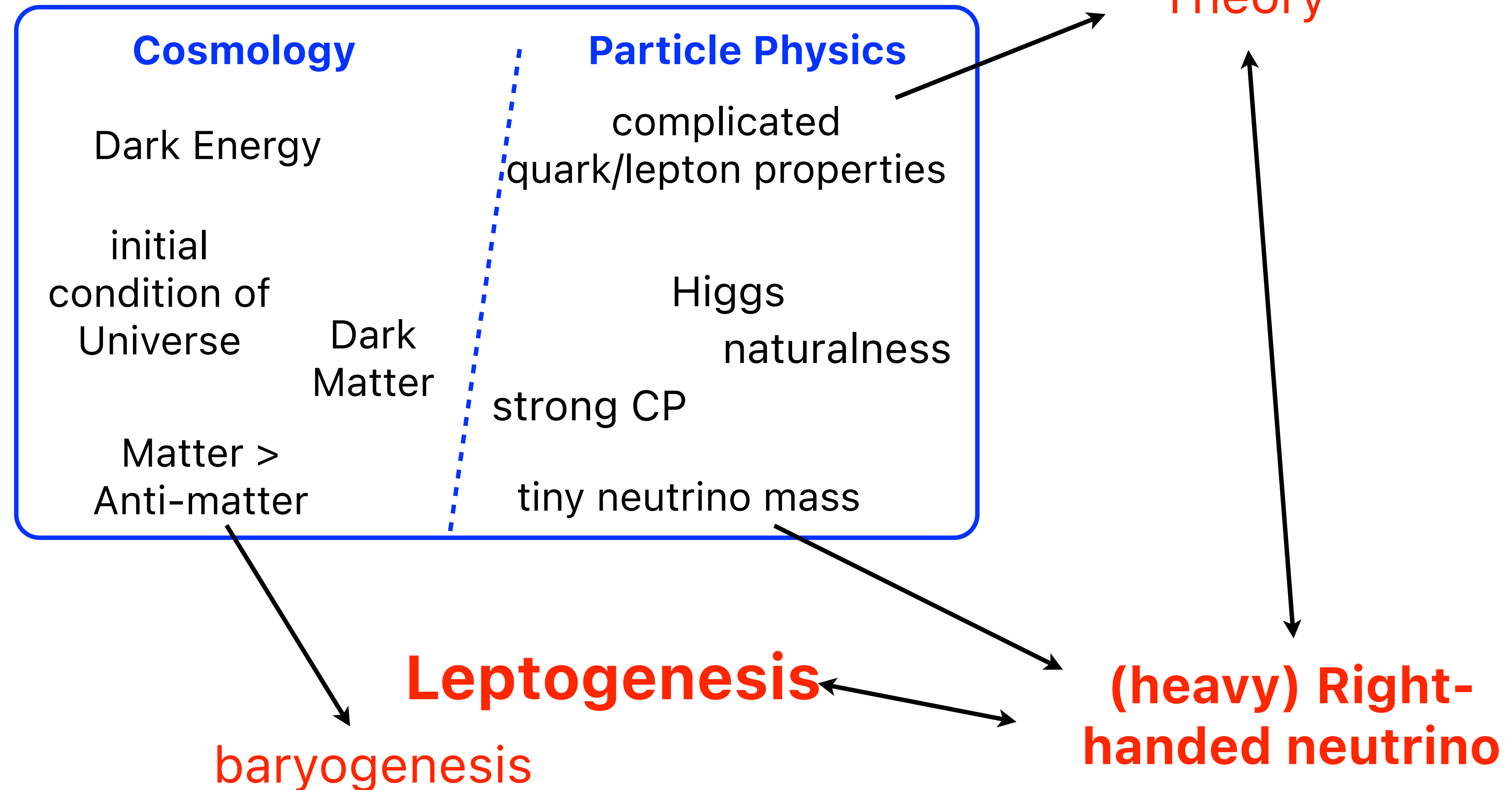
= Hints of Physics beyond the Standard Model



Seesaw and Leptogenesis in a "big picture"

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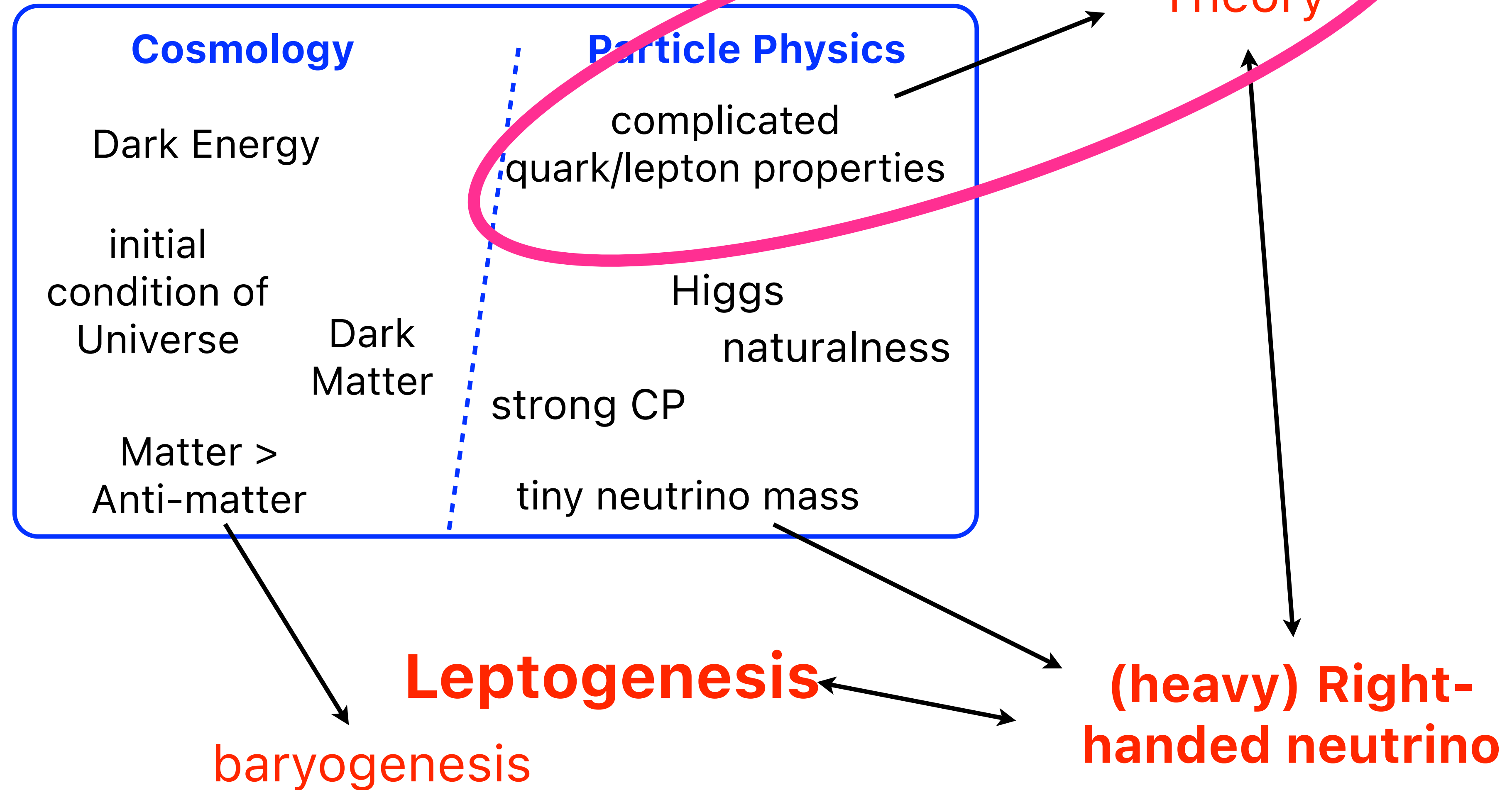
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Seesaw and Leptogenesis in a "big picture"

Puzzles in the Standard Model

= Hints of Physics beyond the Standard Model



Standard Model

left-handed
quark

right-handed
up quark

right-handed
down quark

left-handed
lepton

right-handed
lepton

$$\begin{pmatrix} \text{u} \\ \text{d} \end{pmatrix}_L$$

$$(3, 2)_{+1/6}$$

$$\text{u}_R$$

$$(\bar{3}, 1)_{-2/3}$$

$$\text{d}_R$$

$$(\bar{3}, 1)_{+1/3}$$

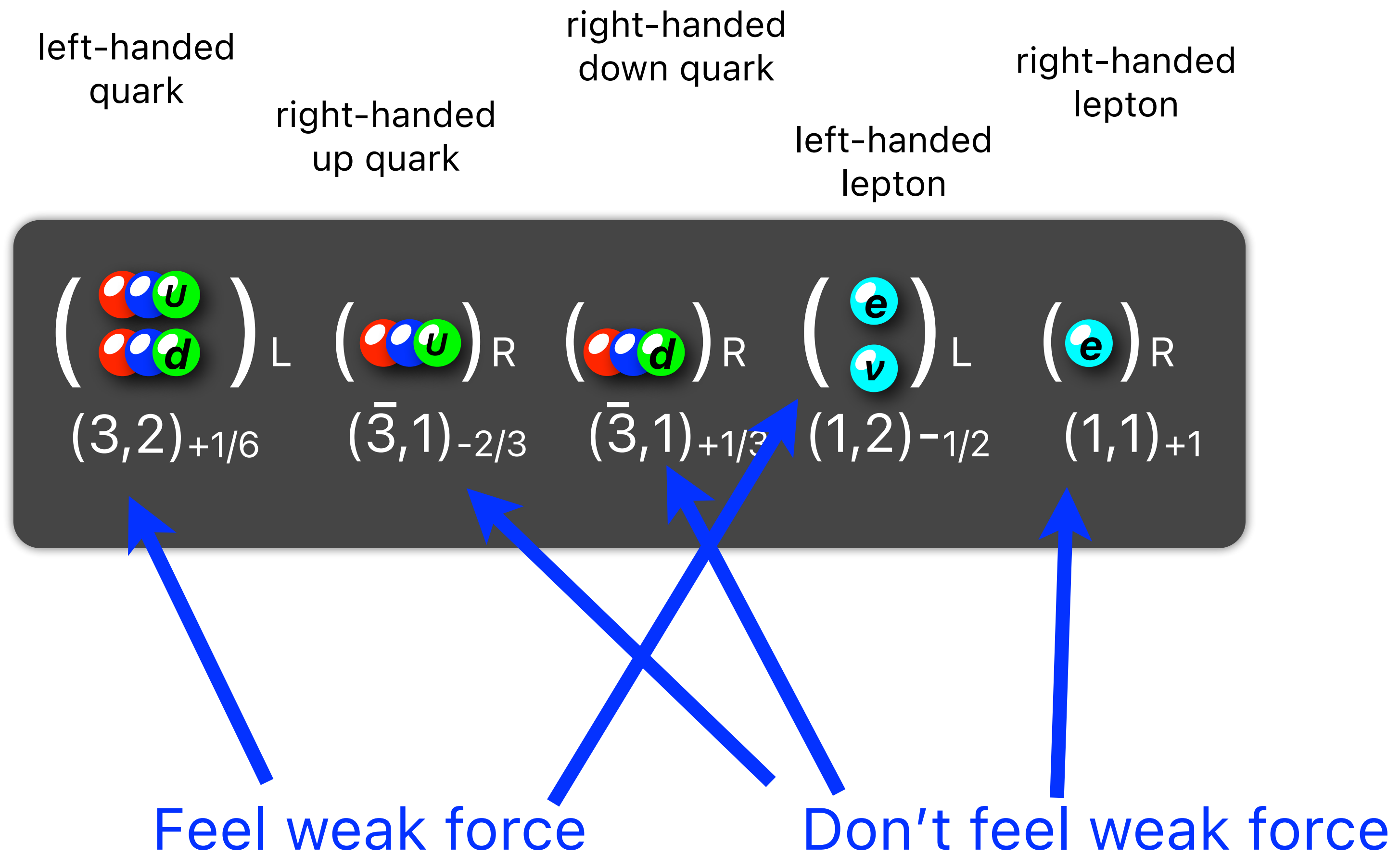
$$\begin{pmatrix} \text{e} \\ \nu \end{pmatrix}_L$$

$$(1, 2)_{-1/2}$$

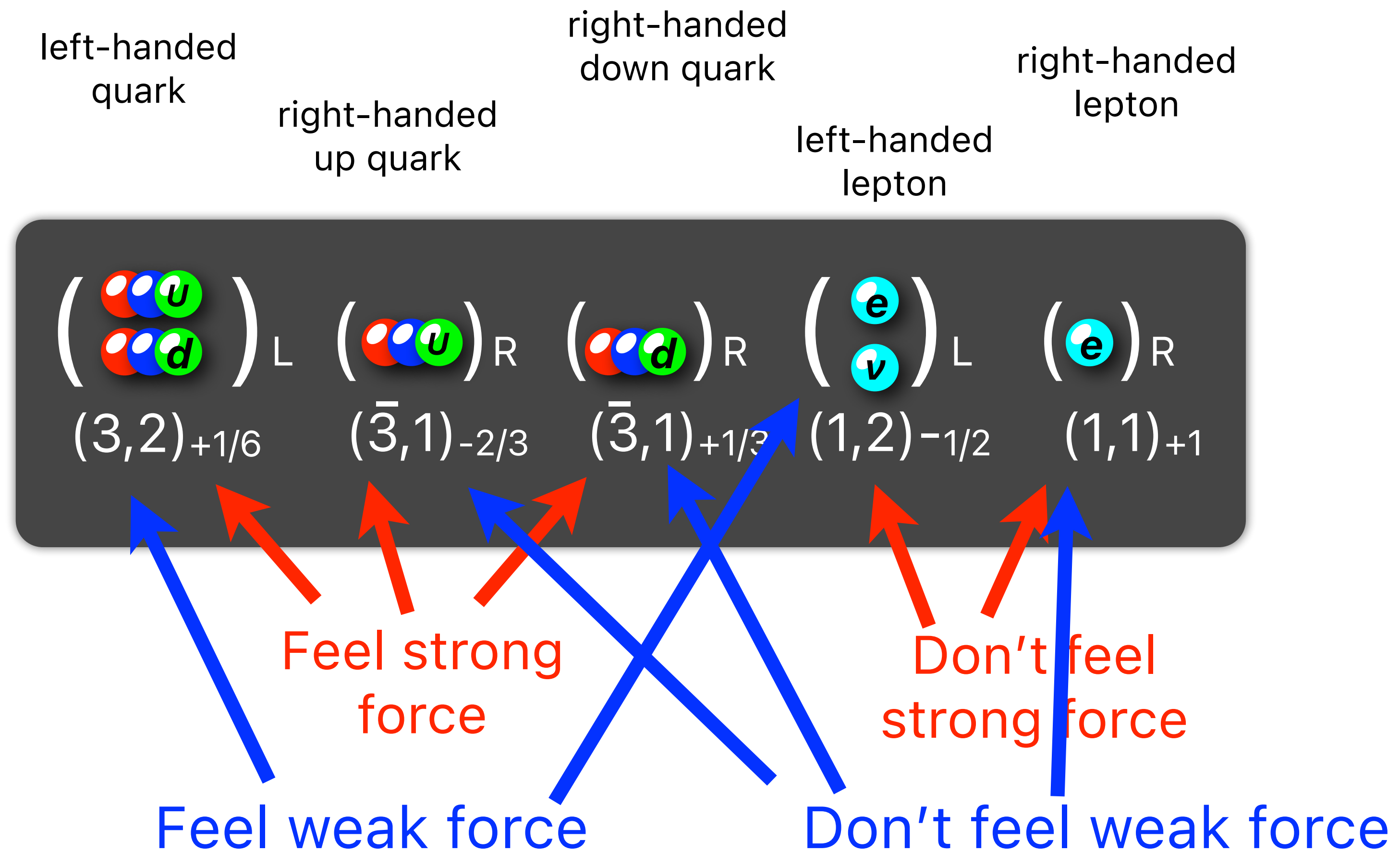
$$\text{e}_R$$

$$(1, 1)_{+1}$$

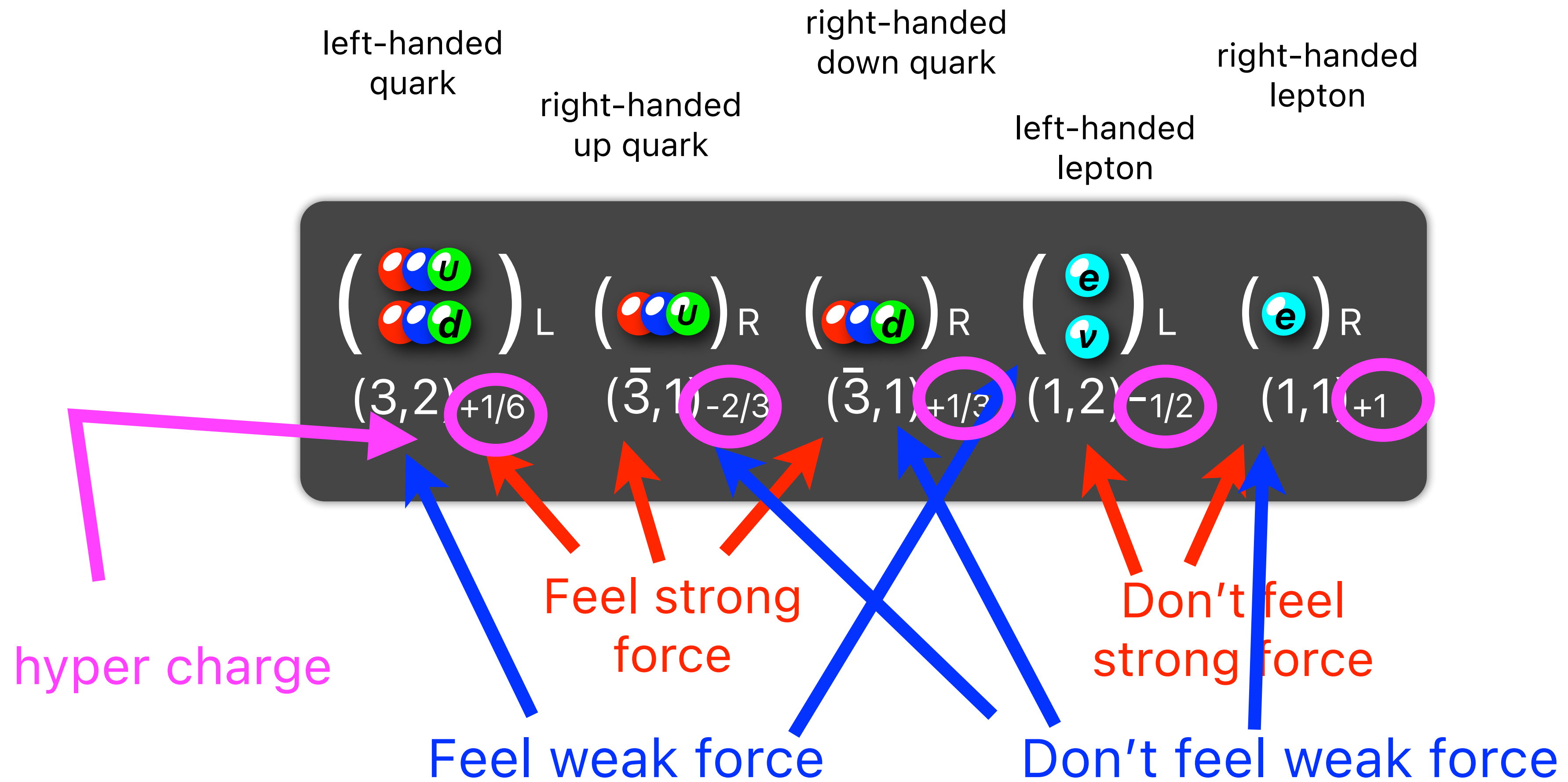
Standard Model



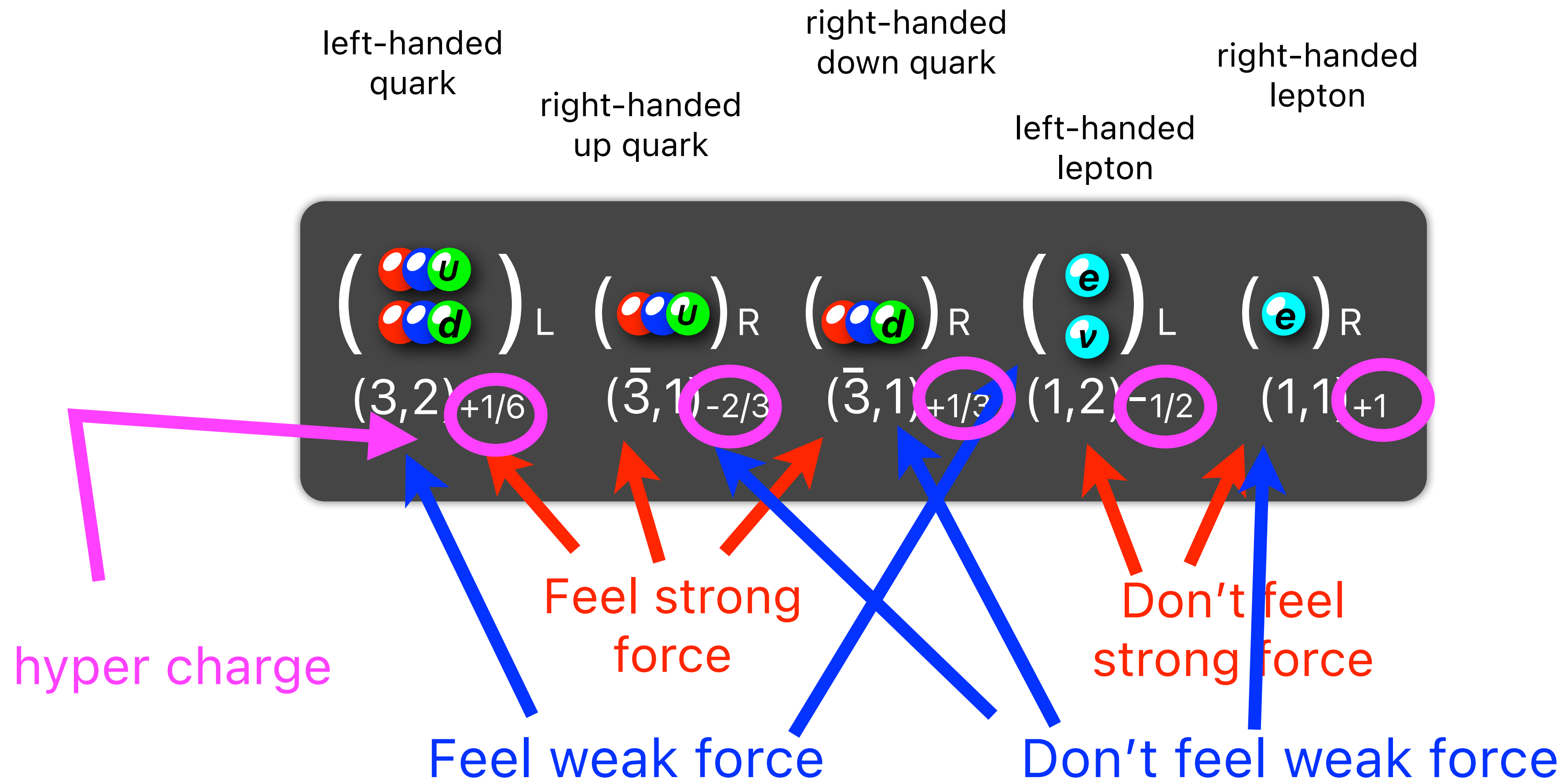
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Standard Model

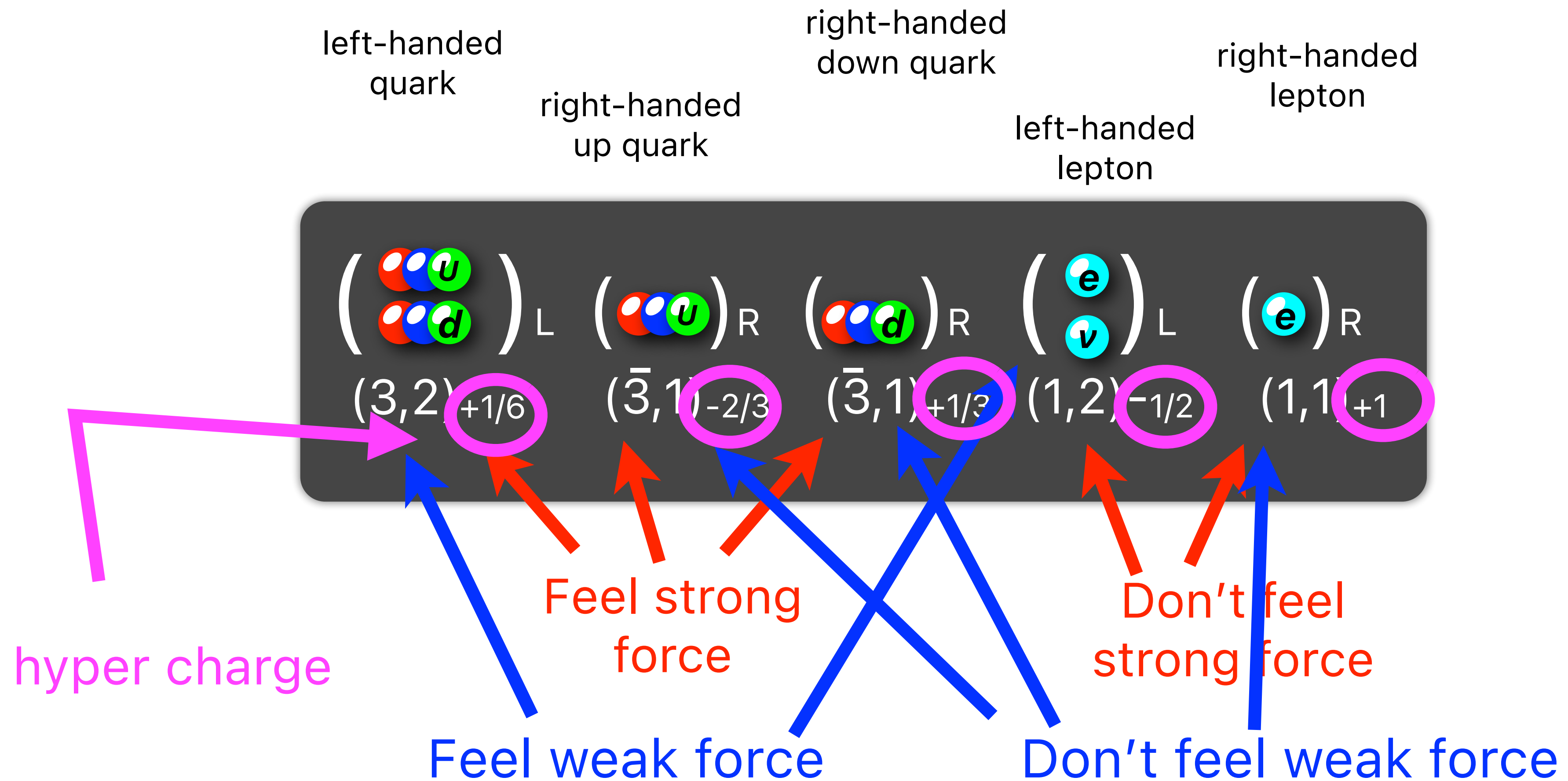


Standard Model



... very complicated !!

Standard Model



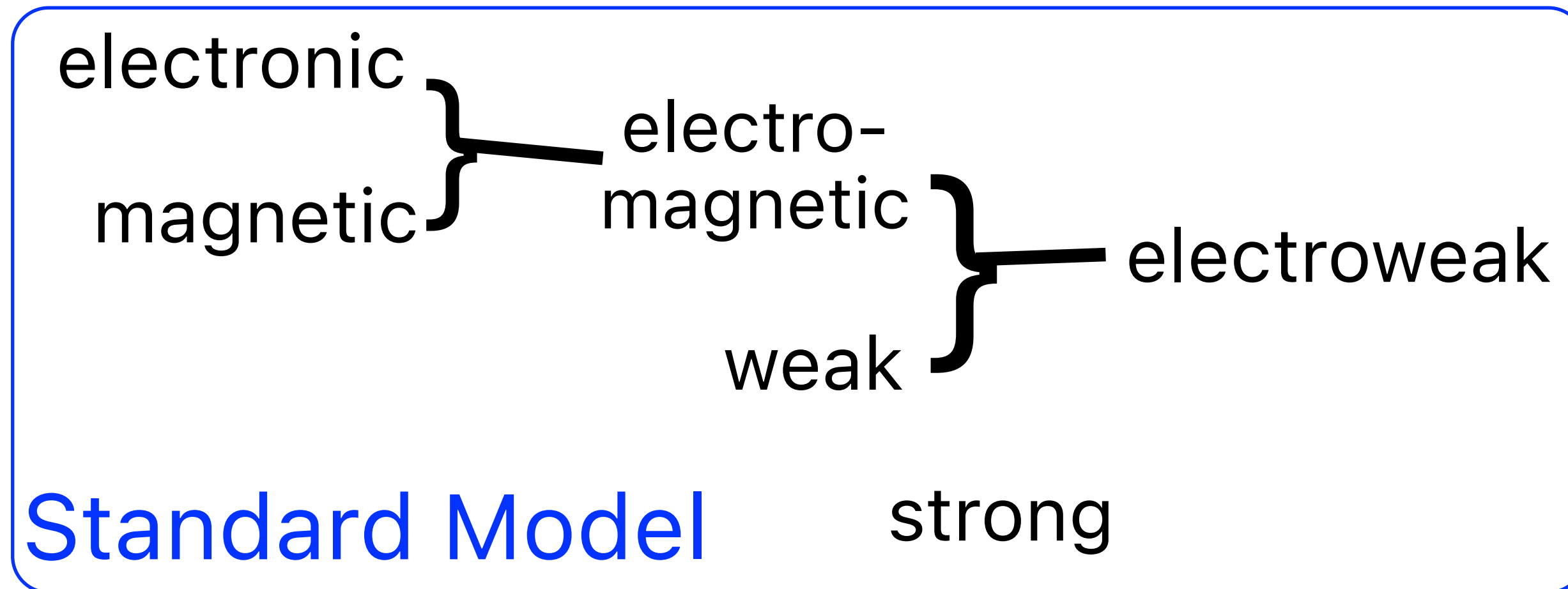
... very complicated !!

Q: any simple, unified theory to explain it?

Standard Model

$$\begin{array}{ccccc}
 \left(\begin{array}{c} u \\ d \end{array} \right)_L & \left(\begin{array}{c} u \\ d \end{array} \right)_R & \left(\begin{array}{c} u \\ d \end{array} \right)_R & \left(\begin{array}{c} e \\ \nu \end{array} \right)_L & \left(\begin{array}{c} e \\ \nu \end{array} \right)_R \\
 (3, 2)_{+1/6} & (\bar{3}, 1)_{-2/3} & (\bar{3}, 1)_{+1/3} & (1, 2)_{-1/2} & (1, 1)_{+1}
 \end{array}$$

Q: any simple, unified theory to explain it?

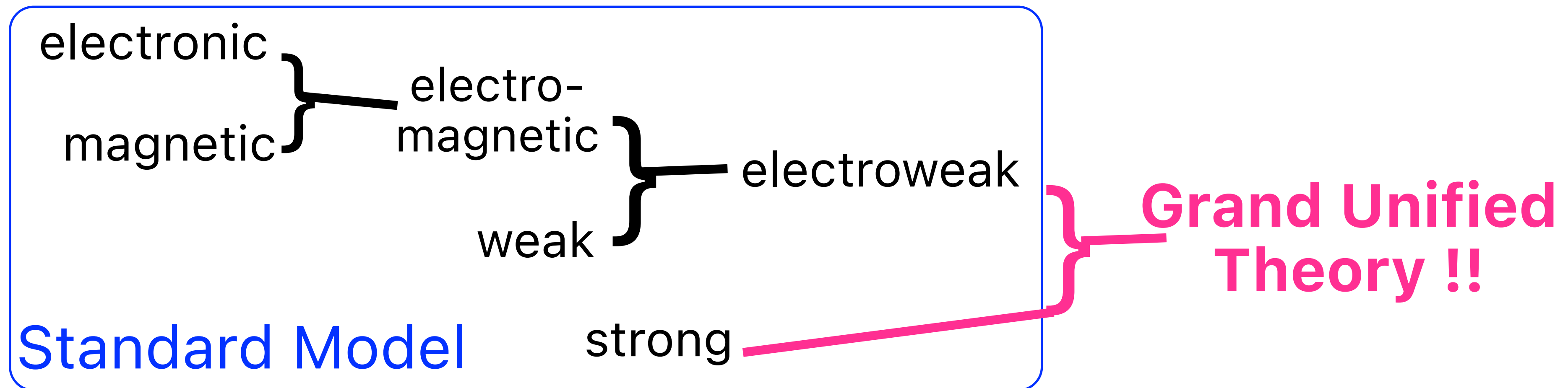


Standard Model

$$\begin{pmatrix} u \\ d \end{pmatrix}_L \quad \begin{pmatrix} u \\ d \end{pmatrix}_R \quad \begin{pmatrix} u \\ d \end{pmatrix}_R \quad \begin{pmatrix} e \\ \nu \end{pmatrix}_L \quad \begin{pmatrix} e \end{pmatrix}_R$$

$$(3, 2)_{+1/6} \quad (\bar{3}, 1)_{-2/3} \quad (\bar{3}, 1)_{+1/3} \quad (1, 2)_{-1/2} \quad (1, 1)_{+1}$$

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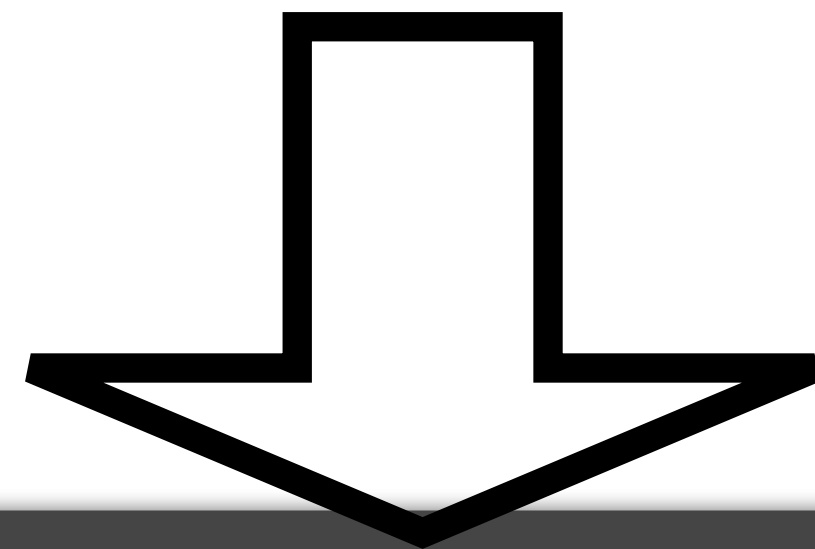


Standard Model

$$\begin{pmatrix} \begin{matrix} \text{u} \\ \text{d} \end{matrix} \\ \begin{matrix} \text{u} \\ \text{d} \end{matrix} \end{pmatrix}_L \quad \begin{pmatrix} \text{u} \\ \text{u} \end{pmatrix}_R \quad \begin{pmatrix} \text{d} \\ \text{d} \end{pmatrix}_R \quad \begin{pmatrix} \text{e} \\ \text{v} \end{pmatrix}_L \quad \begin{pmatrix} \text{e} \\ \text{e} \end{pmatrix}_R$$

$$(3, 2)_{+1/6} \quad (\bar{3}, 1)_{-2/3} \quad (\bar{3}, 1)_{+1/3} \quad (1, 2)_{-1/2} \quad (1, 1)_{+1}$$

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Grand Unified Theory

[SU(5) case]

$$\begin{pmatrix} \begin{matrix} \text{u} \\ \text{d} \\ \text{u} \\ \text{d} \\ \text{e} \end{matrix} \\ \begin{matrix} \text{u} \\ \text{d} \\ \text{e} \end{matrix} \end{pmatrix} \quad \begin{pmatrix} \text{e} \\ \text{v} \\ \text{d} \end{pmatrix}$$

$$10 \quad \bar{5}$$

... beautifully unified
into simple SU(5)
representations !

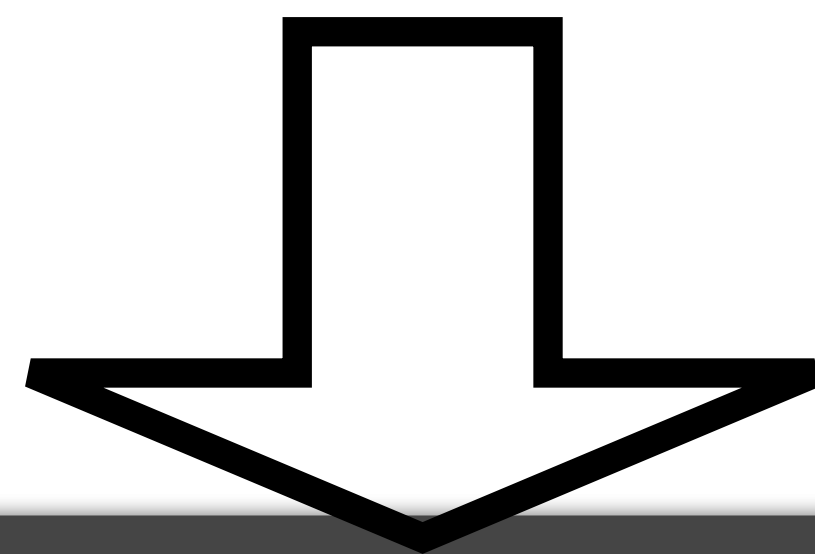
[Georgi, Glashow 1974]

Standard Model

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$$(3, 2)_{+1/6} \quad (\bar{3}, 1)_{-2/3} \quad (\bar{3}, 1)_{+1/3} \quad (1, 2)_{-1/2} \quad (1, 1)_{+1}$$

Q: any simple, unified theory to explain it?



$$1/3 + 1/3 + 1/3 - 1/2 - 1/2 = 0$$

Complicated numbers are naturally explained!

Grand Unified Theory

[SU(5) case]

$$\begin{pmatrix} u \\ d \end{pmatrix}_L \quad \begin{pmatrix} u \\ d \end{pmatrix}_R \quad e_R \quad \begin{pmatrix} e \\ \nu \end{pmatrix}_L \quad d_R$$

$$10 \quad \bar{5}$$

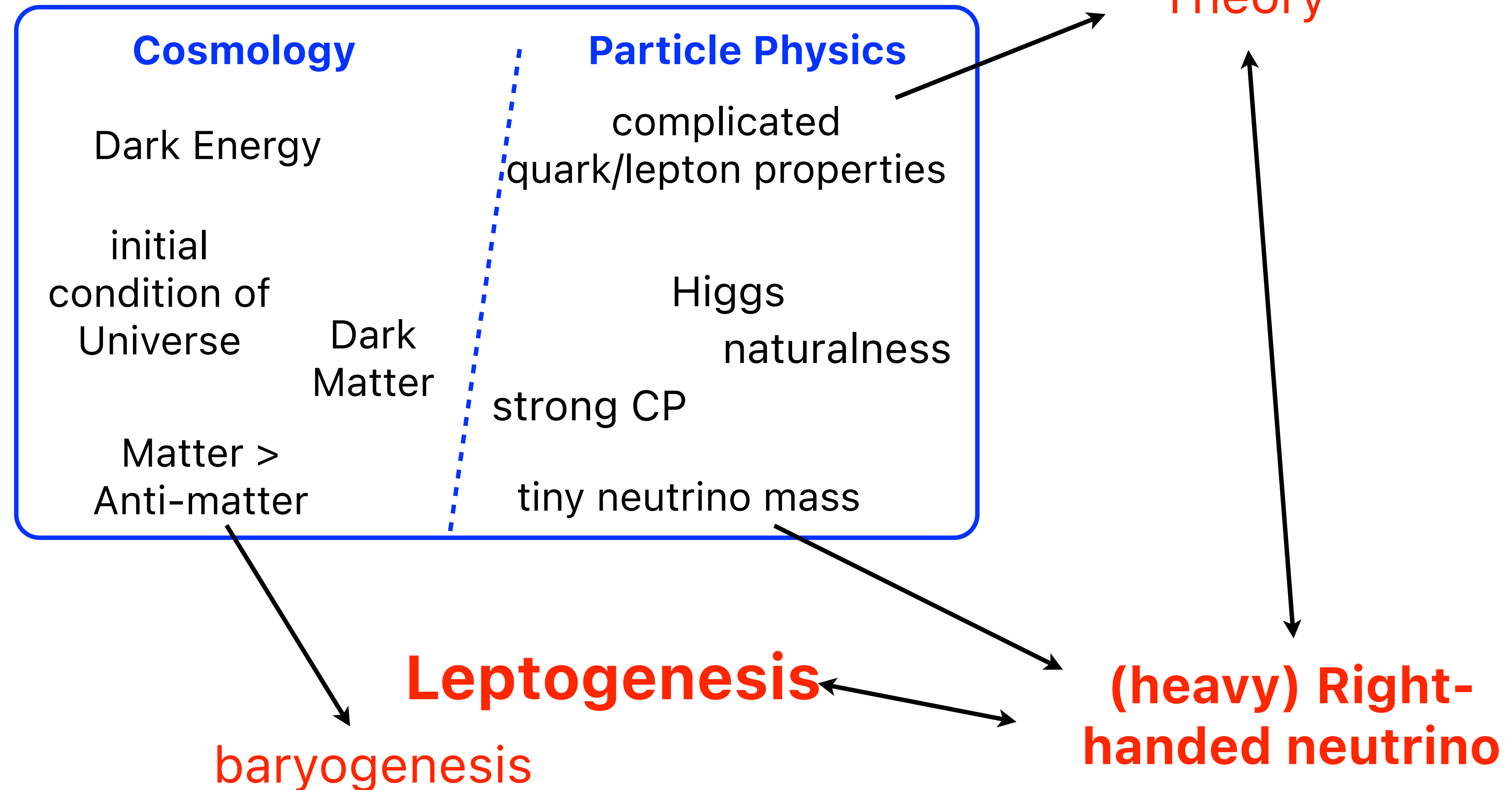
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[Georgi, Glashow 1974]

Seesaw and Leptogenesis in a "big picture"

Puzzles in the Standard Model

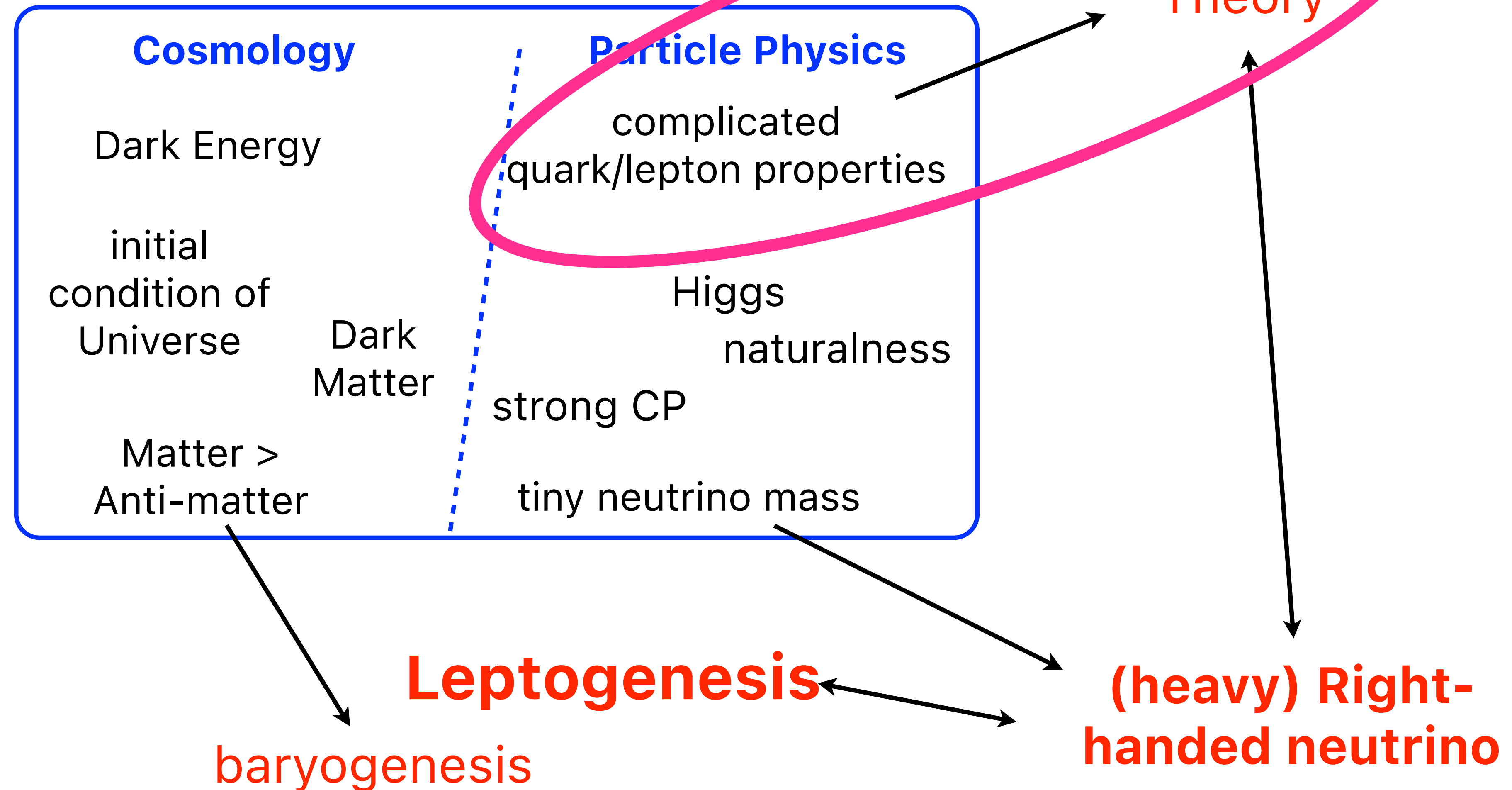
= Hints of Physics beyond the Standard Model



Seesaw and Leptogenesis in a "big picture"

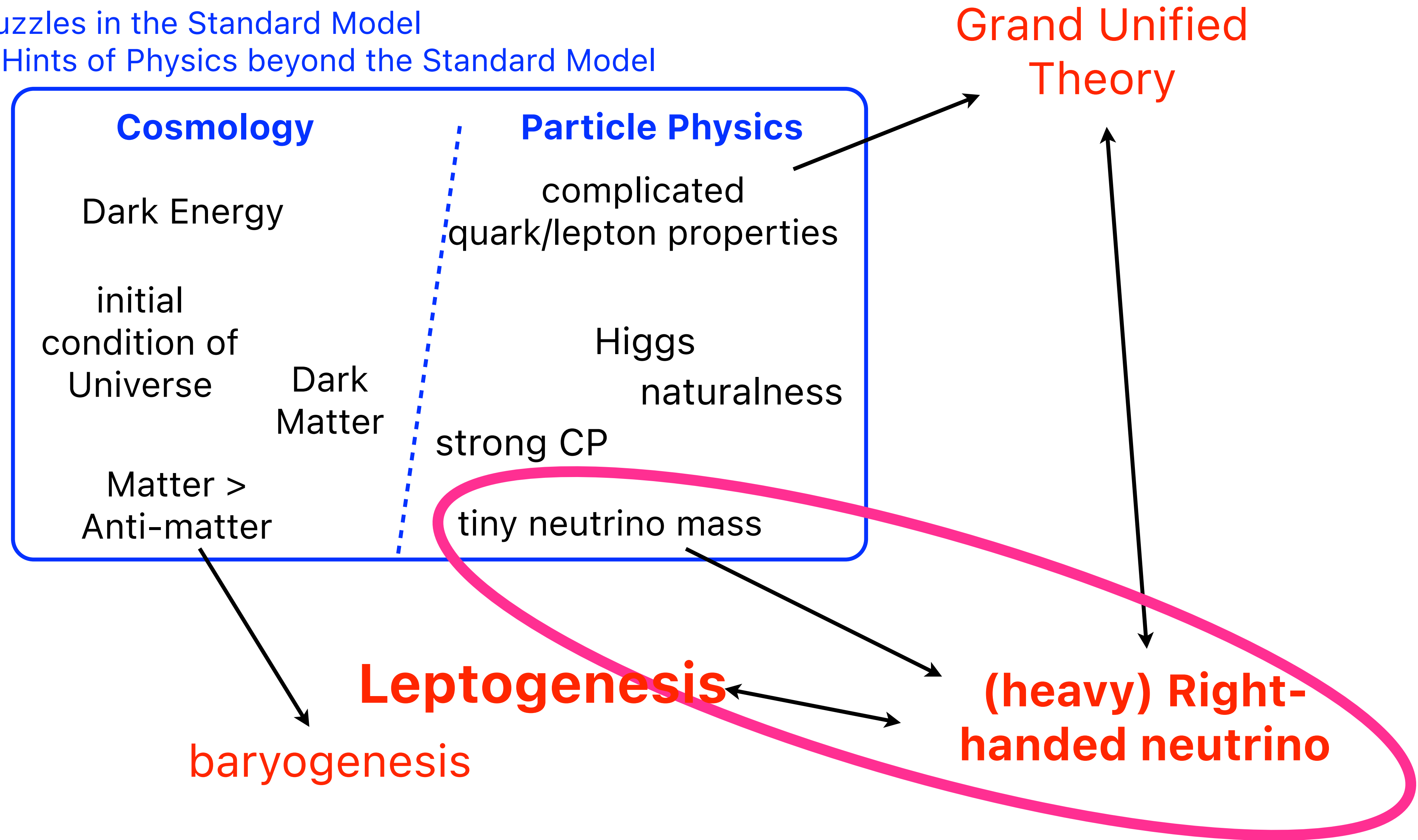
Puzzles in the Standard Model

= Hints of Physics beyond the Standard Model



Seesaw and Leptogenesis in a "big picture"

Puzzles in the Standard Model
= Hints of Physics beyond the Standard Model



puzzle: neutrino masses

$\begin{pmatrix} u \\ d \end{pmatrix}_L$ $(\bar{3}, 1)_{-2/3}$ $(\bar{3}, 1)_{+1/3}$ $\begin{pmatrix} e \\ \nu \end{pmatrix}_L$ $(1, 1)_{+1}$

$(3, 2)_{+1/6}$ $(\bar{3}, 1)_{-2/3}$ $(\bar{3}, 1)_{+1/3}$ $(1, 2)_{-1/2}$ $(1, 1)_{+1}$

left-handed
quark

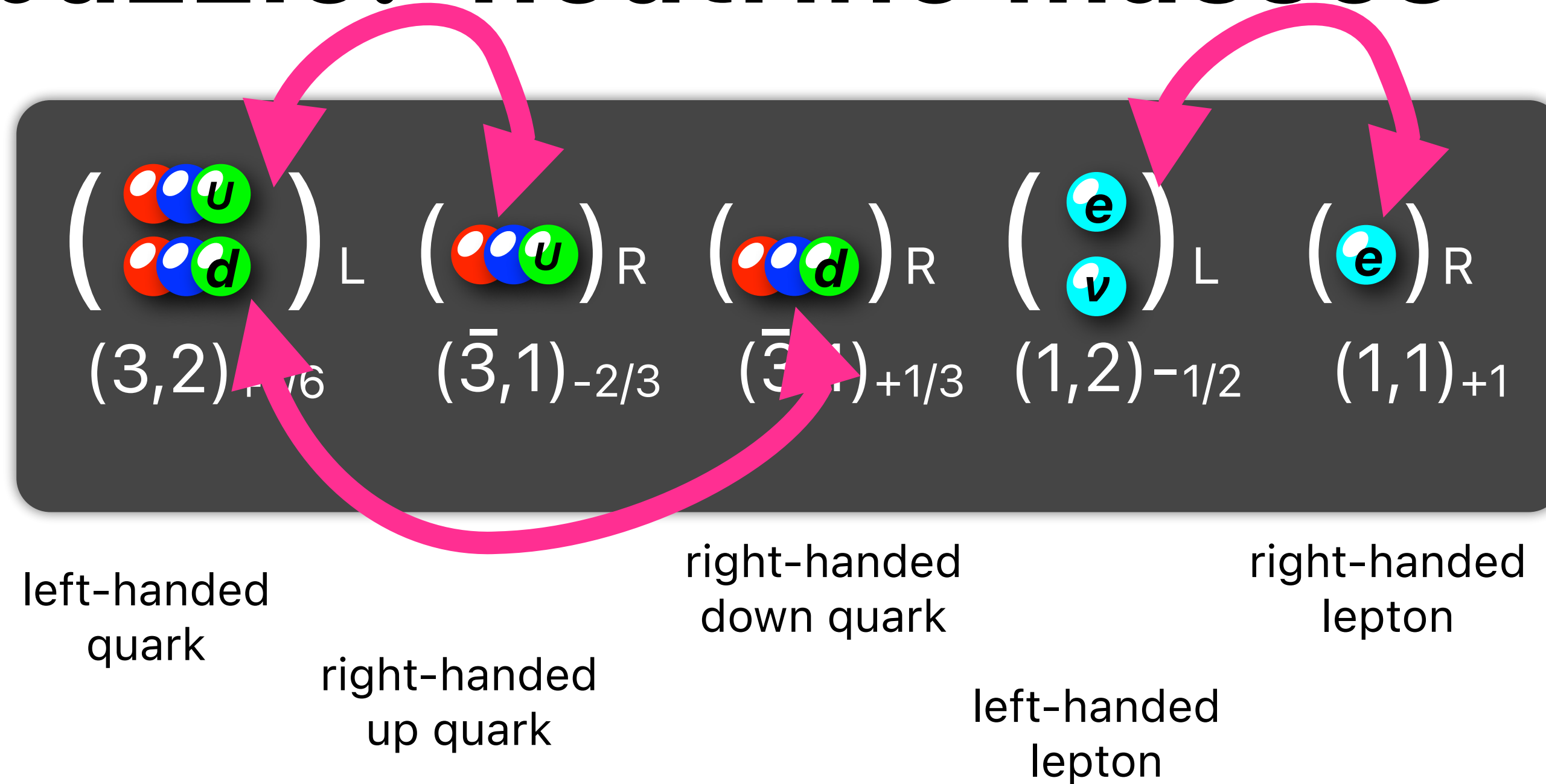
right-handed
up quark

right-handed
down quark

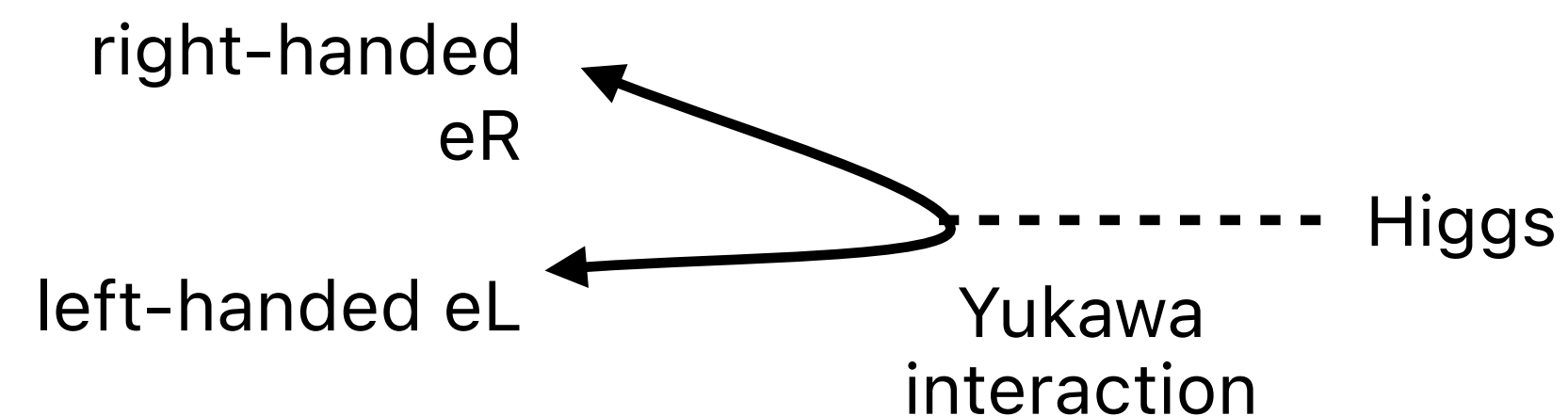
left-handed
lepton

right-handed
lepton

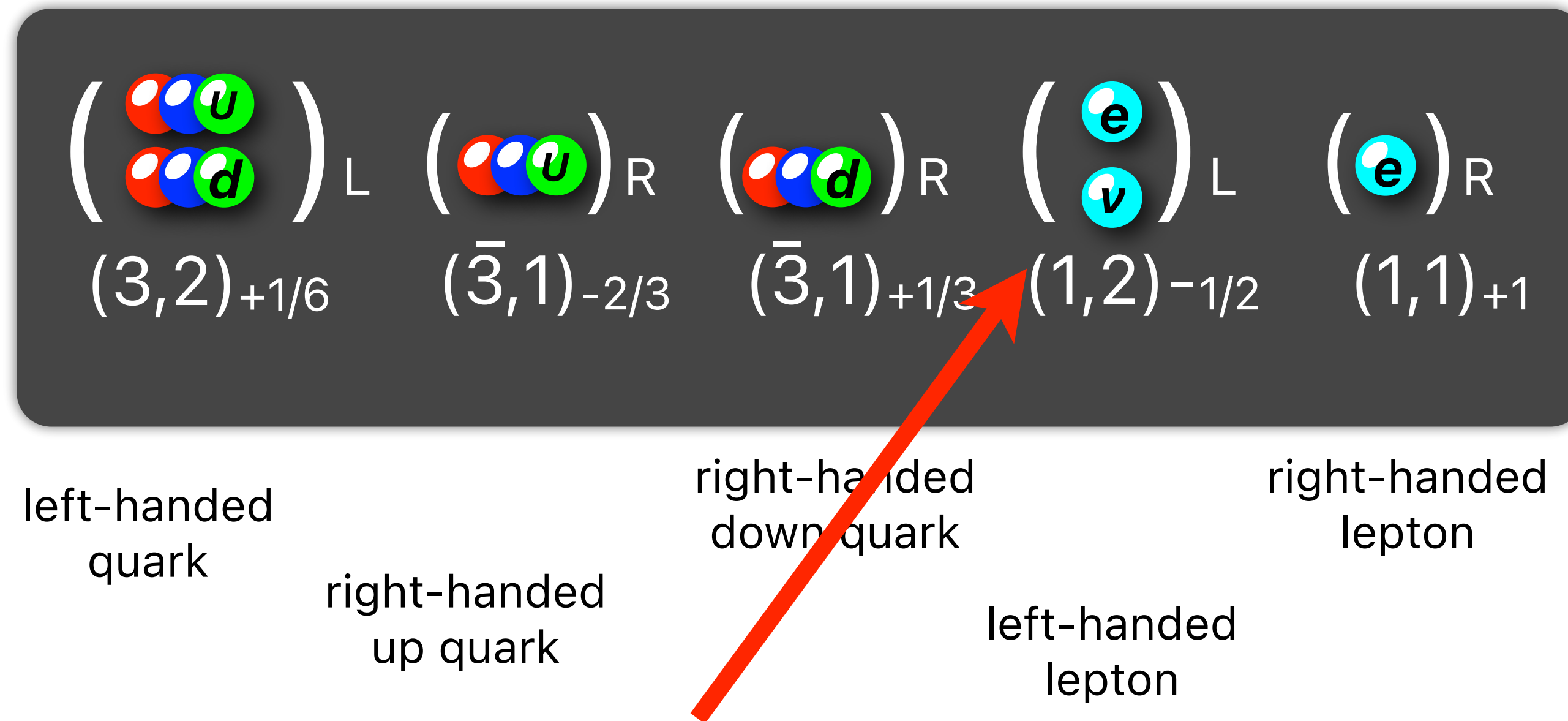
puzzle: neutrino masses



Quarks and leptons have masses by combining left- and right-handed components (via Higgs, Yukawa interaction).



puzzle: neutrino masses



The neutrino has only left-handed component.

==> Massless !!

But the neutrino masses are confirmed by neutrino oscillations.

puzzle: neutrino masses

$$\begin{array}{ccccc} \left(\begin{array}{c} u \\ d \end{array} \right)_L & \left(u \right)_R & \left(d \right)_R & \left(\begin{array}{c} e \\ \nu \end{array} \right)_L & \left(e \right)_R \\ (3,2)_{+1/6} & (\bar{3},1)_{-2/3} & (\bar{3},1)_{+1/3} & (1,2)_{-1/2} & (1,1)_{+1} \end{array}$$

left-handed
quark

right-handed
up quark

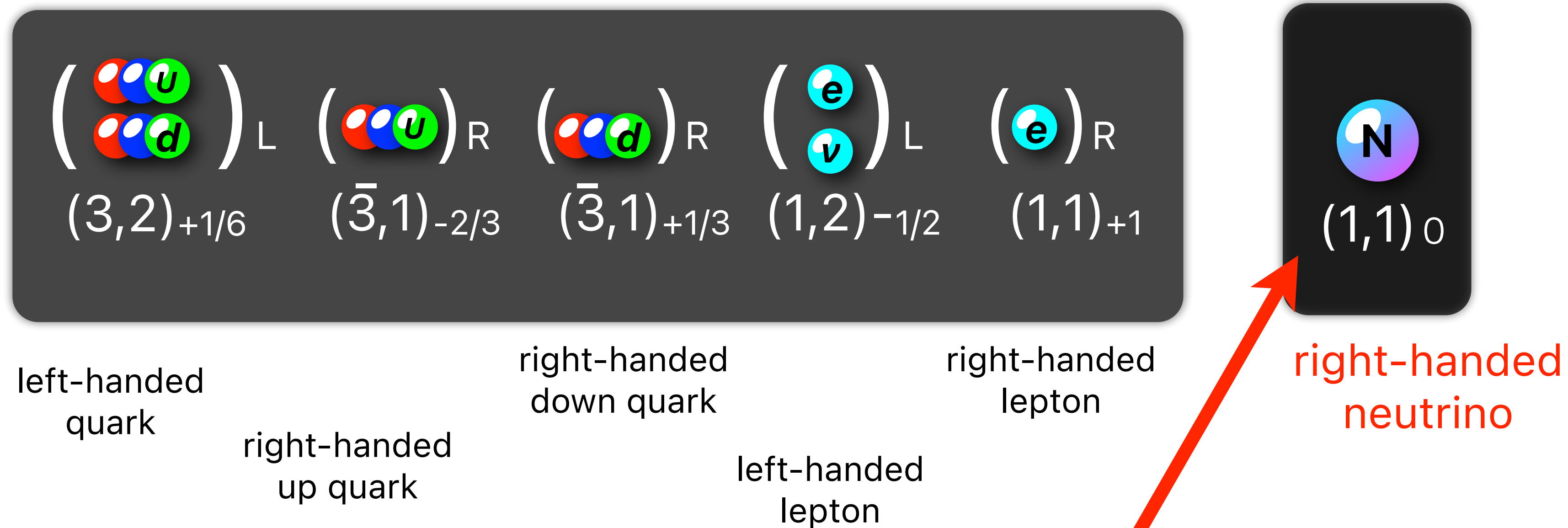
right-handed
down quark

left-handed
lepton

right-handed
lepton

a solution is ...

puzzle: neutrino masses



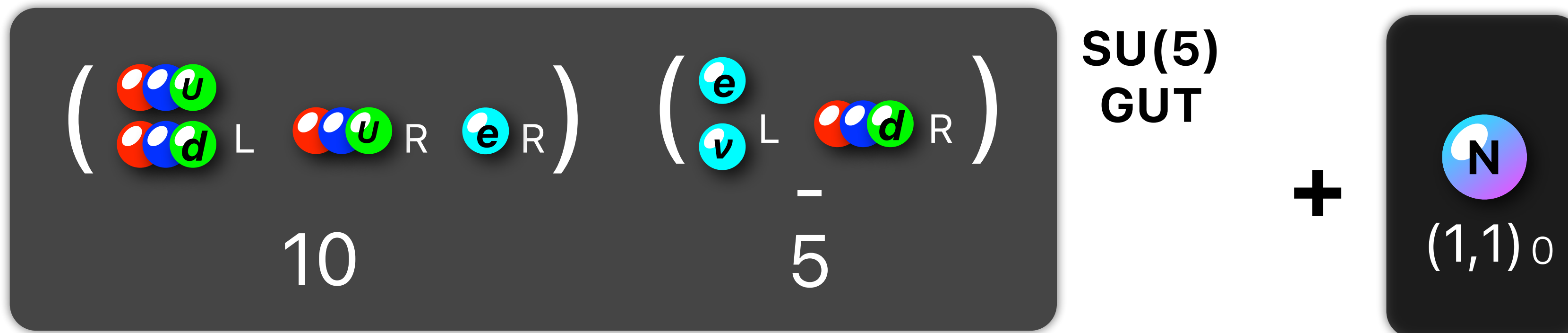
a solution is ...

To add a right-handed neutrino !!

The right-handed neutrino  plays a triple role.

The right-handed neutrino plays a triple role.

① quarks and leptons completely unified



The right-handed neutrino plays a triple role.

① quarks and leptons completely unified

$$\left(\begin{array}{ccc} \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} u_L & \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} u_R & e_R \\ \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} d_L & \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} d_R & \end{array} \right) \quad \left(\begin{array}{cc} e & \\ \nu & \end{array} \right) \quad \begin{array}{l} \text{SU(5)} \\ \text{GUT} \\ 10 \quad -5 \end{array} + \begin{array}{c} \text{N} \\ (1,1)_0 \end{array}$$

$$= \left(\begin{array}{cccccc} \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} u_L & \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} u_R & e_R & e & \nu_L & \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} d_R & N_1 R \\ \begin{array}{c} \color{red}\bullet \color{blue}\bullet \color{green}\bullet \\ \color{red}\bullet \color{blue}\bullet \color{green}\bullet \end{array} d_L & & & & & & \end{array} \right) \quad \begin{array}{l} \text{SO(10)} \\ \text{GUT} \\ 16 \end{array} \quad \begin{array}{l} \text{[Georgi,74} \\ \text{Fritzsch, Minkowski,75]} \end{array}$$

All quarks and leptons unified !

The right-handed neutrino N plays a triple role.

① quarks and leptons completely unified

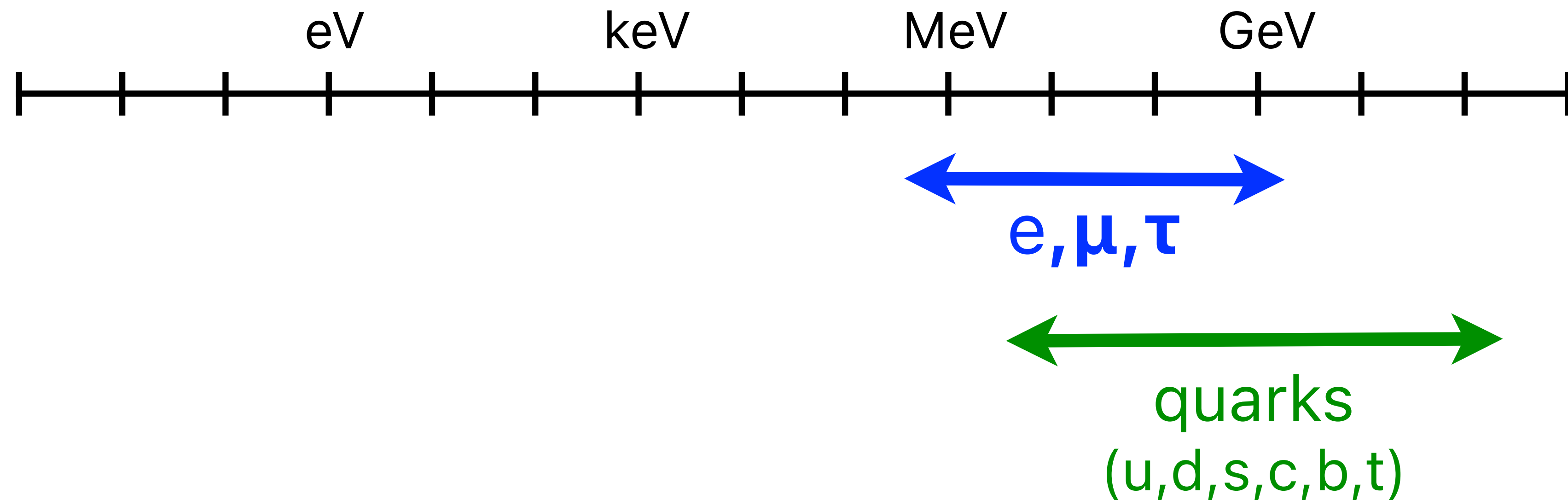
$$= \left(\begin{array}{cccccc} \begin{array}{c} \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \\ \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \end{array} \begin{array}{c} u \\ d \end{array} \text{L} & \begin{array}{c} \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \\ \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \end{array} \begin{array}{c} u \\ d \end{array} \text{R} & \begin{array}{c} \color{cyan}{\bullet} \\ \color{cyan}{\bullet} \end{array} \begin{array}{c} e \\ \nu \end{array} \text{R} & \begin{array}{c} \color{cyan}{\bullet} \\ \color{cyan}{\bullet} \end{array} \begin{array}{c} e \\ \nu \end{array} \text{L} & \begin{array}{c} \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \\ \color{red}{\bullet} \color{blue}{\bullet} \color{green}{\bullet} \end{array} \begin{array}{c} u \\ d \end{array} \text{R} & \begin{array}{c} \color{purple}{\bullet} \\ \color{purple}{\bullet} \end{array} \begin{array}{c} N_1 \\ N_2 \end{array} \text{R} \end{array} \right) = \begin{array}{c} (\uparrow \downarrow \downarrow \downarrow \uparrow) \\ (\uparrow \downarrow \downarrow \uparrow \downarrow) \\ (\uparrow \downarrow \uparrow \downarrow \downarrow) \\ (\downarrow \uparrow \downarrow \downarrow \uparrow) \\ (\downarrow \uparrow \downarrow \uparrow \downarrow) \\ (\downarrow \uparrow \uparrow \downarrow \downarrow) \\ (\uparrow \uparrow \uparrow \uparrow \downarrow) \\ (\uparrow \uparrow \uparrow \downarrow \uparrow) \\ (\uparrow \uparrow \downarrow \uparrow \uparrow) \\ (\downarrow \downarrow \uparrow \uparrow \downarrow) \\ (\downarrow \downarrow \uparrow \downarrow \uparrow) \\ (\downarrow \downarrow \downarrow \uparrow \uparrow) \\ (\uparrow \downarrow \uparrow \uparrow \uparrow) \\ (\downarrow \uparrow \uparrow \uparrow \uparrow) \\ (\uparrow \uparrow \downarrow \downarrow \downarrow) \\ (\downarrow \downarrow \downarrow \downarrow \downarrow) \end{array}$$

16

The right-handed neutrino plays a triple role.

② explains **tiny** neutrino mass

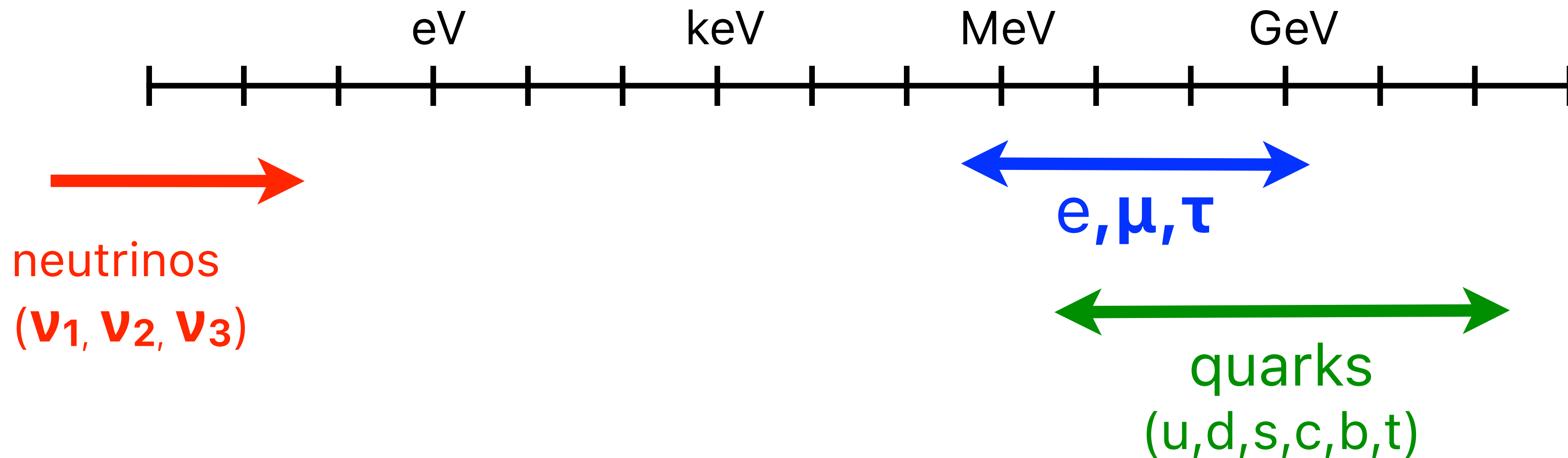
masses of quarks and leptons



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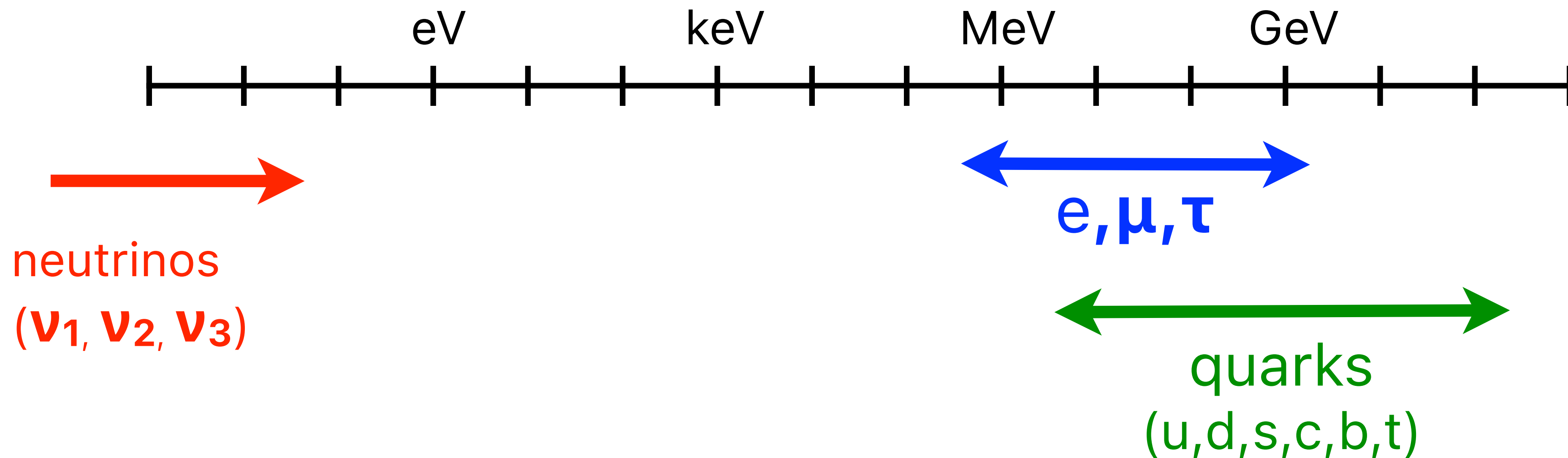
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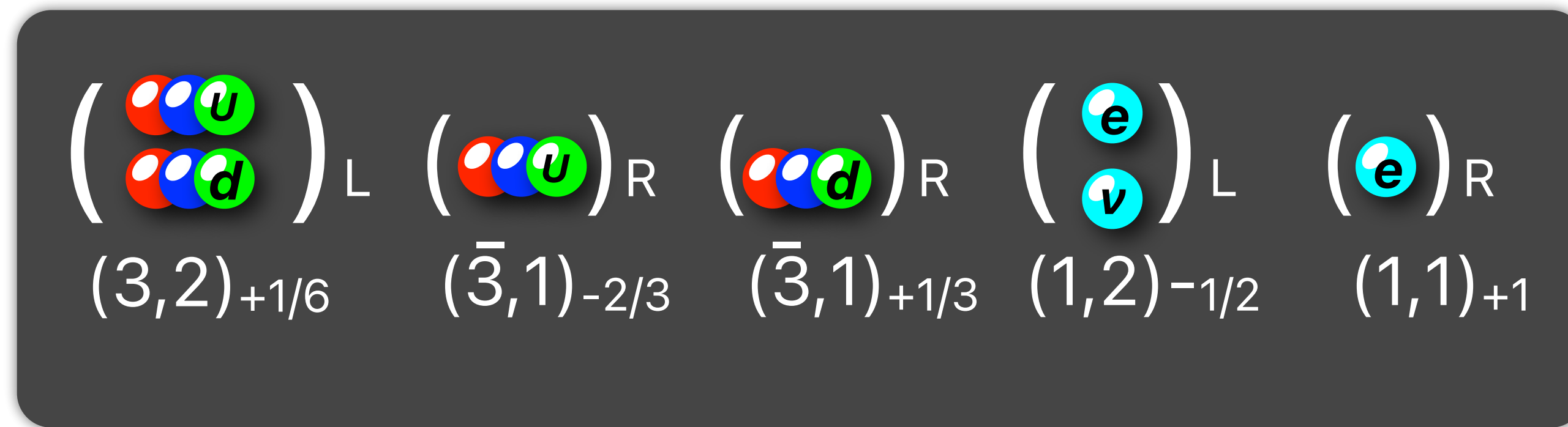
masses of quarks and leptons



- • • why neutrino masses are so small??

The right-handed neutrino plays a triple role.

② explains **tiny** neutrino mass



left-handed
quark

right-handed
up quark

right-handed
down quark

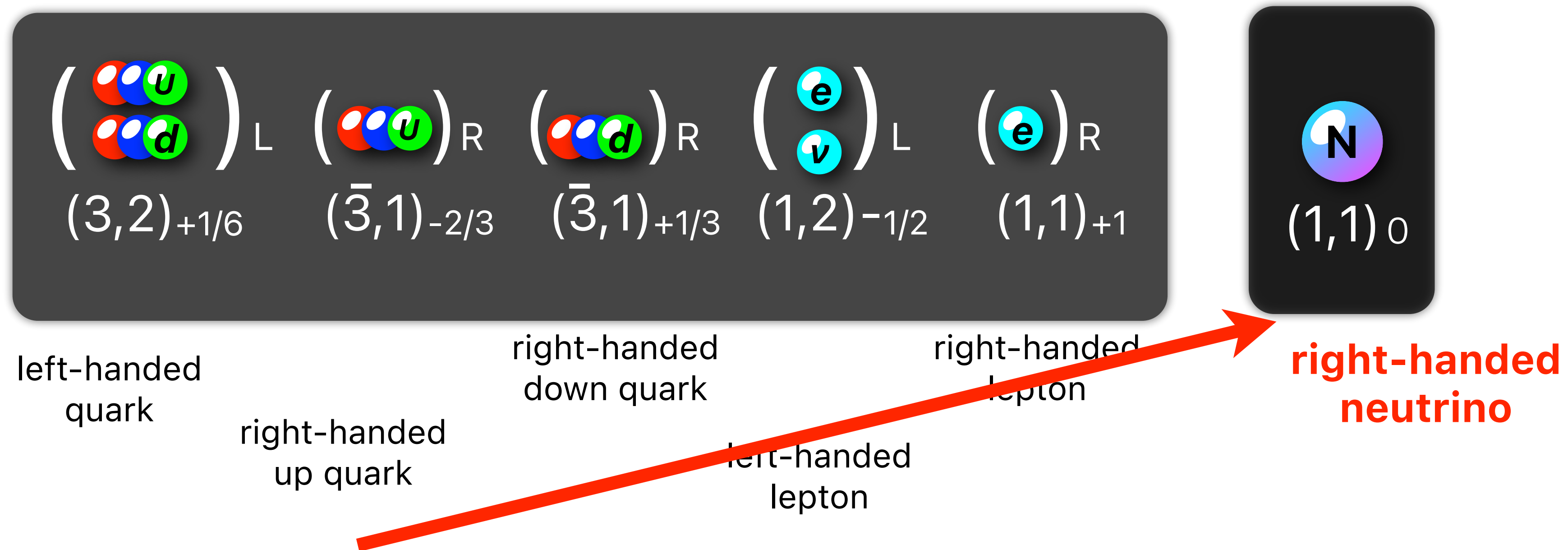
left-handed
lepton

right-handed
lepton

**right-handed
neutrino**

The right-handed neutrino plays a triple role.

② explains **tiny** neutrino mass



This guy is special singlet (feels none of three (EM, weak, and strong) forces.)

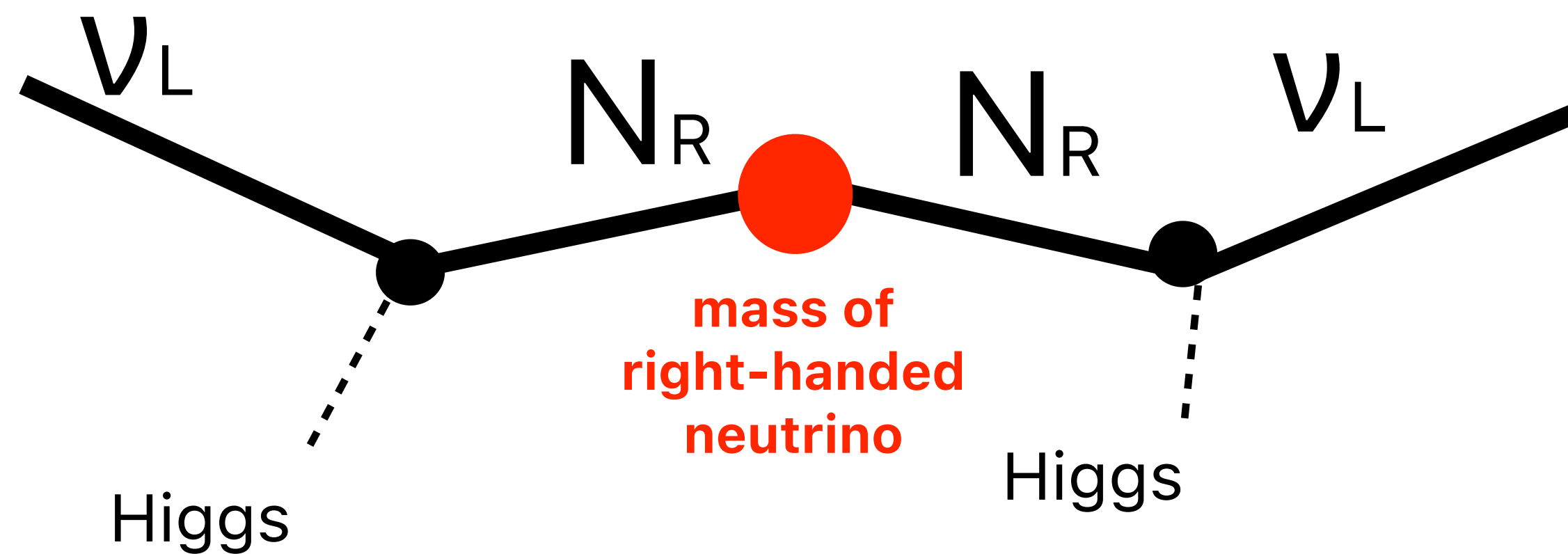
→ it has no charge.

→ it can be its own anti-particle (Majorana particle).

→ it can have a mass without Higgs VEV.

The right-handed neutrino plays a triple role.

② explains **tiny** neutrino mass

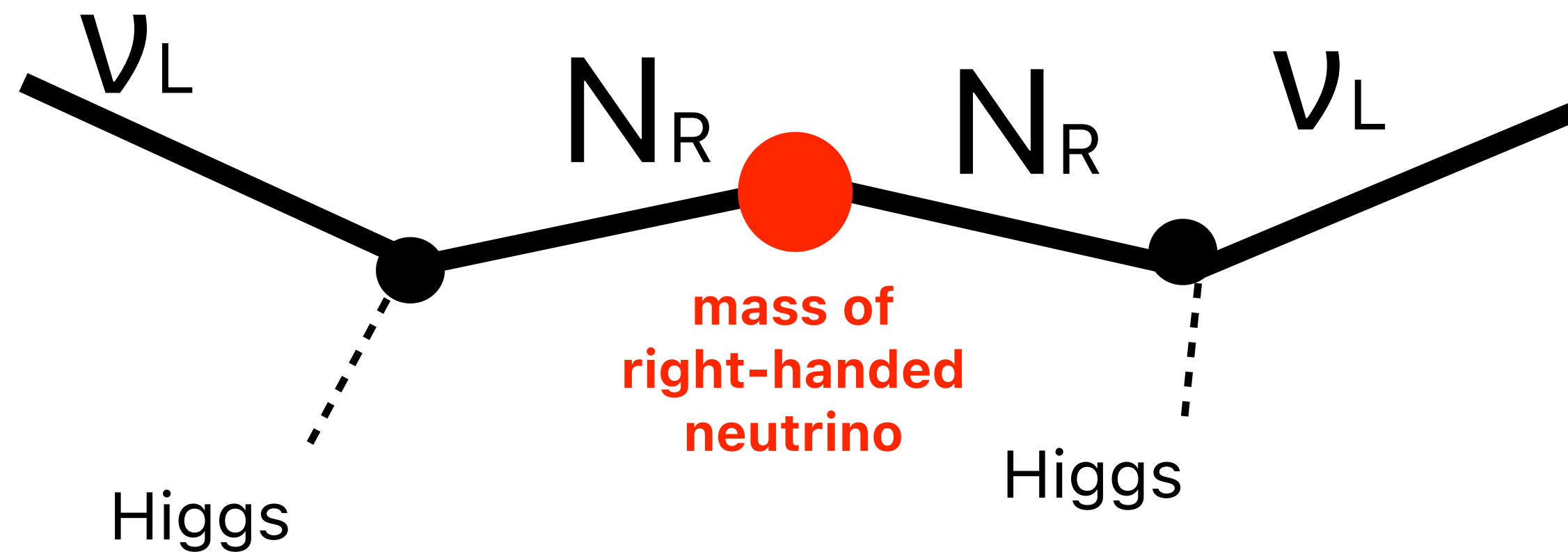


$$\text{Neutrino mass (seen e.g., by oscillation exp.)} = \frac{(\sim \text{Higgs VEV})^2}{\text{mass of right-handed neutrino}}$$

heavy R.H.v \rightarrow small neutrino masses ("see-saw mechanism")

The right-handed neutrino plays a triple role.

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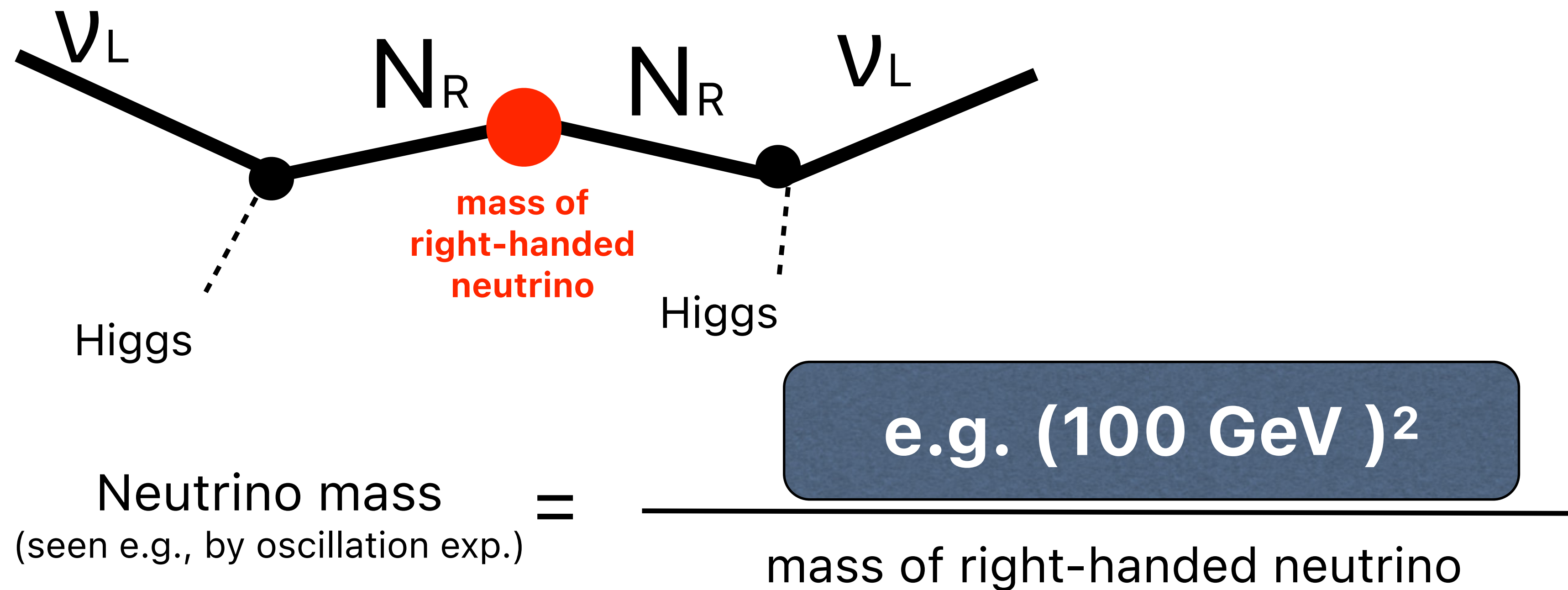


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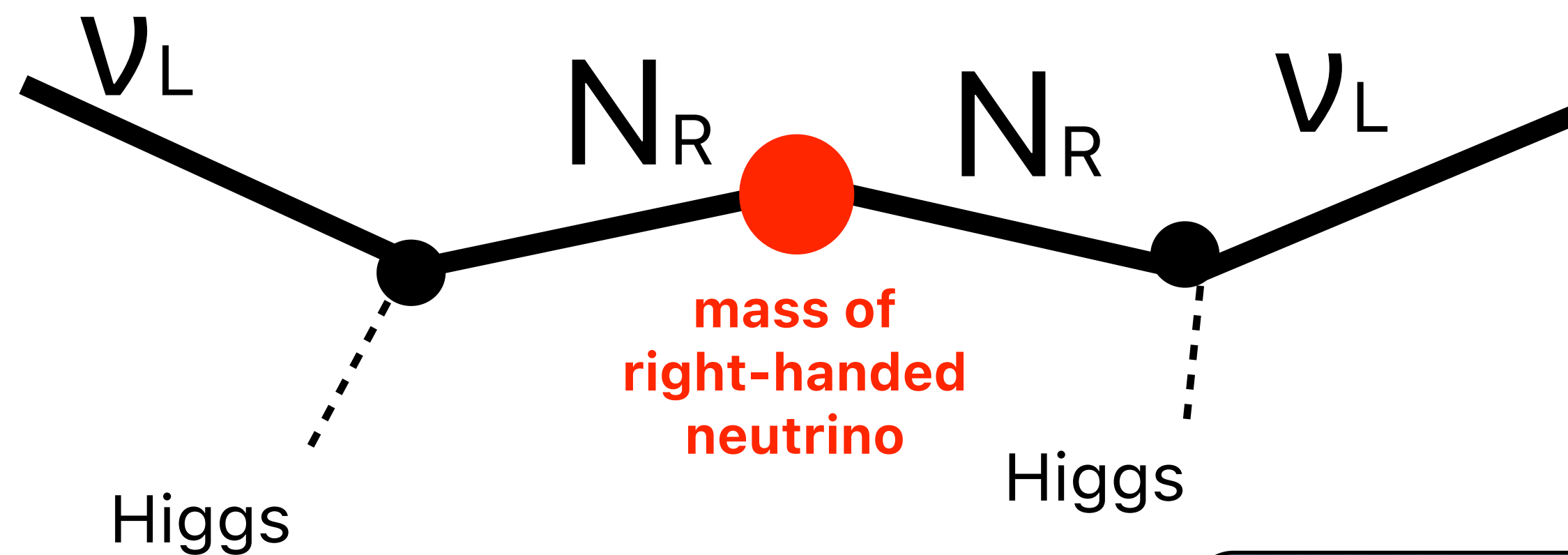
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Neutrino mass
(seen e.g., by oscillation exp.)

=

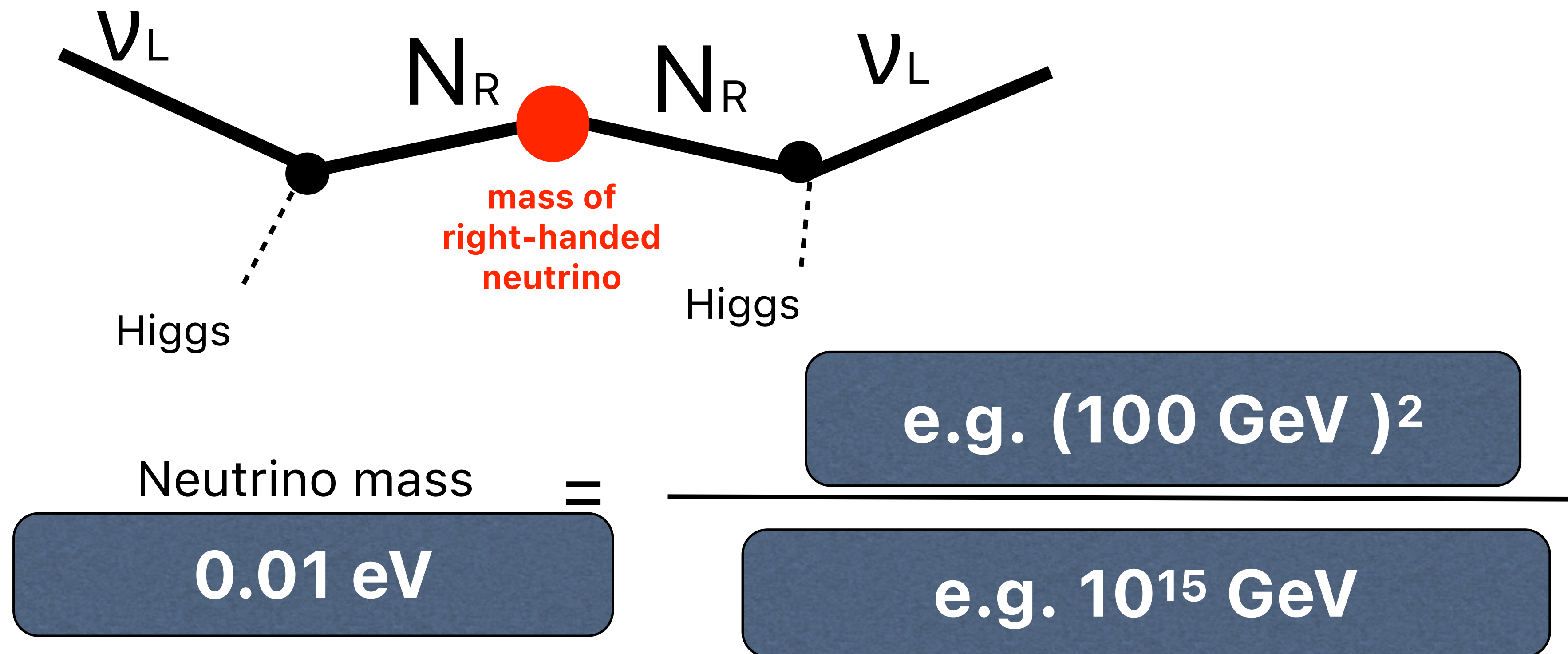
e.g. $(100 \text{ GeV})^2$

e.g. 10^{15} GeV

heavy R.H.v \rightarrow small neutrino masses ("see-saw mechanism")

The right-handed neutrino plays a triple role.

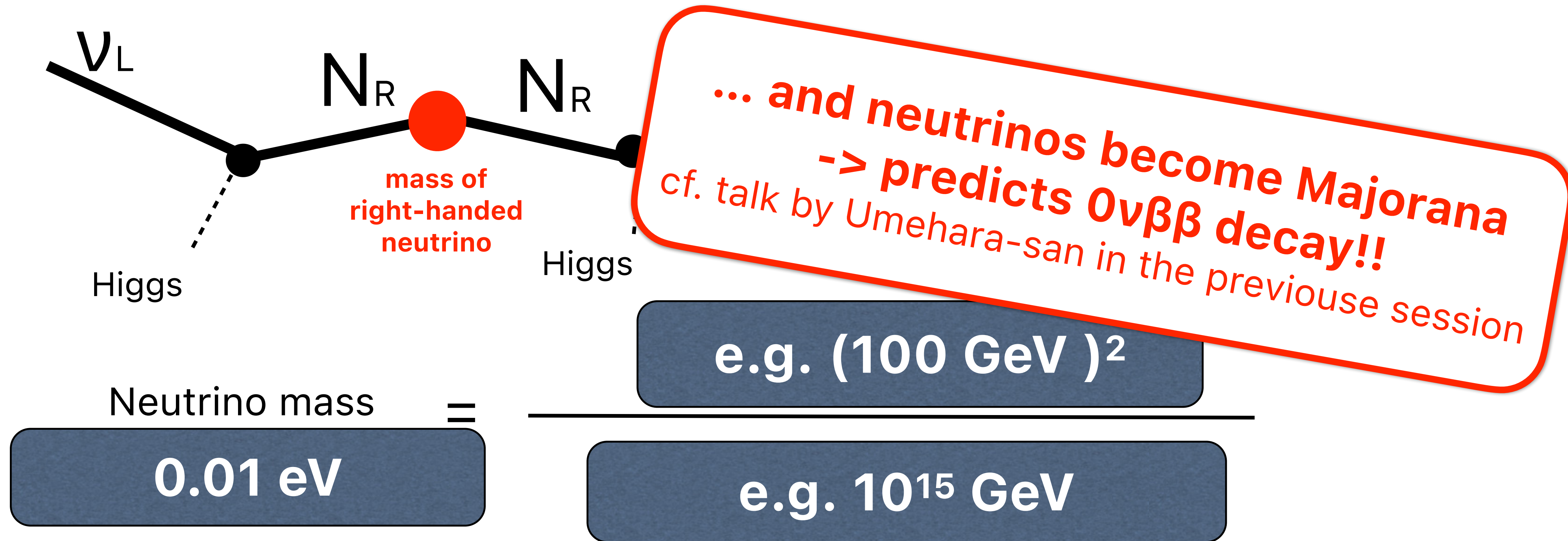
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The right-handed neutrino N plays a triple role.

② explains **tiny** neutrino mass



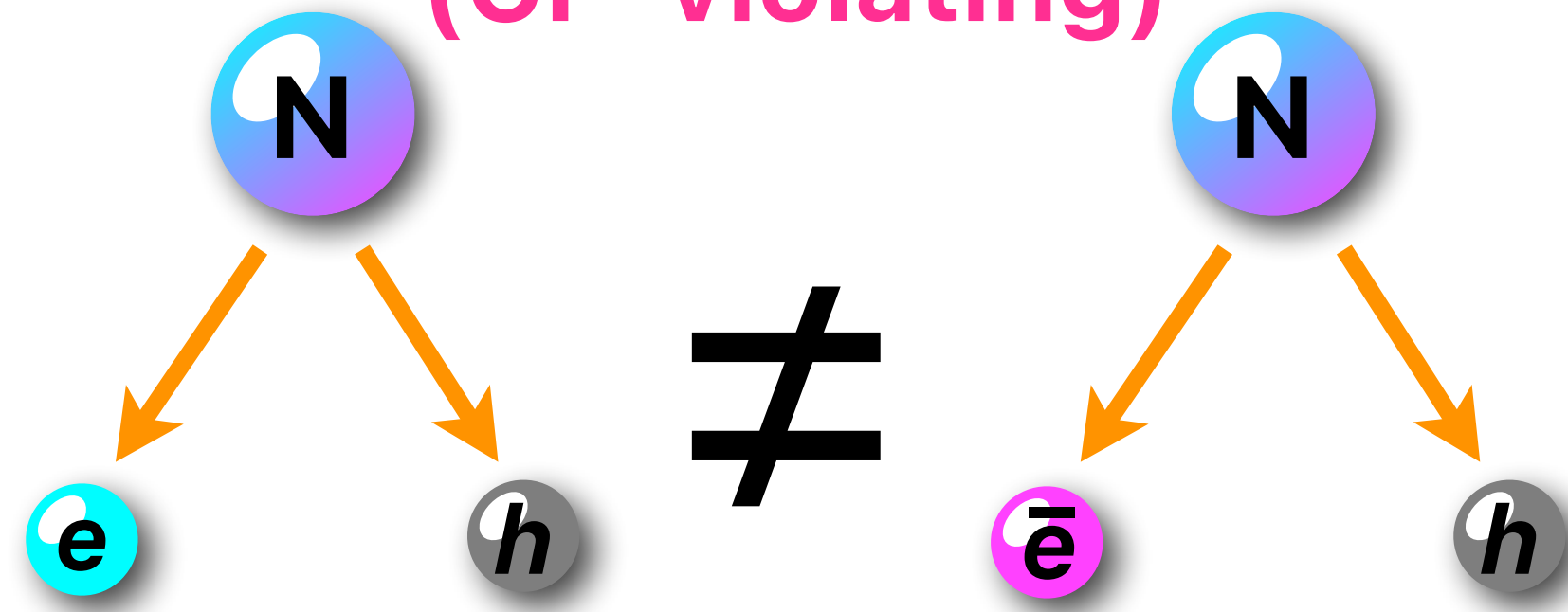
heavy R.H.v \rightarrow small neutrino masses ("see-saw mechanism")

The right-handed neutrino N plays a triple role.

③ explains matter > anti-matter asymmetry of the universe.

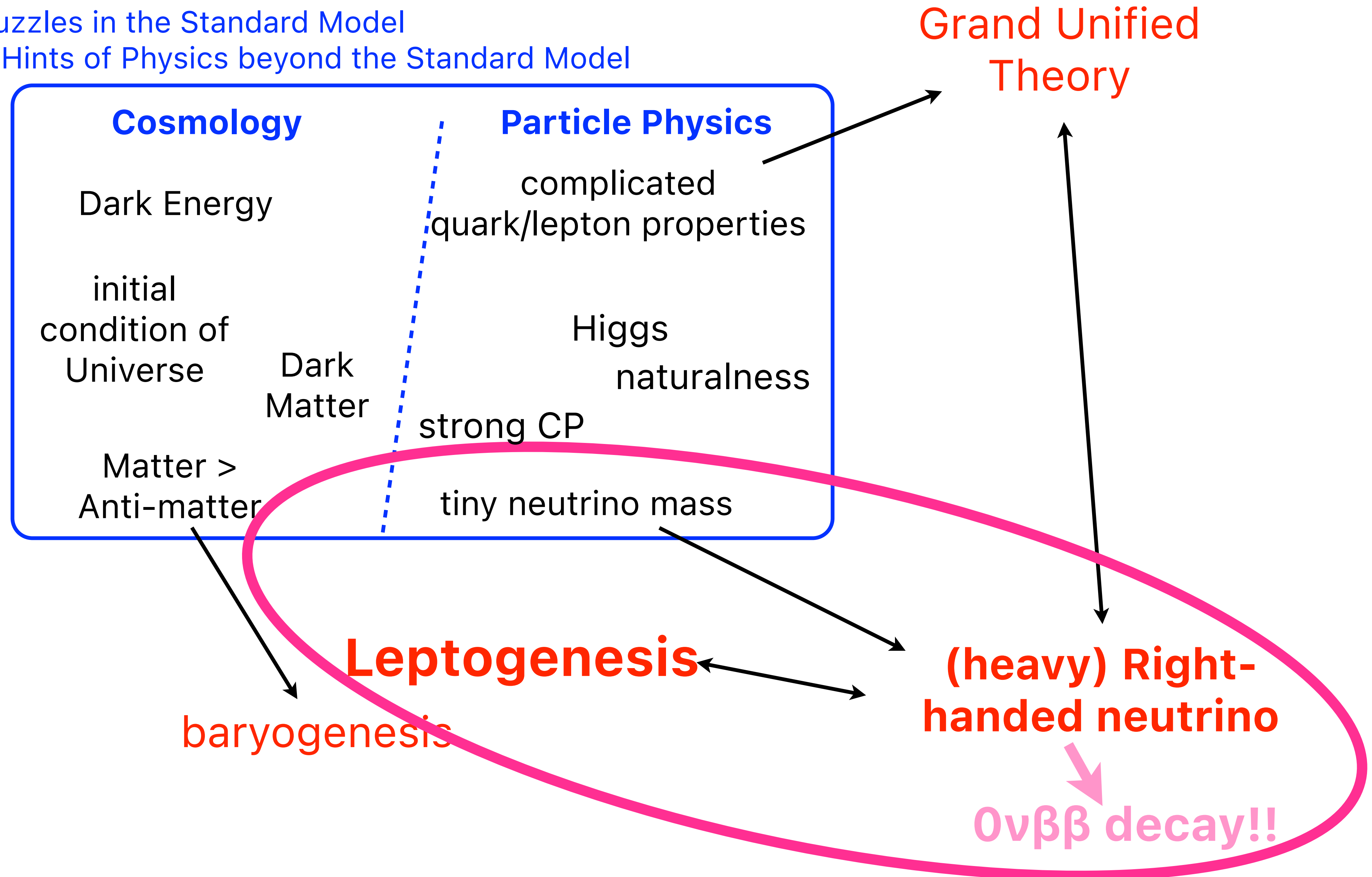
-----> **Leptogenesis !!**

right-handed neutrino decay
(CP-violating)



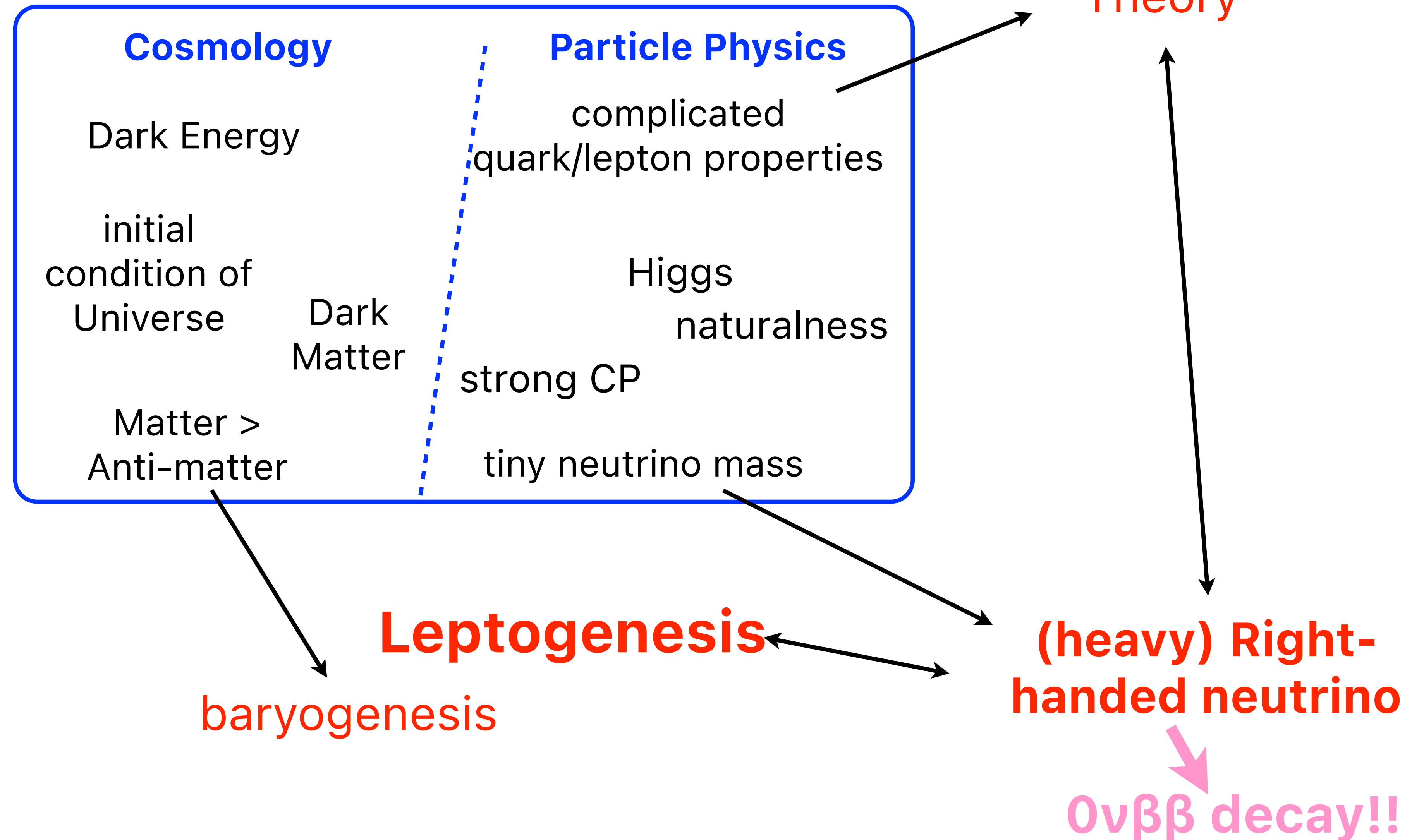
Seesaw and Leptogenesis in a "big picture"

Puzzles in the Standard Model
= Hints of Physics beyond the Standard Model



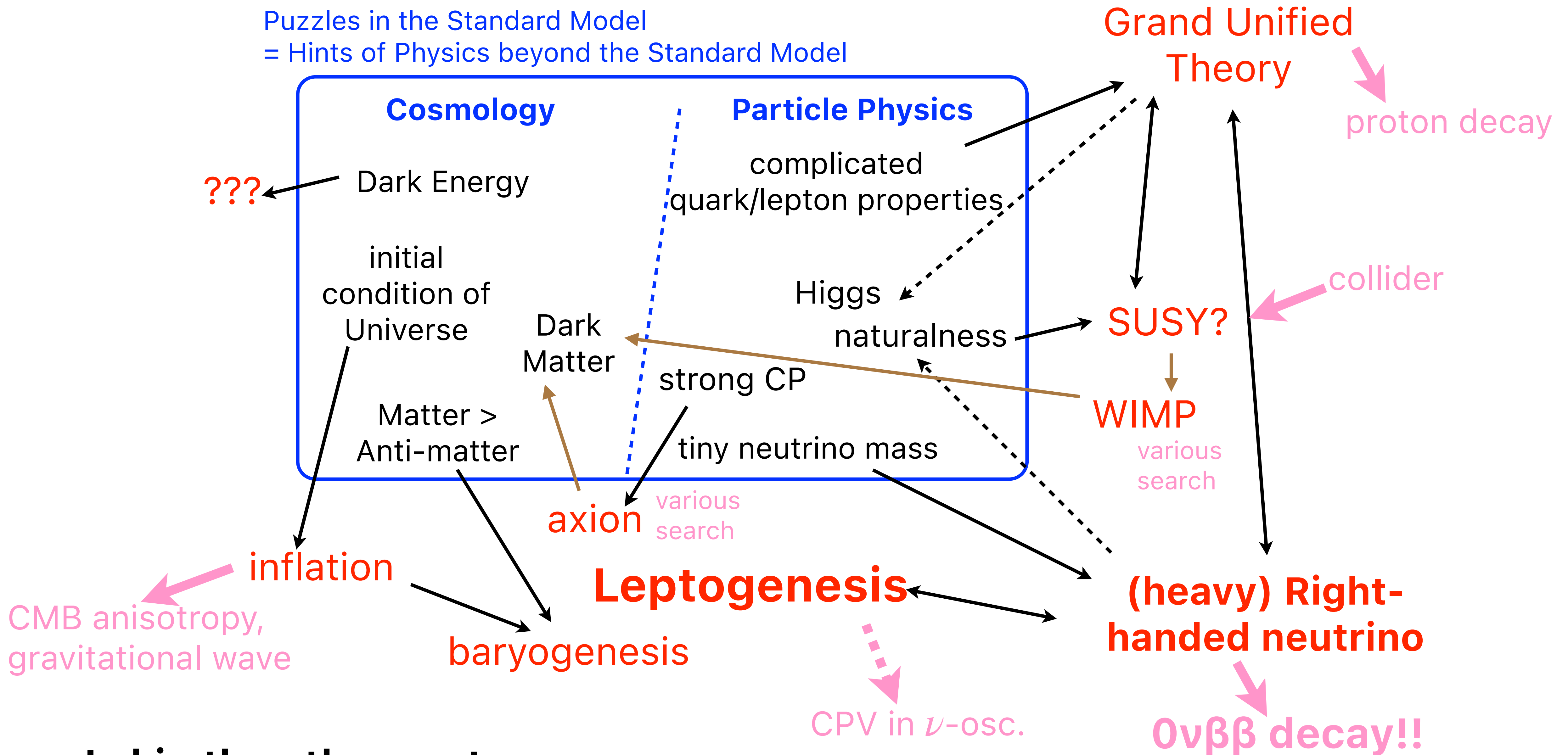
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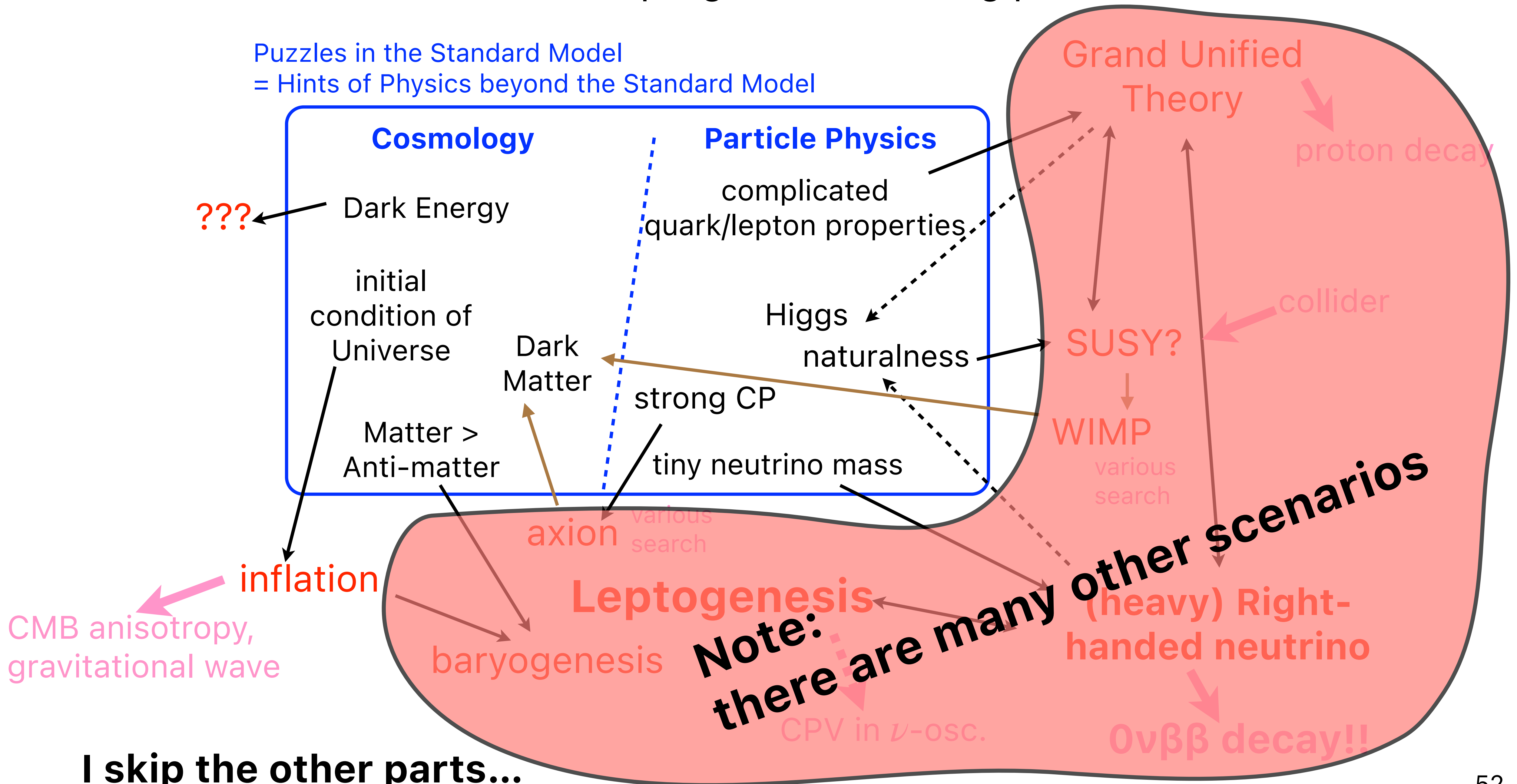
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I skip the other parts...

Seesaw and Leptogenesis in a "big picture"

Puzzles in the Standard Model
= Hints of Physics beyond the Standard Model



I skip the other parts...

Plan

- Leptogenesis

- ▶ Baryon Asymmetry of the Universe

- ▶ Why "Lepto"genesis?

- ▶ Seesaw and Leptogenesis in a "big picture"

- Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

- Summary

Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

K. Asai, KH, N. Nagata, S. Tseng [arXiv:2005.01039] JCAP **11** (2020) 013

cf. K. Asai, KH, N. Nagata, S. Tseng, K. Tsumura, [arXiv:1811.07571] Phys.Rev. **D99** (2019) 055029

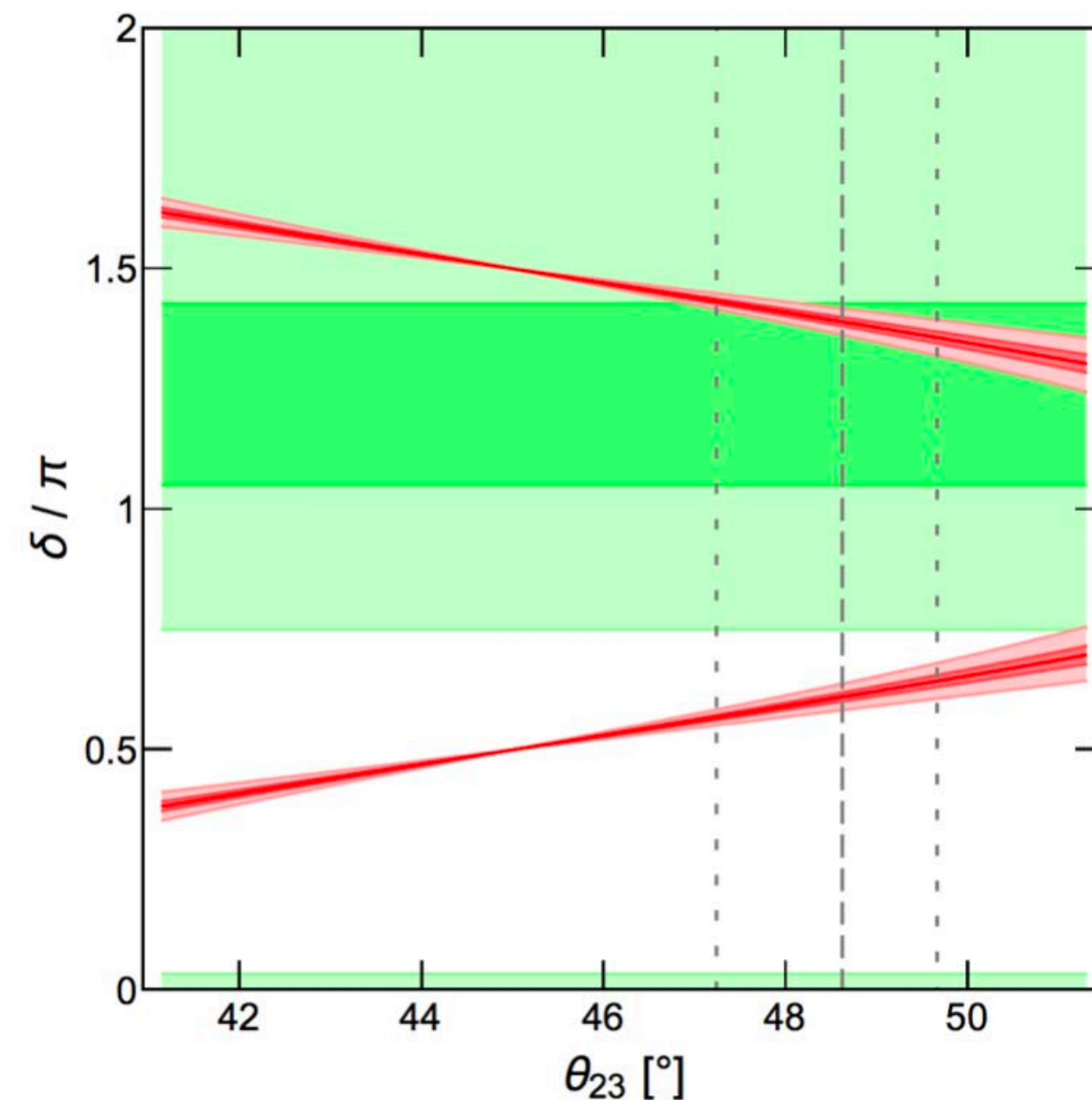
K. Asai, KH, N. Nagata, [arXiv:1705.00419] Eur.Phys.J. **C77** (2017) 763

- gauged $U(1)_{\mu-\tau}$ model: one of the simplest, anomaly-free extension of the Standard Model.

- In minimal models (with just one scalar) neutrino mass matrix is constrained. $m_\nu^{-1} = \begin{pmatrix} * & * & * \\ * & 0 & * \\ * & * & 0 \end{pmatrix}$

-> predictions!

• Dirac CP phase



• $0\nu\beta\beta$ double beta decay.

$$\langle m_{\beta\beta} \rangle \gtrsim \begin{cases} 0.027 \text{ eV} & \text{for } \theta_{23} \lesssim 50.1^\circ \text{ [1}\sigma\text{, NuFit5.0]} \\ 0.017 \text{ eV} & \text{for } \theta_{23} \lesssim 51.7^\circ \text{ [3}\sigma\text{, NuFit5.0]} \end{cases}$$

✱ The other parameters are fixed to be the best fit value.

==> testable in the next-generation $0\nu\beta\beta$ experiments.

Example: Leptogenesis in the minimal gauged $U(1)_{\mu-\tau}$ model.

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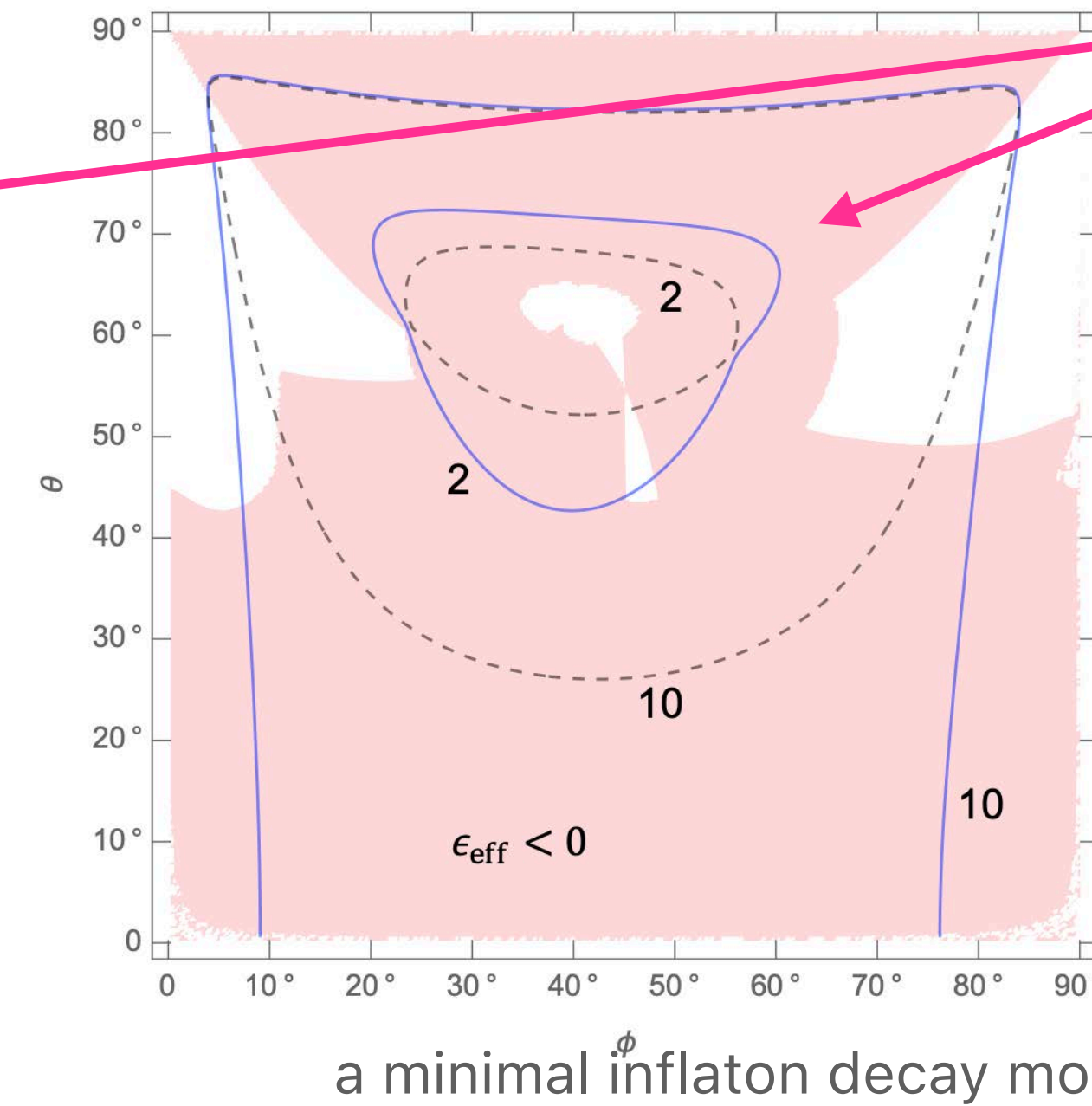
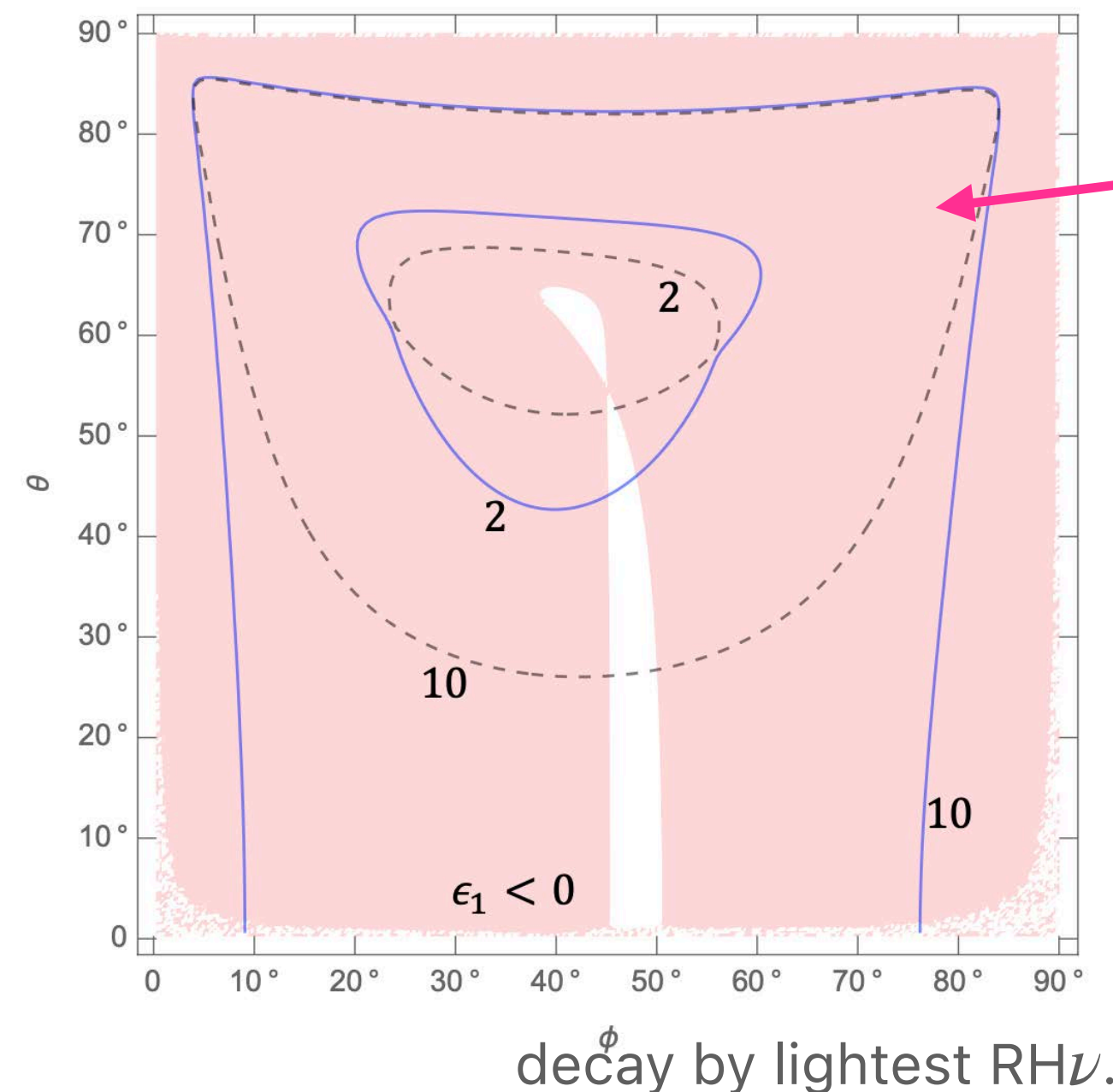
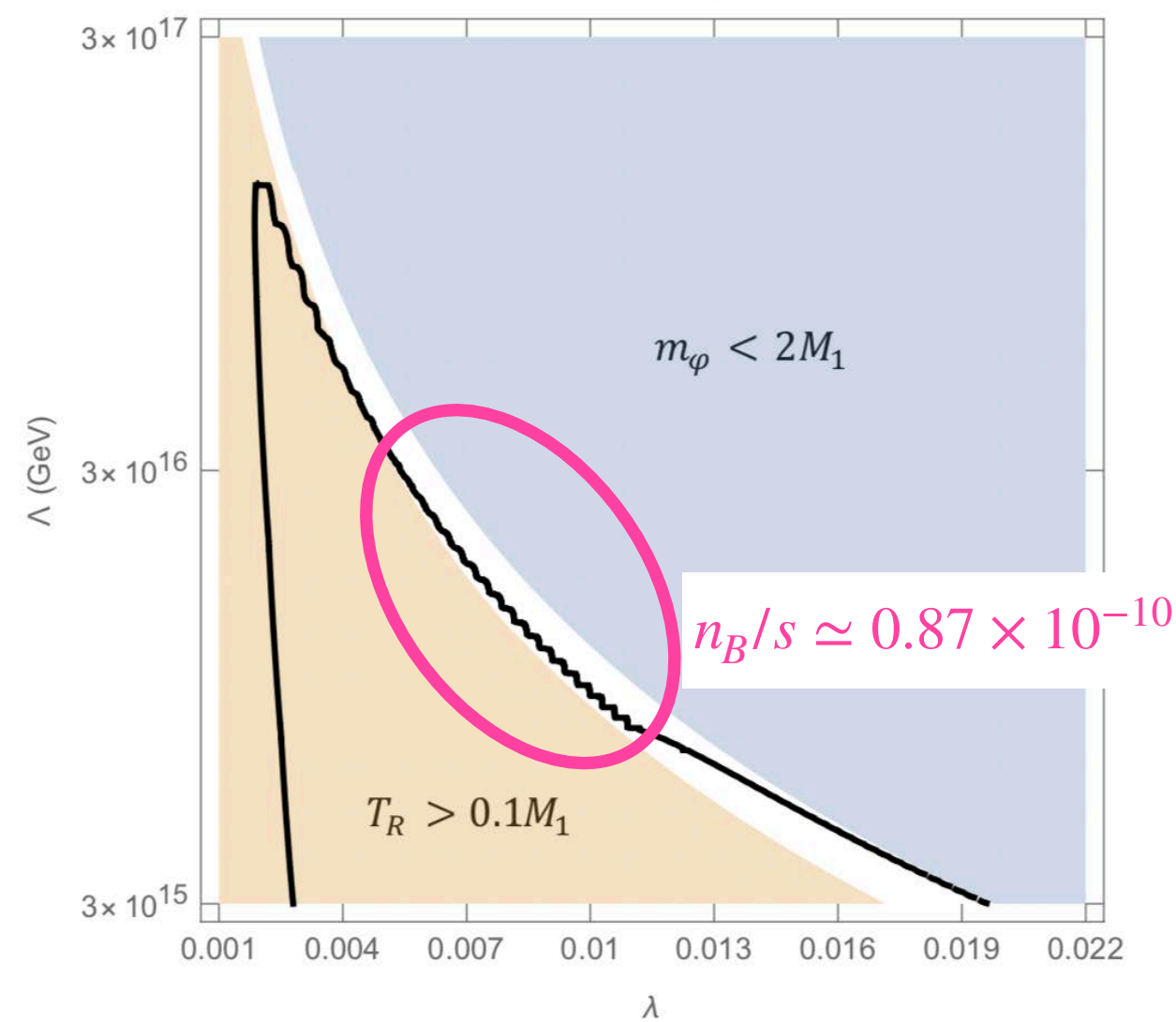
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-> predictions!

- Correlation between the cosmological sign of baryon asymmetry and the Dirac CP phase of neutrino oscillation.**

Leptogenesis works.



$\delta > \pi \rightarrow$ matter remains
 $\delta < \pi \rightarrow$ anti-matter remains

T2K (global fit) suggests $\delta > \pi$.

Summary

- The Baryon Asymmetry of the Universe = one of the evidences of BSM.
- **Leptogenesis** can naturally explain it.
- **Right-handed neutrino (with large Majorana mass) plays a triple role.**
 - (1). **Small neutrino masses.** (seesaw)
 - (2). **Unification** of all quarks and leptons. (16 rep. of SO(10).)
 - (3). **Leptogenesis.** (matter-antimatter asymmetry)
- There are various kinds of Leptogenesis. (Most of them predict **$0\nu\beta\beta$ decay.**)
- An example: the minimal gauged $U(1)_{\mu-\tau}$ model. Predictions for neutrino physics.

Backup

What is necessary

to generate the **Baryon Asymmetry of the Universe?**

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Sakharov's 3 conditions [Sakharov 1967]

• Baryon number (B) violation

• C and CP violation

• Out-of-equilibrium

What is necessary

to generate the **Baryon Asymmetry of the Universe?**

Sakharov's 3 conditions [Sakharov 1967]

- Baryon number (B) violation

If all processes conserve B, then impossible to have $n_B = 0 \rightarrow n_B \neq 0$.

- C and CP violation

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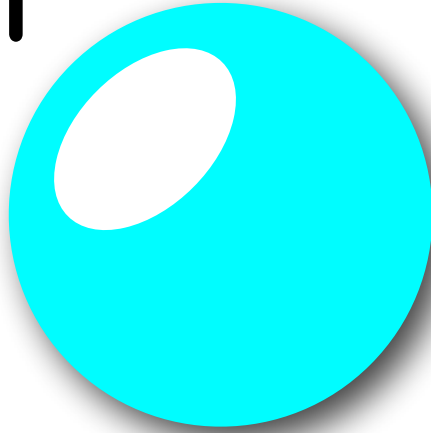
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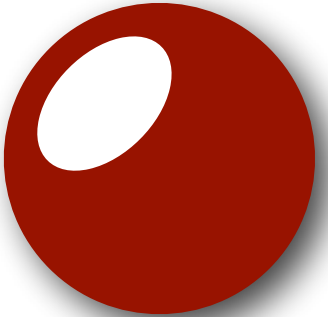
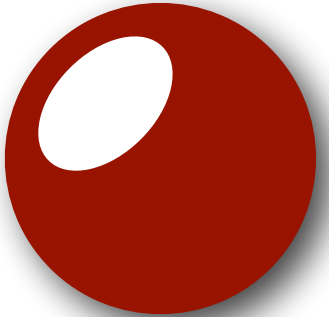
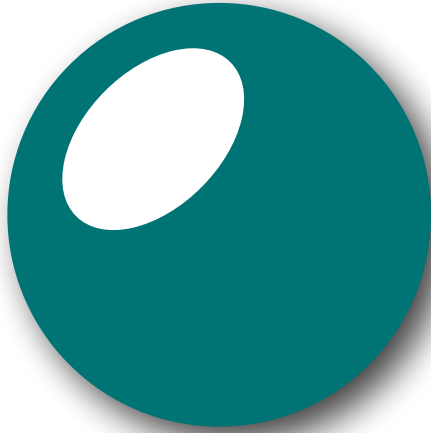
- Out-of-equilibrium

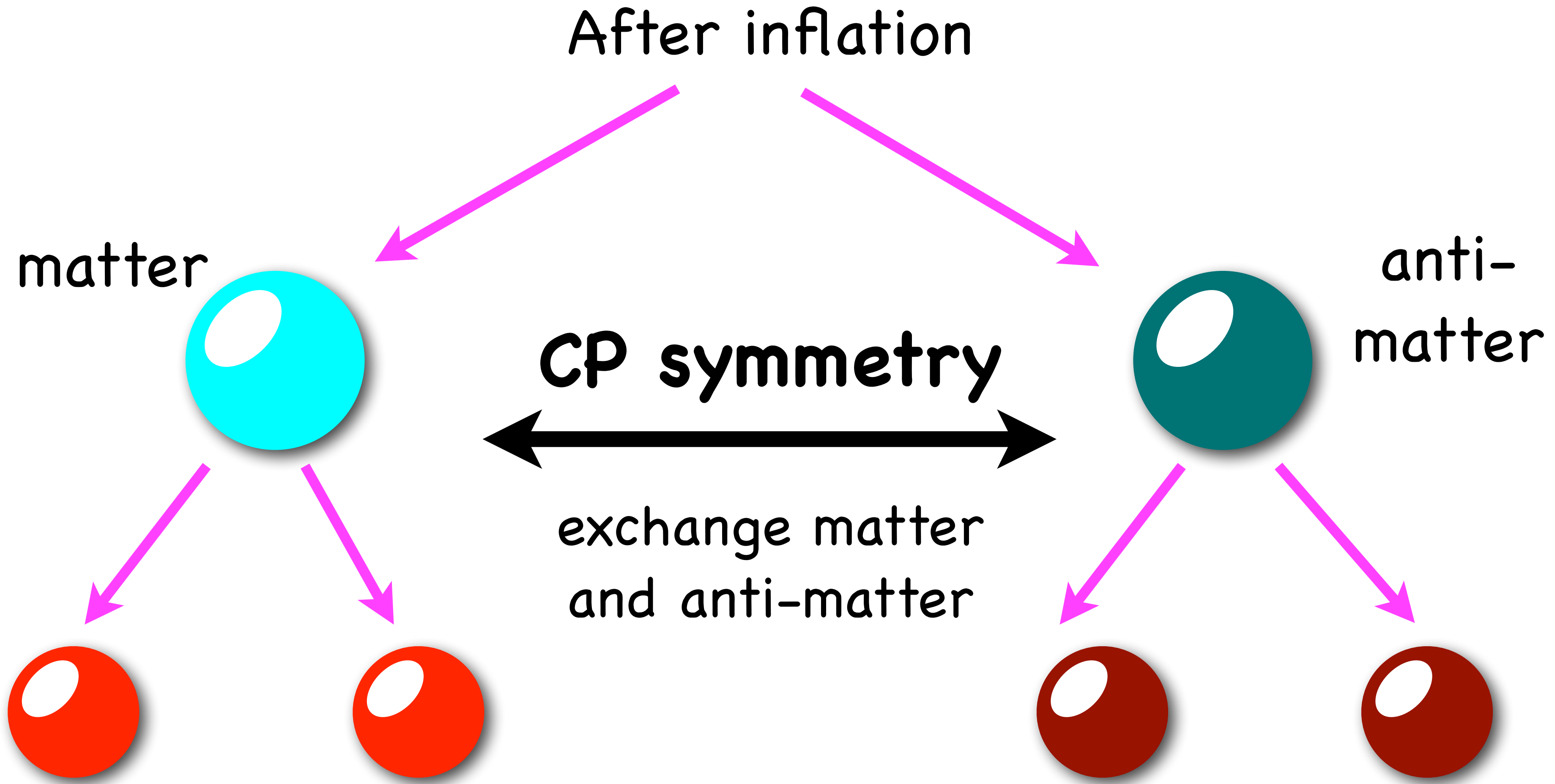
After inflation

matter

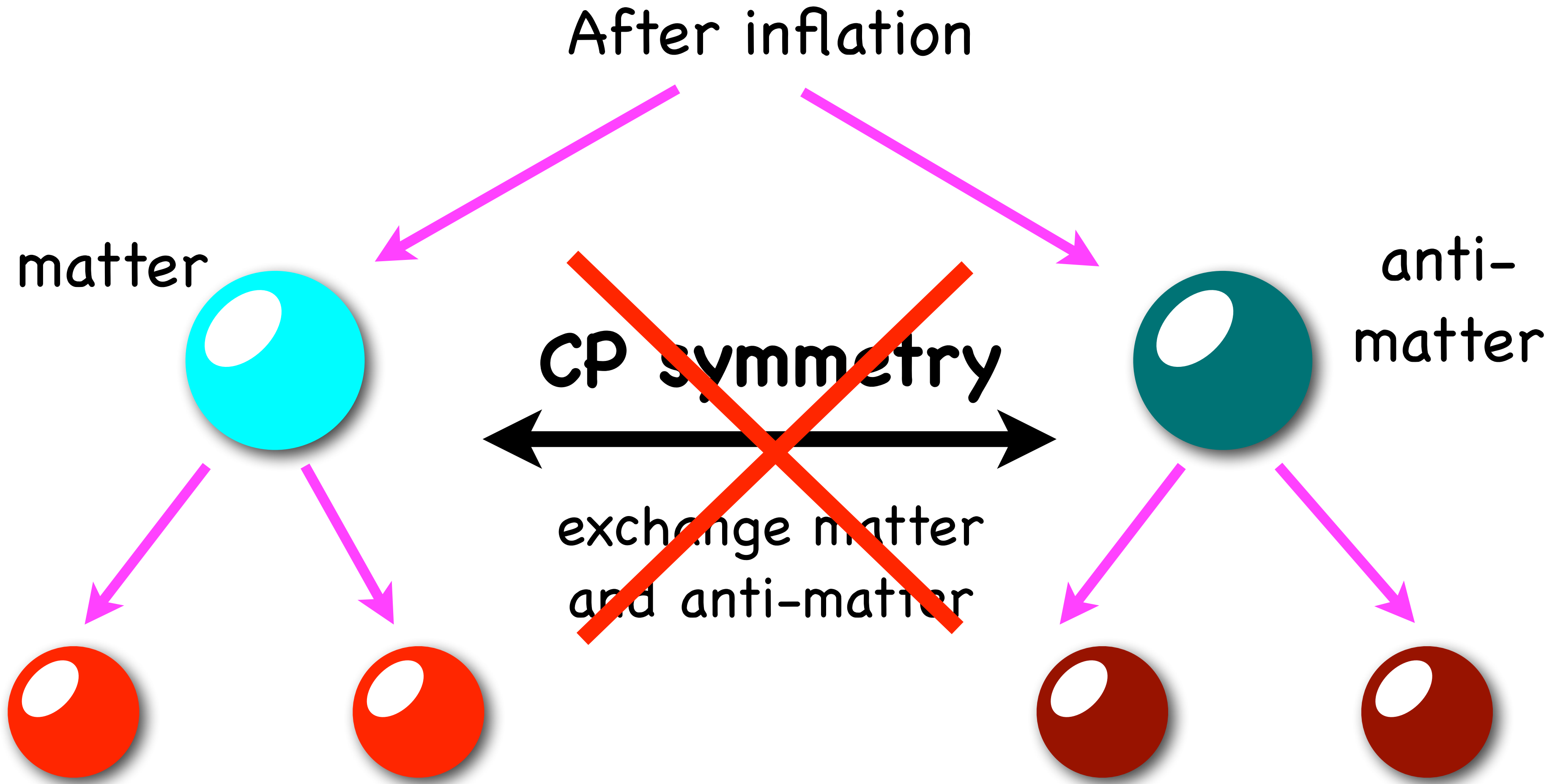


anti-matter





As far as **CP is conserved**, there is no difference between matter and anti-matter.



If CP is violated, there can be a difference between matter and anti-matter.

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Sakharov's 3 conditions [Sakharov 1967]

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- C and CP violation

If all processes conserve CP, then impossible to have $n_B = 0 \rightarrow n_B \neq 0$.

- Out-of-equilibrium

If the processes $n_B < 0 \leftrightarrow n_B = 0 \leftrightarrow n_B > 0$ are in thermal equilibrium, then the system arrives at the equilibrium state ($n_B = 0$).

The system must be out-of-equilibrium, such that $n_B = 0$  $n_B > 0$.

Leptogenesis

Leptogenesis

[Fukugita, Yanagida, 1986]

Model: Standard Model + R.H. ν

Cosmology: Standard thermal cosmology

Extremely simple!

No complicated model/cosmology required.

Leptogenesis

[Fukugita, Yanagida, 1986]

scenario

Leptogenesis

[Fukugita, Yanagida, 1986]

scenario

temperature \searrow RH ν 's mass \swarrow
step 1: $T > M_R$: N_1 are in thermal bath.

Leptogenesis

[Fukugita, Yanagida, 1986]

scenario

step 1: $T > M_R$: N_1 are in thermal bath.

temperature \swarrow M_R \swarrow RH ν 's mass

step 2: $T \sim M_R$: N_1 decay. (CP violation + out-of-eq.)
--> generate Lepton asymmetry, $\Delta L \neq 0$.

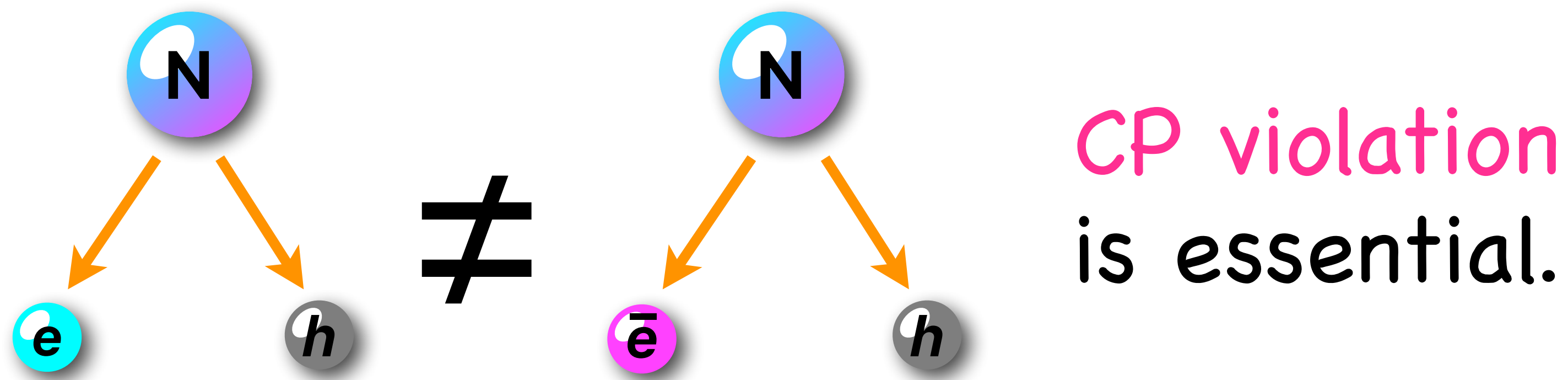
Leptogenesis

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scenario

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Leptogenesis

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scenario

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temperature \swarrow M_R \swarrow RH ν 's mass

step 2: $T \sim M_R$: N_1 decay. (CP violation + out-of-eq.)
--> generate Lepton asymmetry, $\Delta L \neq 0$.

step 3: Lepton asymmetry $\Delta L \neq 0$ \dashrightarrow Baryon asymmetry $\Delta B \neq 0$

(automatic in SM ! thanks to "sphaleron")

[Kuzmin, Rubakov, Shaposhnikov, 1985]

Leptogenesis

[Fukugita, Yanagida, 1986]

Result: (I skip all the details of the calculation...
For derivations and references, see, e.g., [KH: hep-ph/0212305](#))

Leptogenesis

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$$\frac{n_B}{s} \simeq 0.3 \times 10^{-10} \left(\frac{\kappa}{0.1} \right) \left(\frac{M_1}{10^9 \text{ GeV}} \right) \cdot \left(\frac{m_{\nu 3}}{0.05 \text{ eV}} \right) \delta_{\text{eff}}$$

Leptogenesis

[Fukugita, Yanagida, 1986]

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final baryon
asymmetry


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final baryon
asymmetry



$$\frac{n_B}{s}$$

$$\simeq 0.3 \times 10^{-10}$$

$$\left(\frac{\kappa}{0.1} \right)$$

RH ν 's mass



$$\left(\frac{M_1}{10^9 \text{ GeV}} \right)$$

$$\cdot \left(\frac{m_{\nu 3}}{0.05 \text{ eV}} \right)$$

$$\delta_{\text{eff}}$$

Leptogenesis

[Fukugita, Yanagida, 1986]

Result:

(I skip all the details of the calculation...

For derivations and references, see, e.g., [KH: hep-ph/0212305](#))

final baryon asymmetry \rightarrow $\frac{n_B}{s} \simeq 0.3 \times 10^{-10} \left(\frac{\kappa}{0.1} \right) \left(\frac{M_1}{10^9 \text{ GeV}} \right) \cdot \left(\frac{m_{\nu 3}}{0.05 \text{ eV}} \right) \delta_{\text{eff}}$

RH ν 's mass \rightarrow M_1

heaviest neutrino mass (\sim atmospheric) \rightarrow $m_{\nu 3}$

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wash-out factor (< 1)
(calculable: by Boltzmann eq.)

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$$\delta_{\text{eff}} \equiv \frac{\text{Im} \left[(\hat{h}_{13})^2 + \frac{m_{\nu 2}}{m_{\nu 3}} (\hat{h}_{12})^2 + \frac{m_{\nu 1}}{m_{\nu 3}} (\hat{h}_{11})^2 \right]}{|\hat{h}_{13}|^2 + |\hat{h}_{12}|^2 + |\hat{h}_{11}|^2} < 1$$

Yukawa

Leptogenesis

[Fukugita, Yanagida, 1986]

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Yukawa

Predictable / Calculable in terms of [SM + R.H. ν] Lagrangian !

Leptogenesis

[Fukugita, Yanagida, 1986]

Result:

(I skip all the details of the calculation...

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final baryon asymmetry

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heaviest neutrino mass (\sim atmospheric)

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heaviest neutrino mass (\sim atmospheric)

wash-out factor (< 1)
(calculable: by Boltzmann eq.)

effective CP violating phase

$\frac{n_B}{s}$ (observed) = $(0.88 \pm 0.02) \times 10^{-10}$ [PDG, 2012]

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final baryon asymmetry $\frac{n_B}{s}$

RH ν 's mass M_1

heaviest neutrino mass (\sim atmospheric) $m_{\nu 3}$

wash-out factor (< 1) (calculable: by Boltzmann eq.) κ

effective CP violating phase δ_{eff}

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It works !! (for $M_R > 10^9 - 10^{10}$ GeV). 74