

# FLUID + JET

Yasuki Tachibana

QCD相転移やQGP生成のモデル化による  
重イオン衝突の時空発展の理解に向けた理論・実験共同研究会

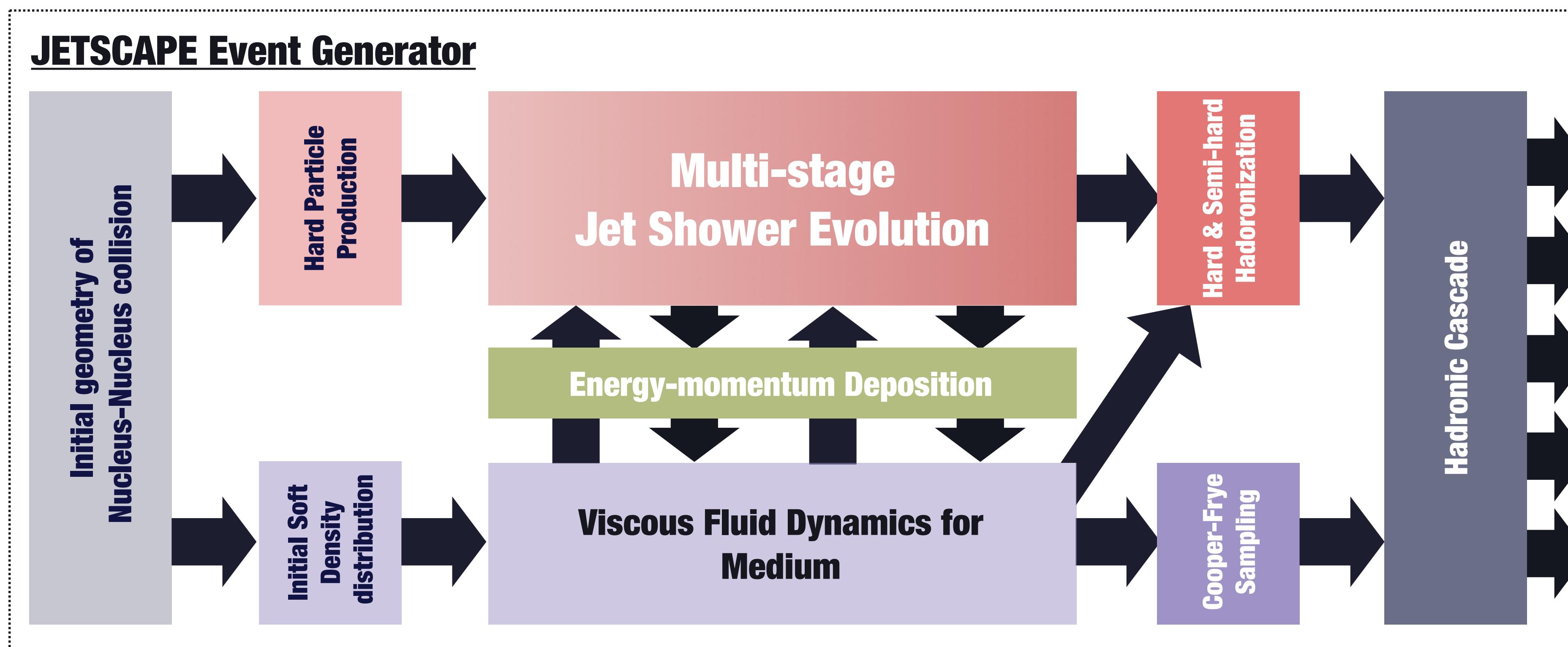
September 24th, 2021

# Jet Evolution in JETSCAPE

# JETSCAPE framework

- MC event generator package for heavy ion collisions

- General, modular and extensible
- Communication between modules



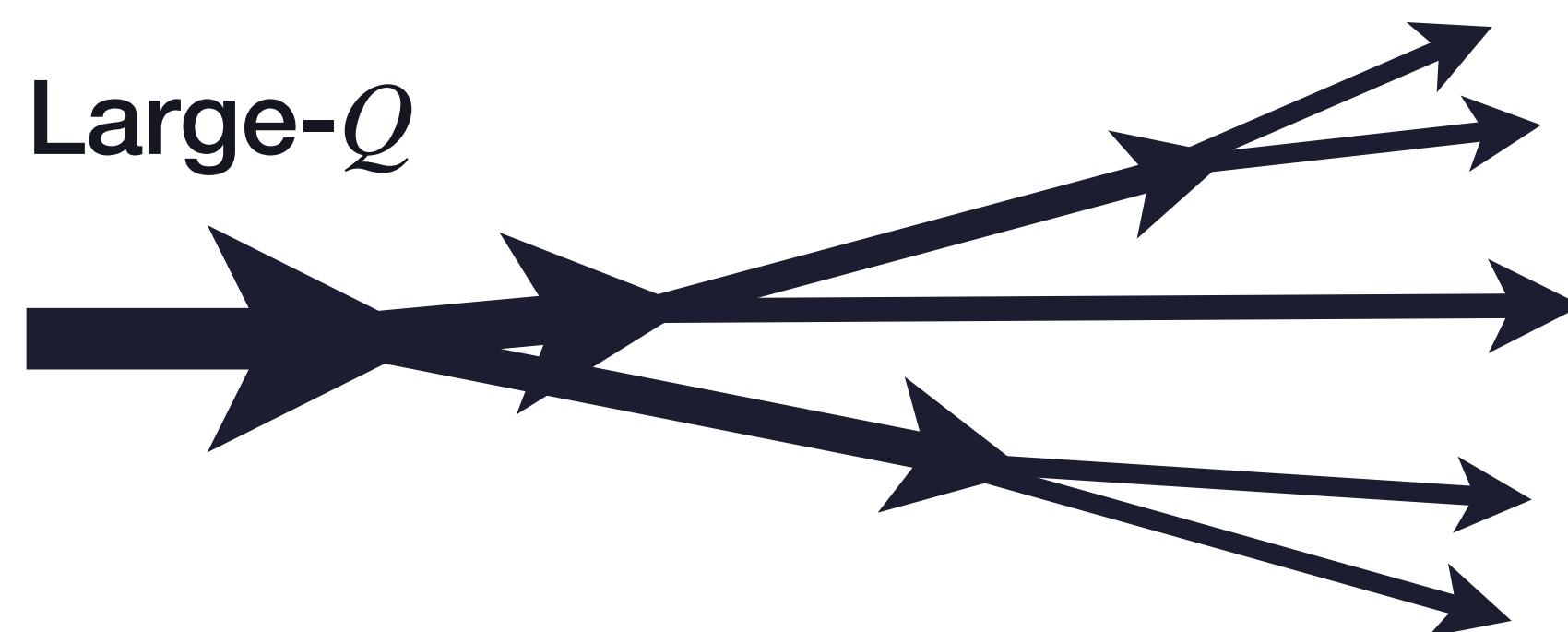
# Multi-scale jet evolution

Majumder, Putschke (16), JETSCAPE (17)

In-vacuum

- In-vacuum: Virtuality ordered splitting

Small- $Q$



$Q^2$ : virtuality (off-shellness)

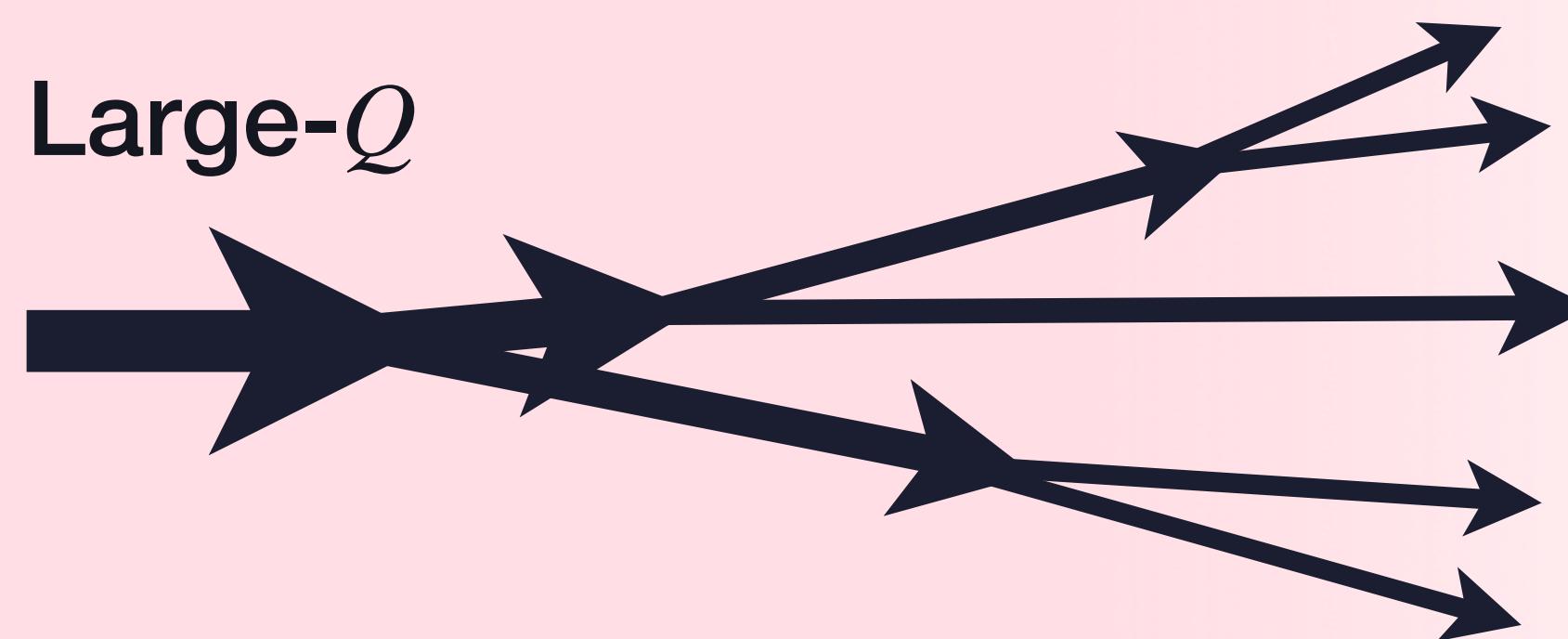
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In-medium

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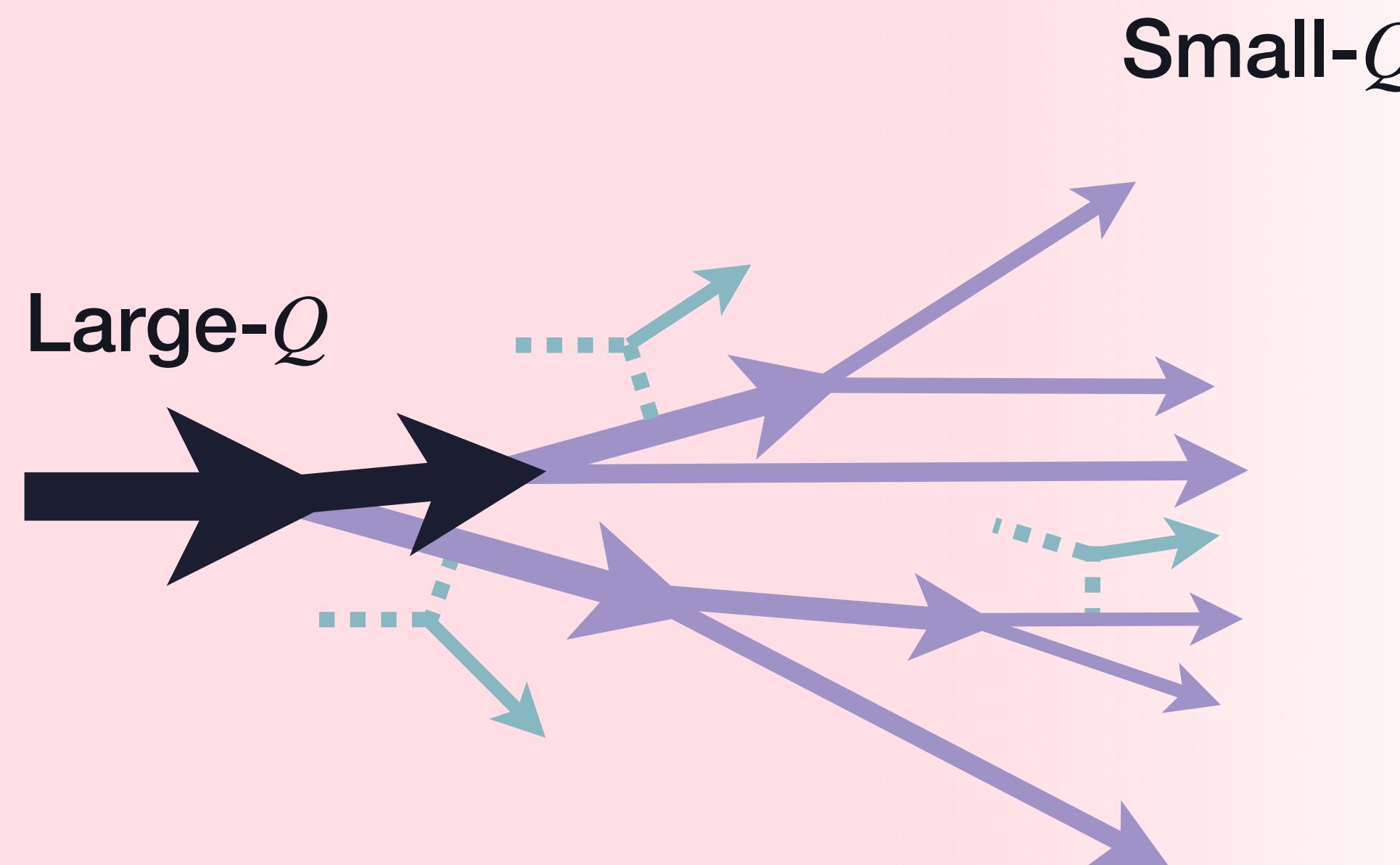


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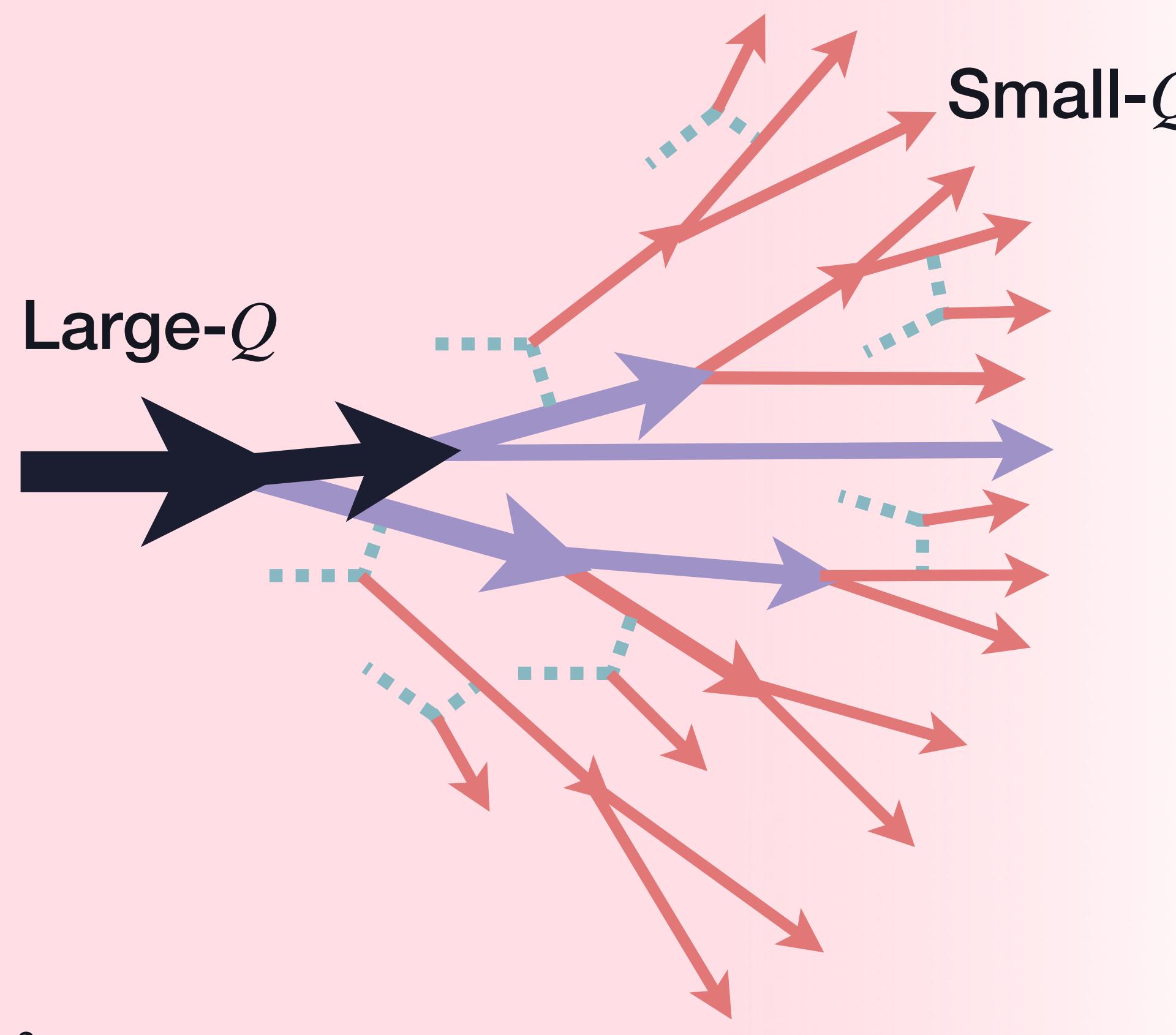
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- Large- $Q$ : Medium effect on the top of in-vacuum splitting  
**(Medium modified splitting)**

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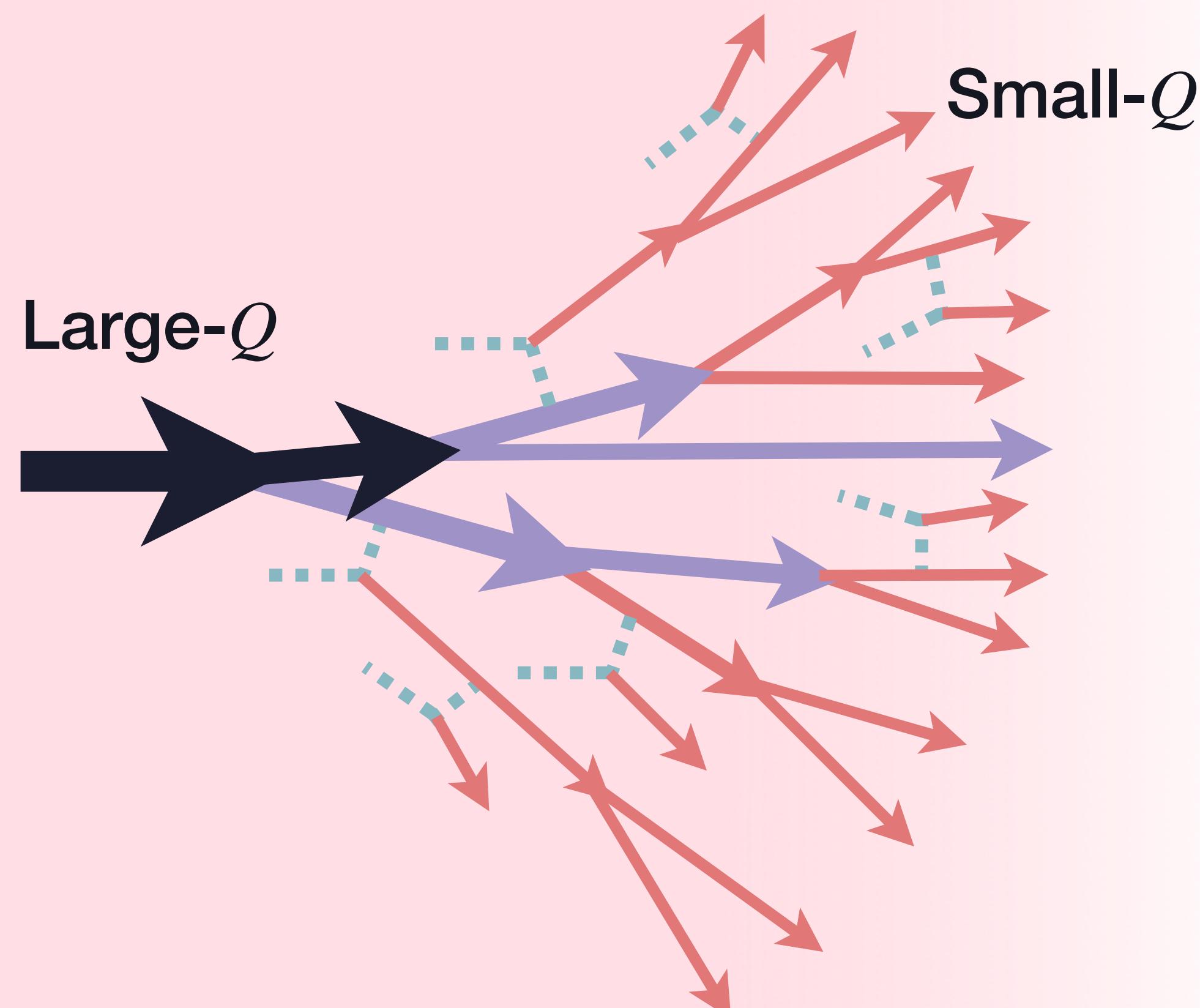
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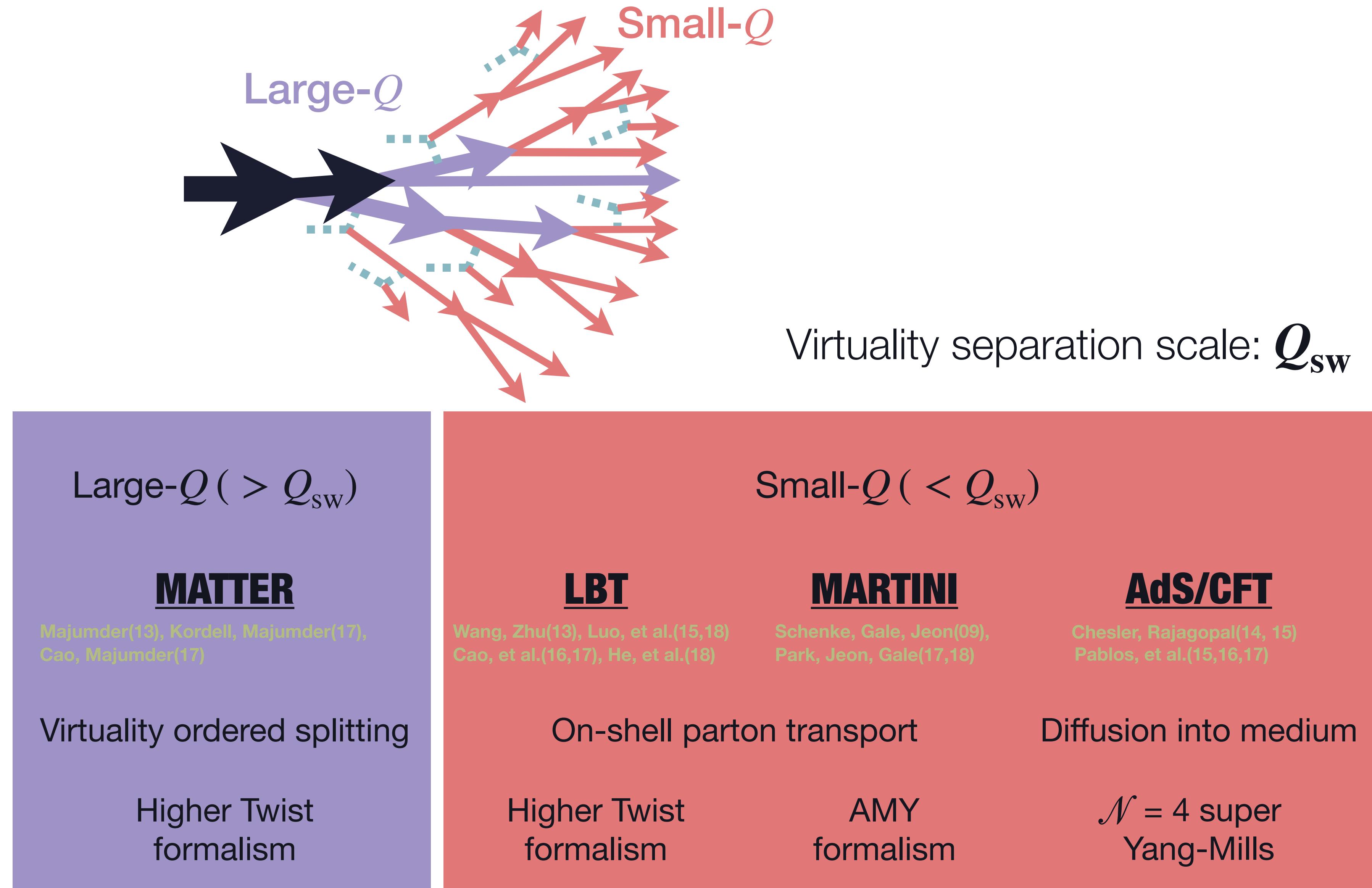


- In-vacuum: Virtuality ordered splitting
- Large- $Q$ : Medium effect on the top of in-vacuum splitting  
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Cannot be described by a single model  
→ Combination of multiple models

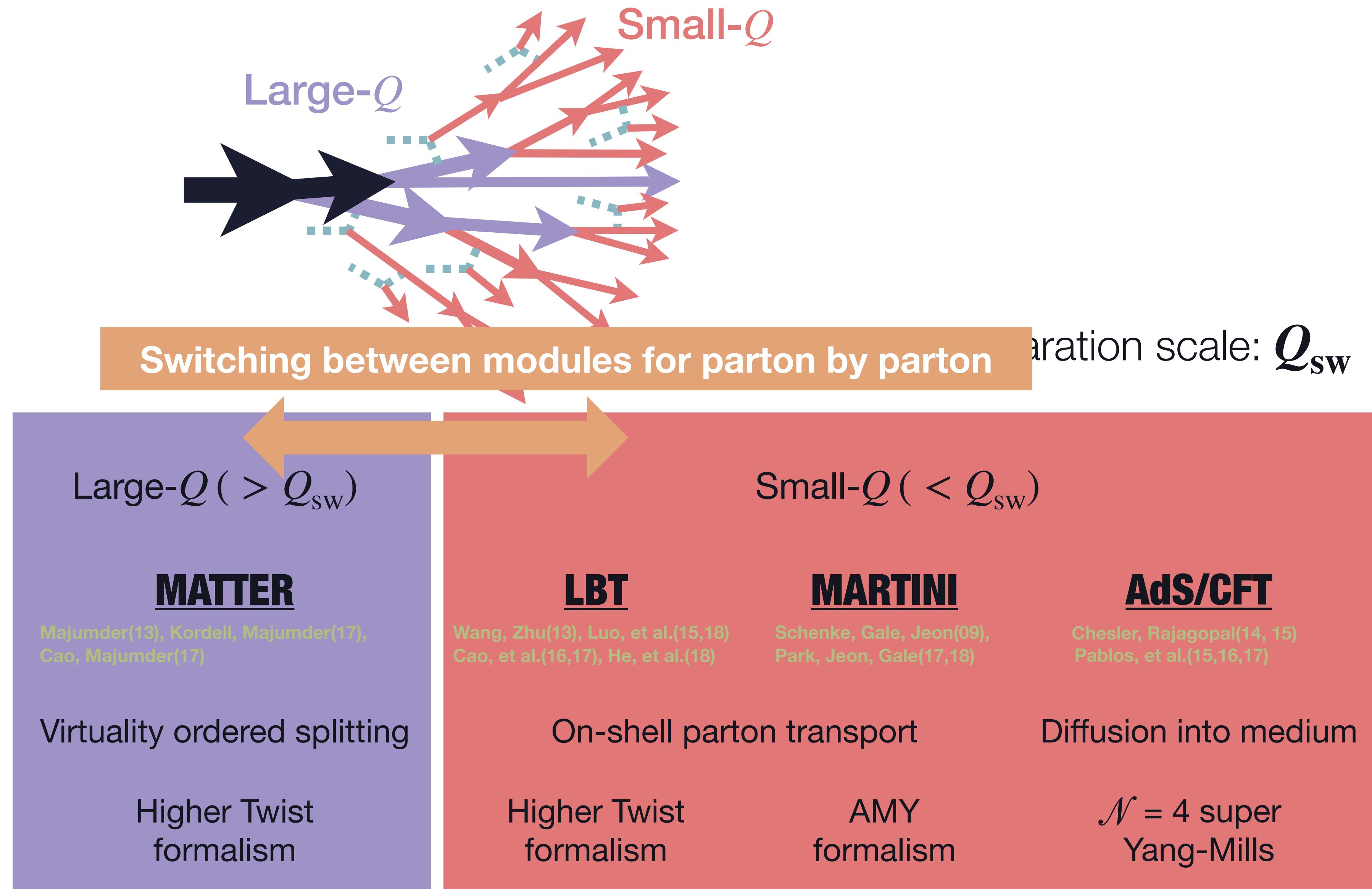
# Multi-stage description for jet evolution

JETSCAPE (17)



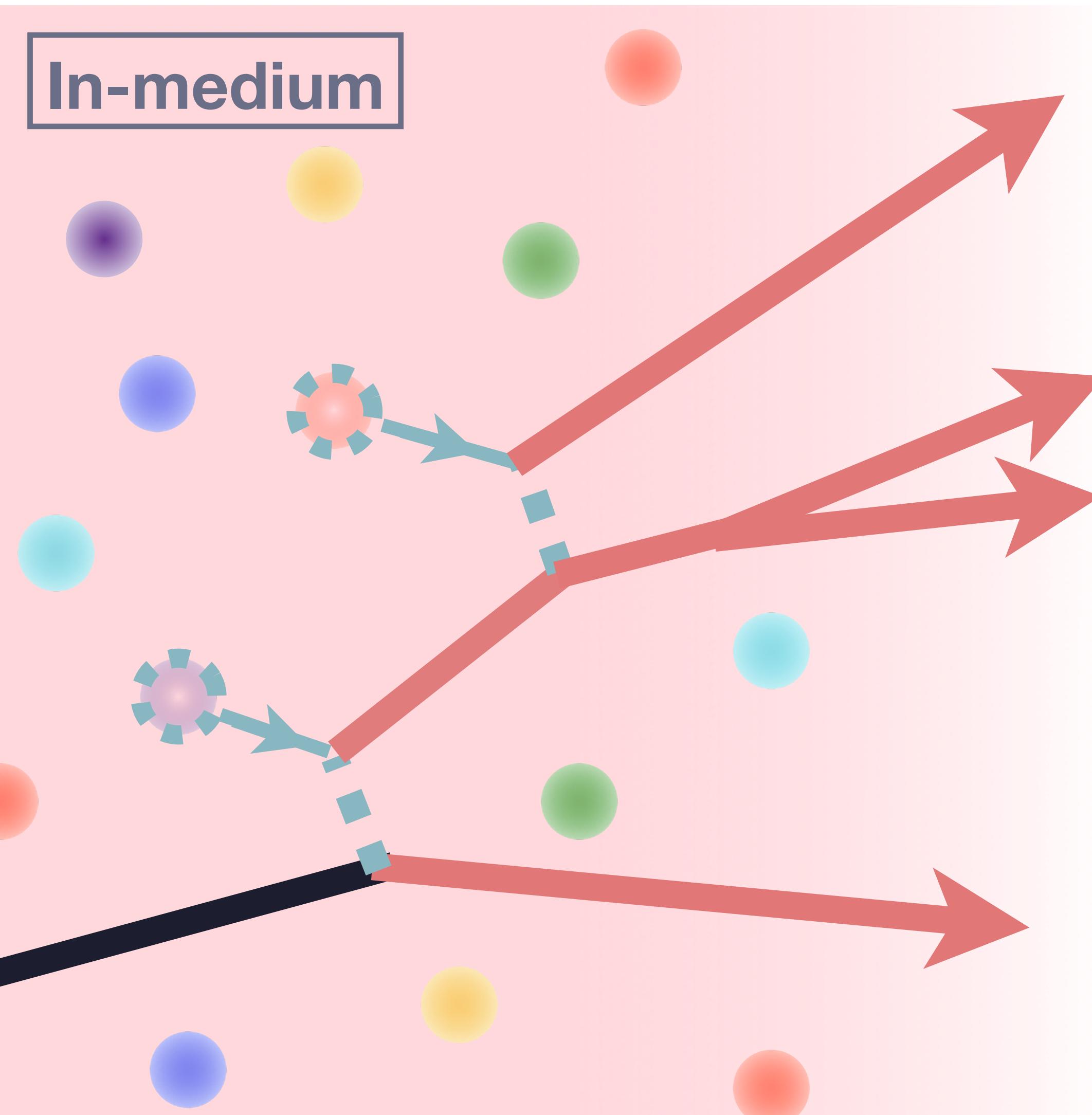
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# Medium response by weakly-coupled recoils

Zapp et al. ('13), Wang, Zhu (13), Luo, et al. (15,18), Park, Jeon, Gale (18), Cao, Majumder (18)



## Recoils

- Medium partons kicked out by jet partons
- Evolve as small- $Q^2$  partons in jet shower
- Infinite thermalization time ( $E > E_{\text{med}}$ )

## Hole: Picked up energy and momentum

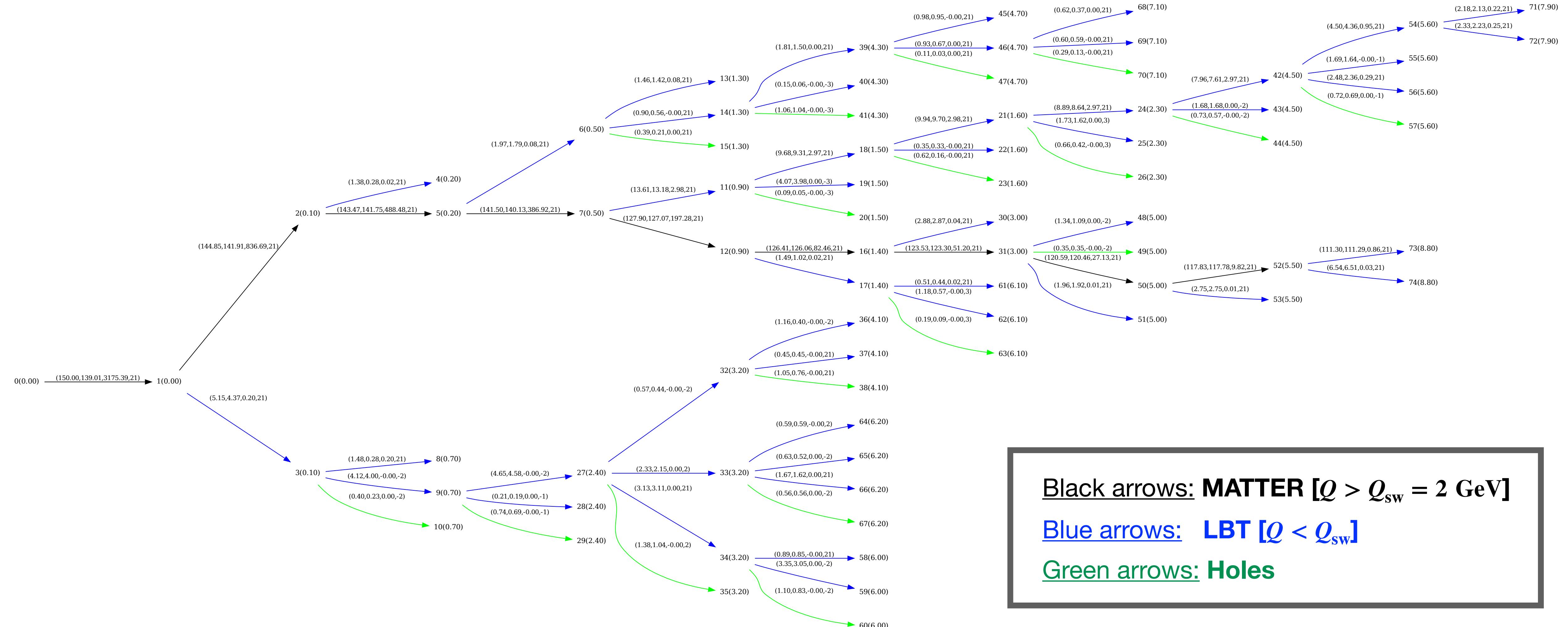
- Sampled from thermal medium
- Subtracted from final signal

$$\left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{signal}} = \left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{jet shower}} - \left. \frac{dp^\mu}{d\eta d\phi} \right|_{\text{picked-up}}$$

# Multi-stage description for jet evolution

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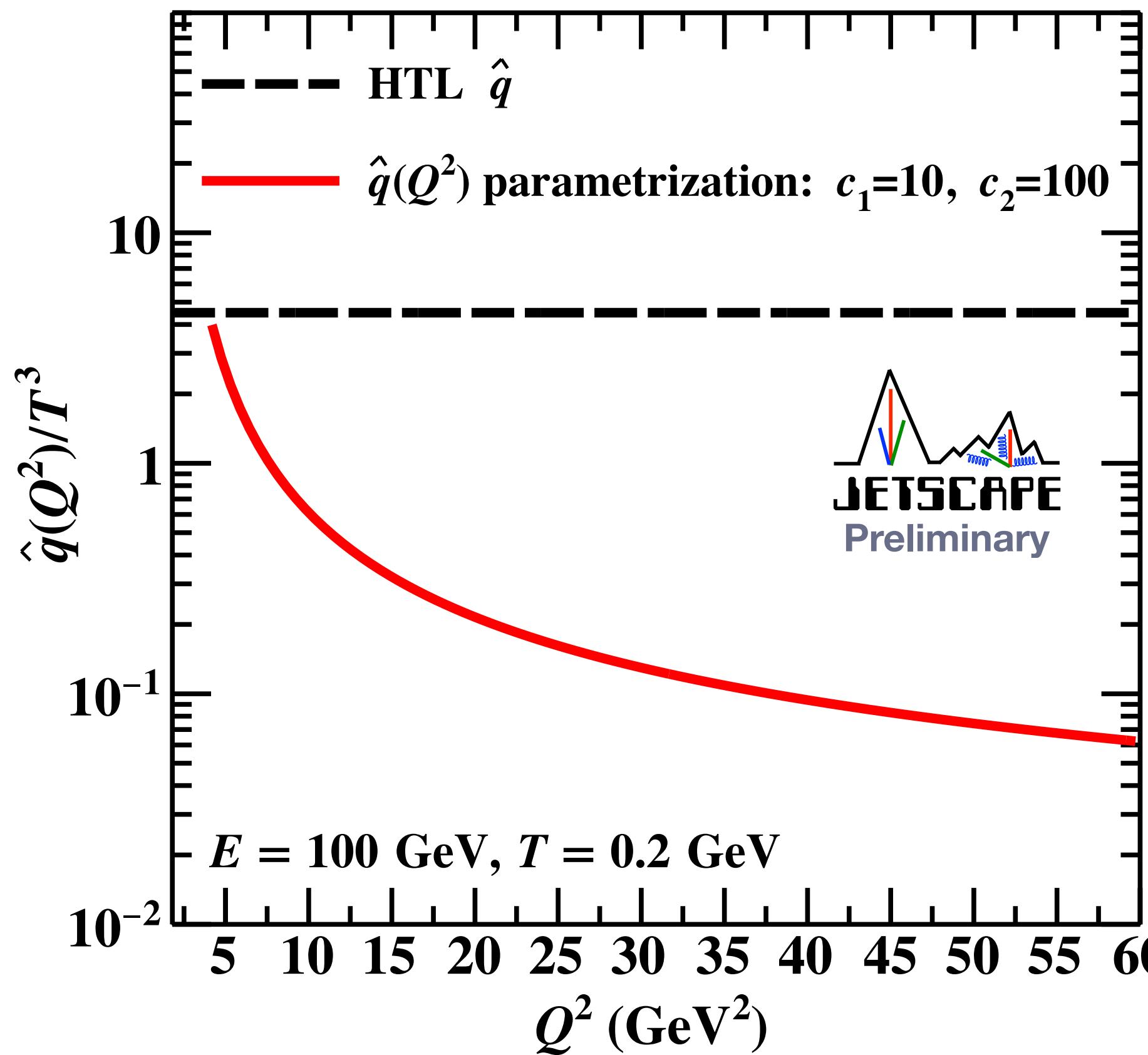
- Graph of parton shower generated by JETSCAPE



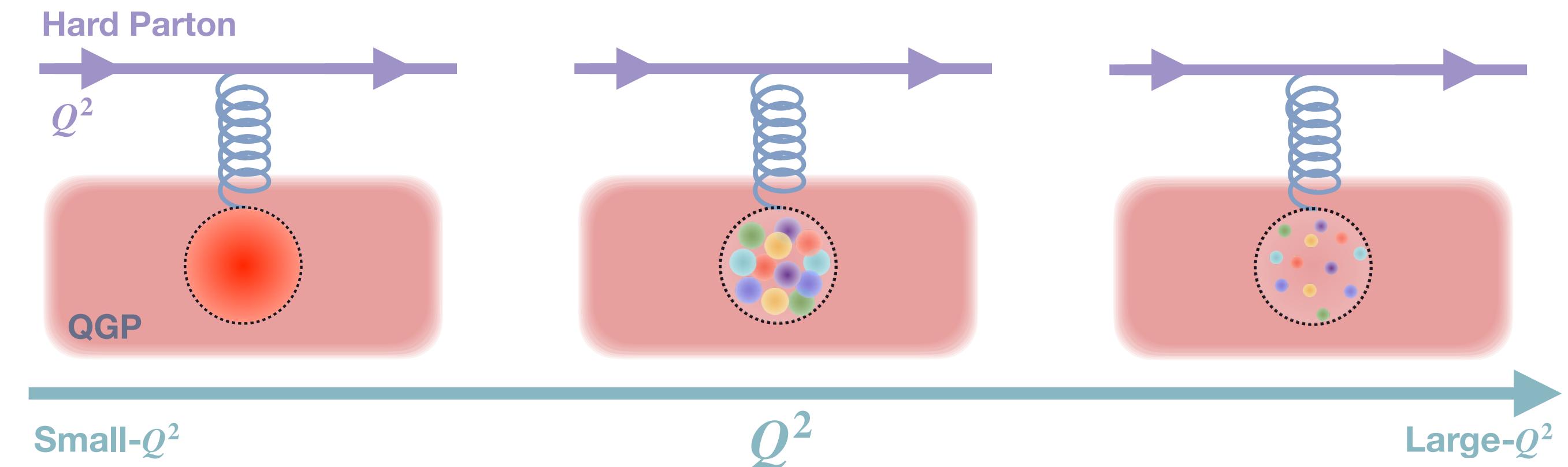
# Recent Update

JERSCAPE (in preparation)

- **Virtuality dependence  
in jet quenching parameter  $\hat{q}$**



- Based on scale evolution of QGP constituent distribution  
**Kumar, Majumder, Shen (20)**

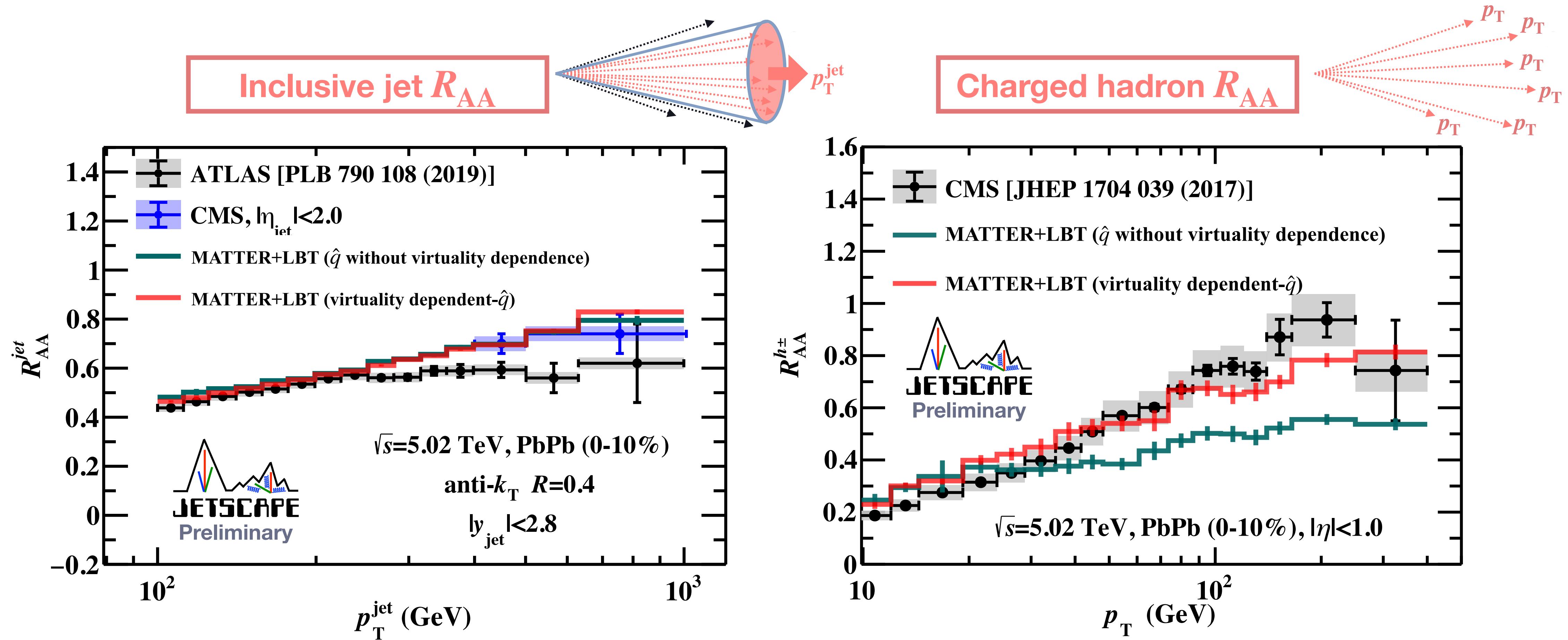


- Less interaction for larger virtuality partons
- Extend the model applicability to further broader scale

# Jet and high- $p_T$ particle energy loss

JERSCAPE (in preparation)

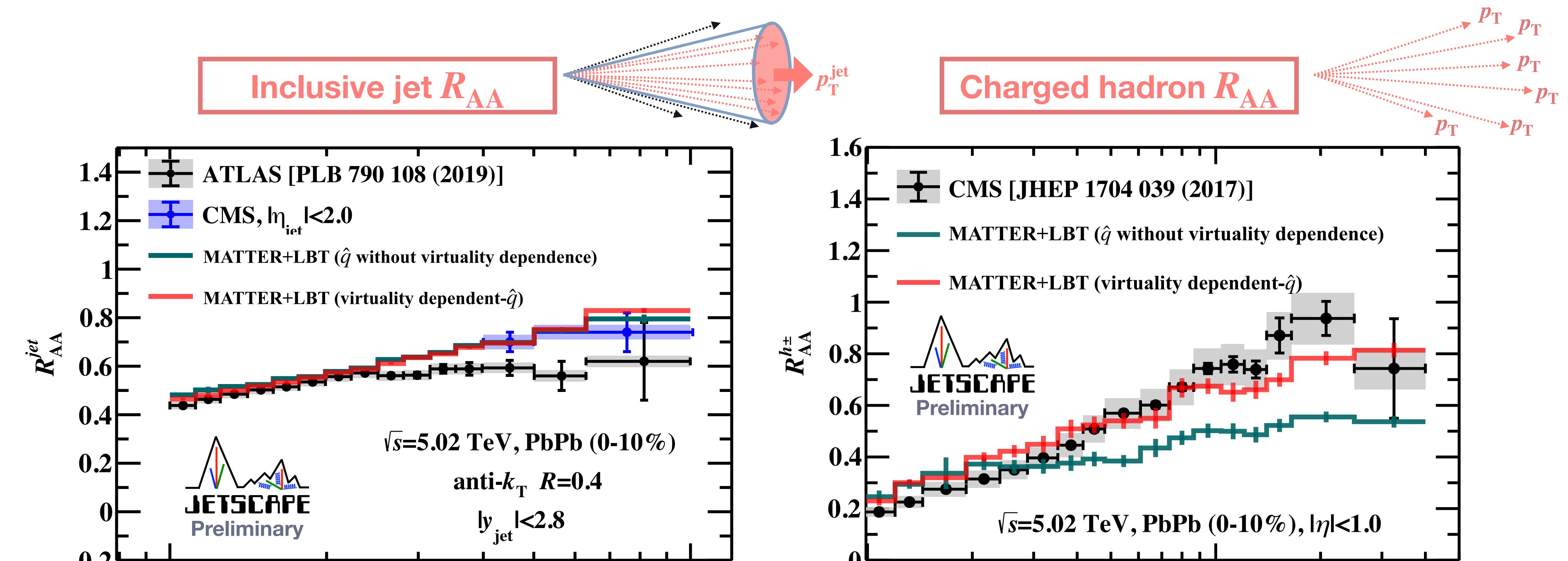
- Jet and high- $p_T$  particle energy loss for PbPb@5.02 TeV



# Jet and high- $p_T$ particle energy loss

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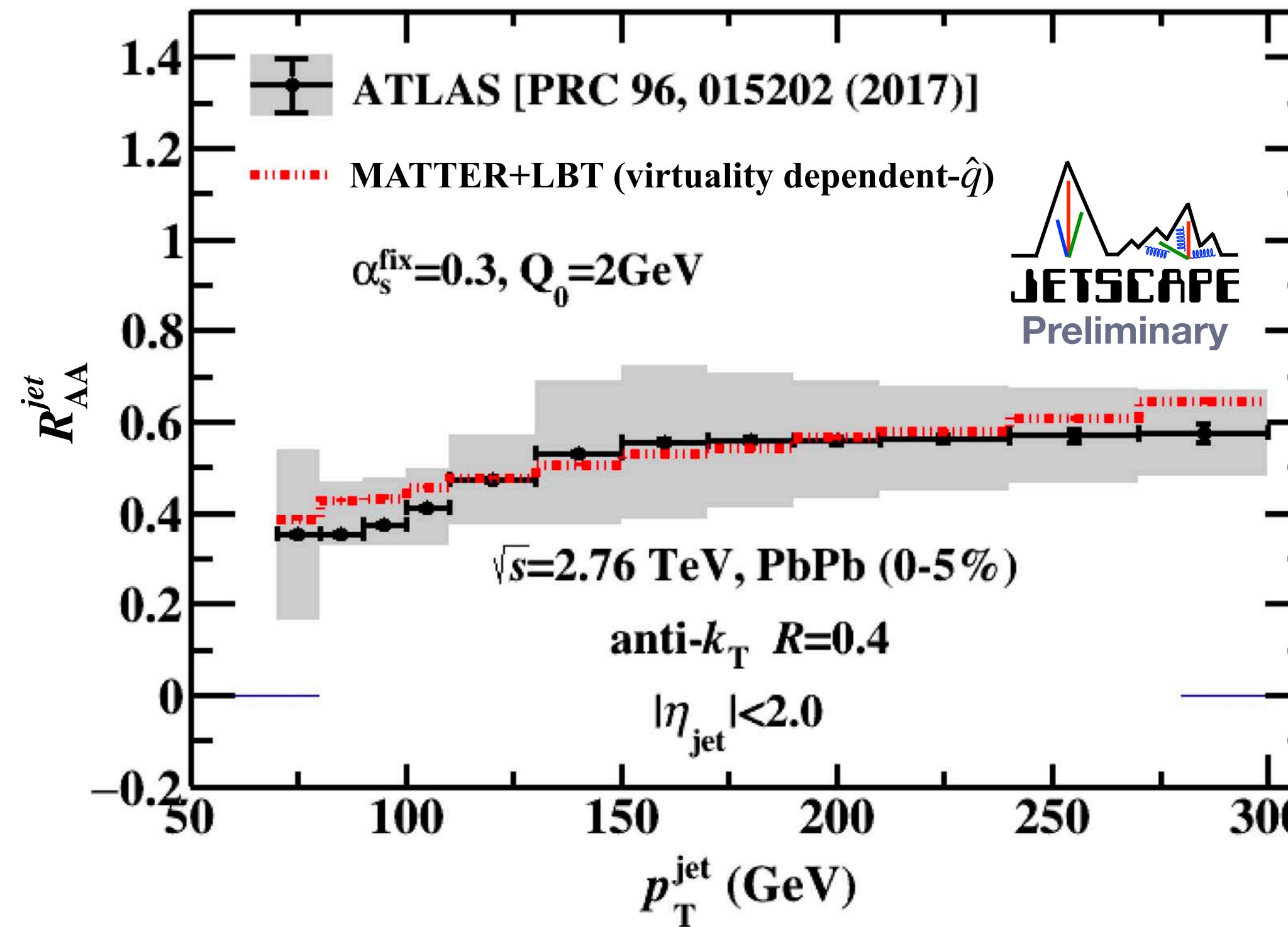
- Very first success in simultaneous description of data for jet and hadrons
- Significant effect of virtuality dependence in energy loss

# Jet and high- $p_{\text{T}}$ particle energy loss

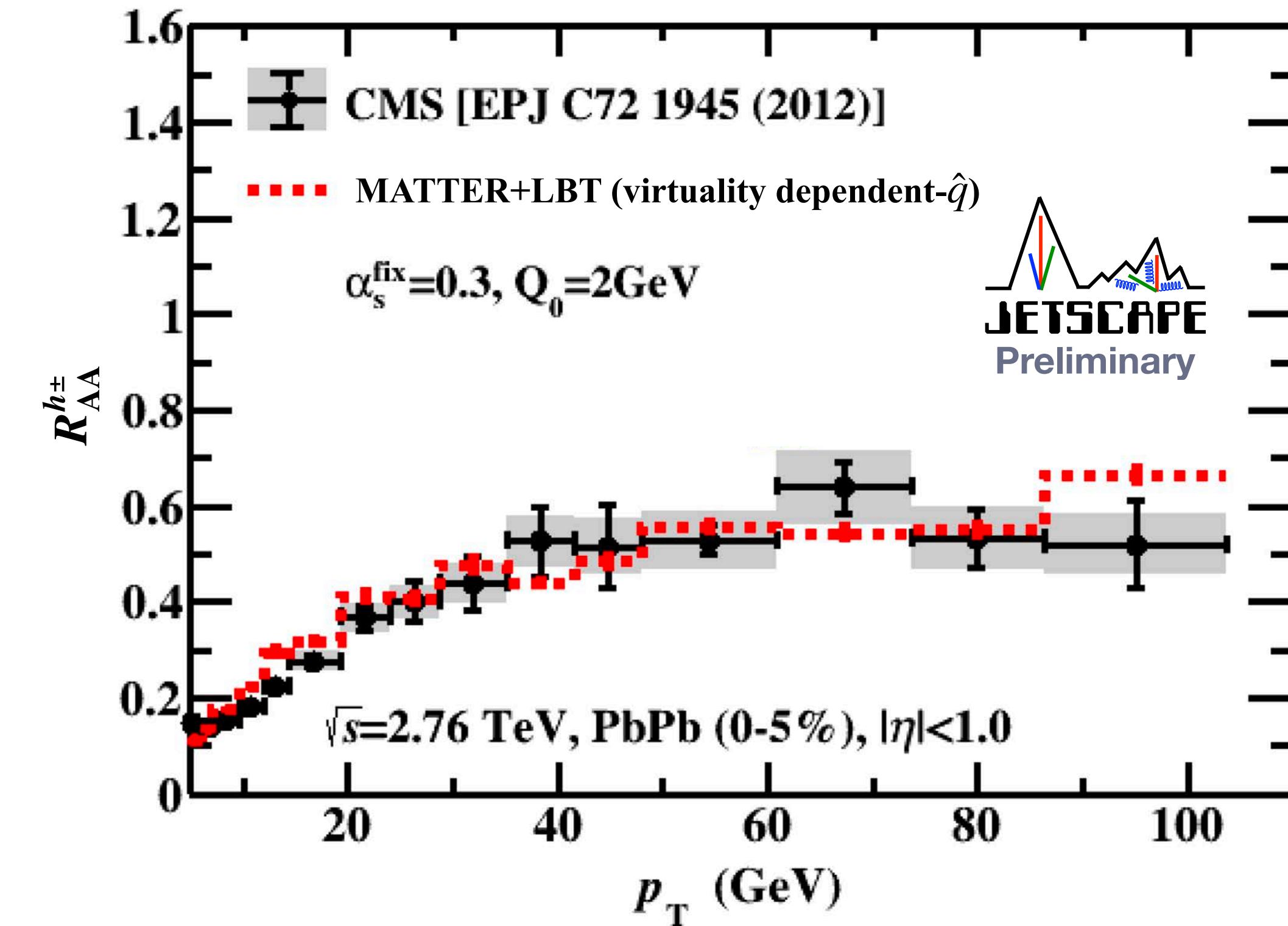
- Jet and high- $p_{\text{T}}$  particle energy loss for PbPb@2.76 TeV

The same parameter set as 5.02 TeV is used

Inclusive jet  $R_{\text{AA}}$



Charged hadron  $R_{\text{AA}}$



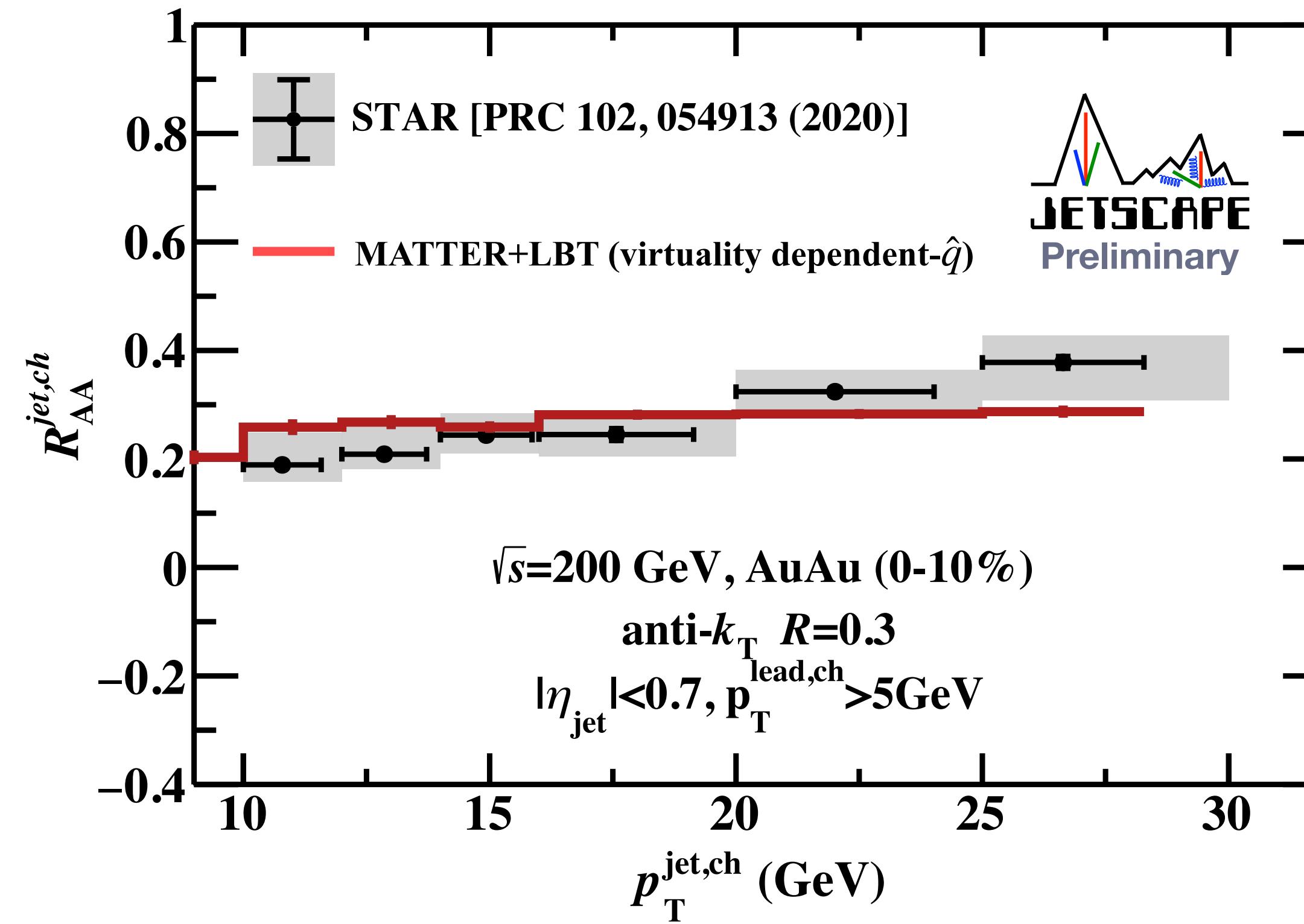
# Jet and high- $p_T$ particle energy loss

JERSCAPE (in preparation)

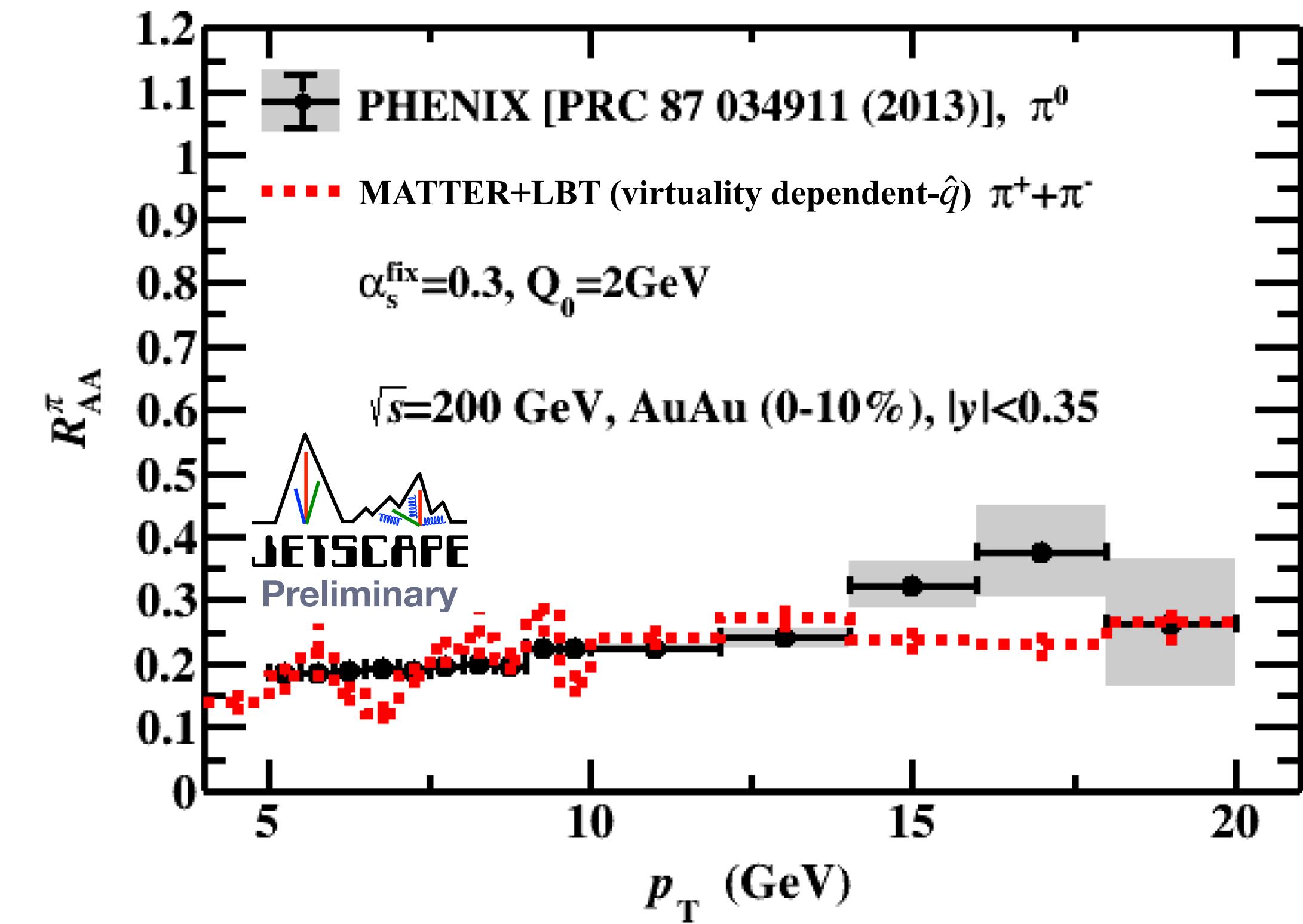
- Jet and high- $p_T$  particle energy loss for AuAu@200 GeV

The same parameter set as 5.02 TeV is used

Charged jet  $R_{AA}$



Pion  $R_{AA}$



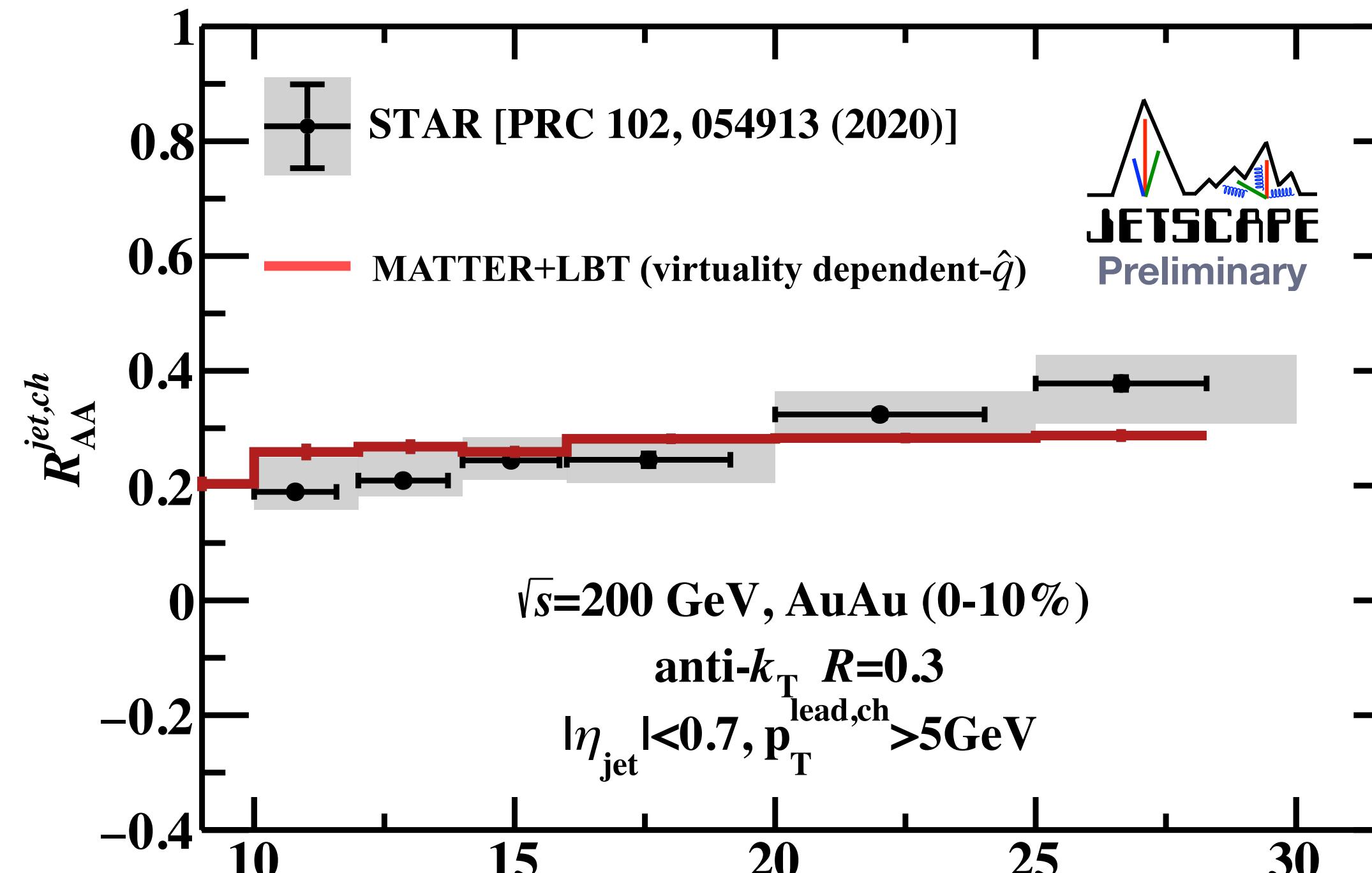
# Jet and high- $p_T$ particle energy loss

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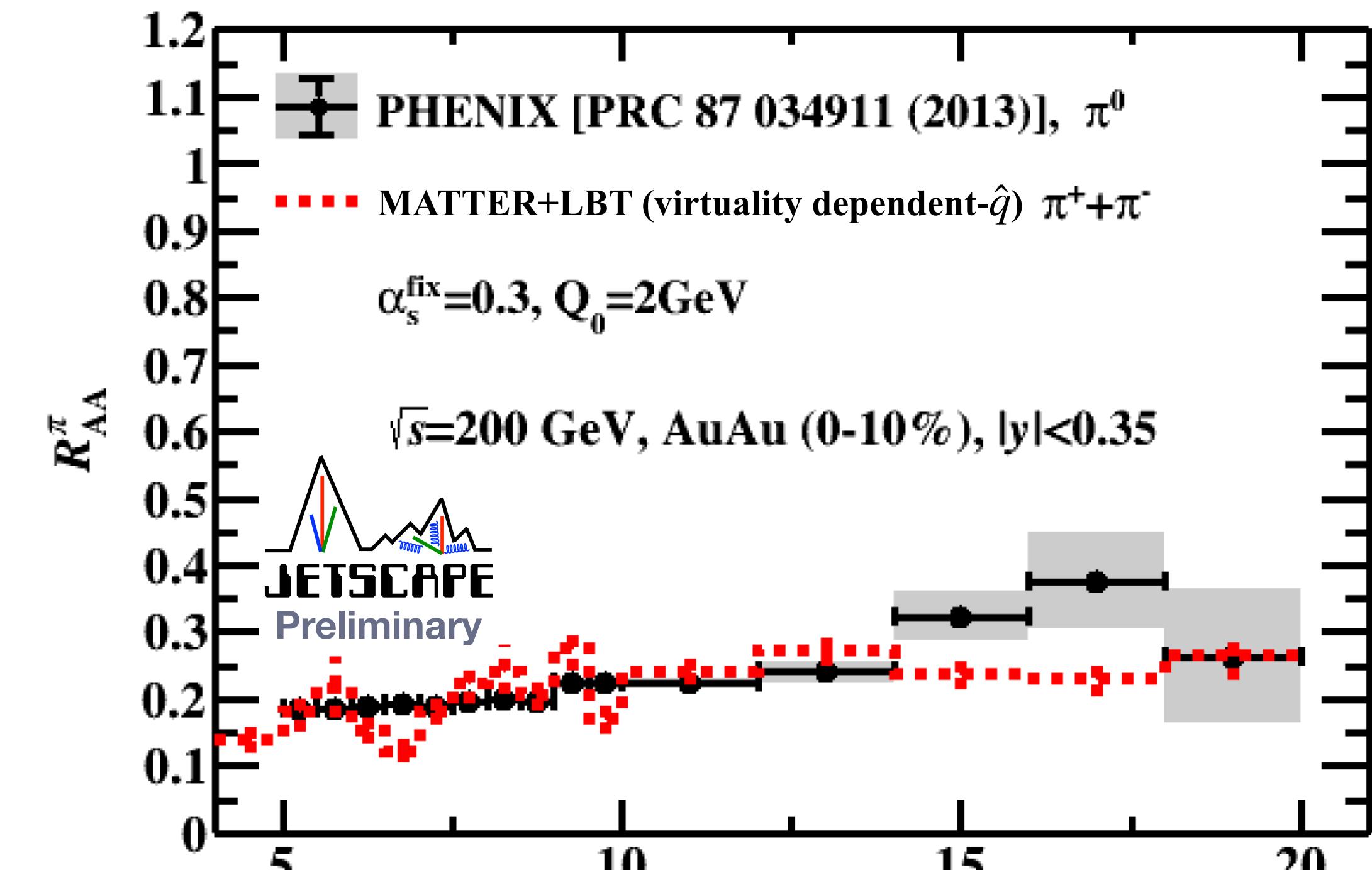
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Charged jet  $R_{AA}$



Pion  $R_{AA}$



- Simultaneous description of different  $\sqrt{s_{NN}}$  with the same parameter set



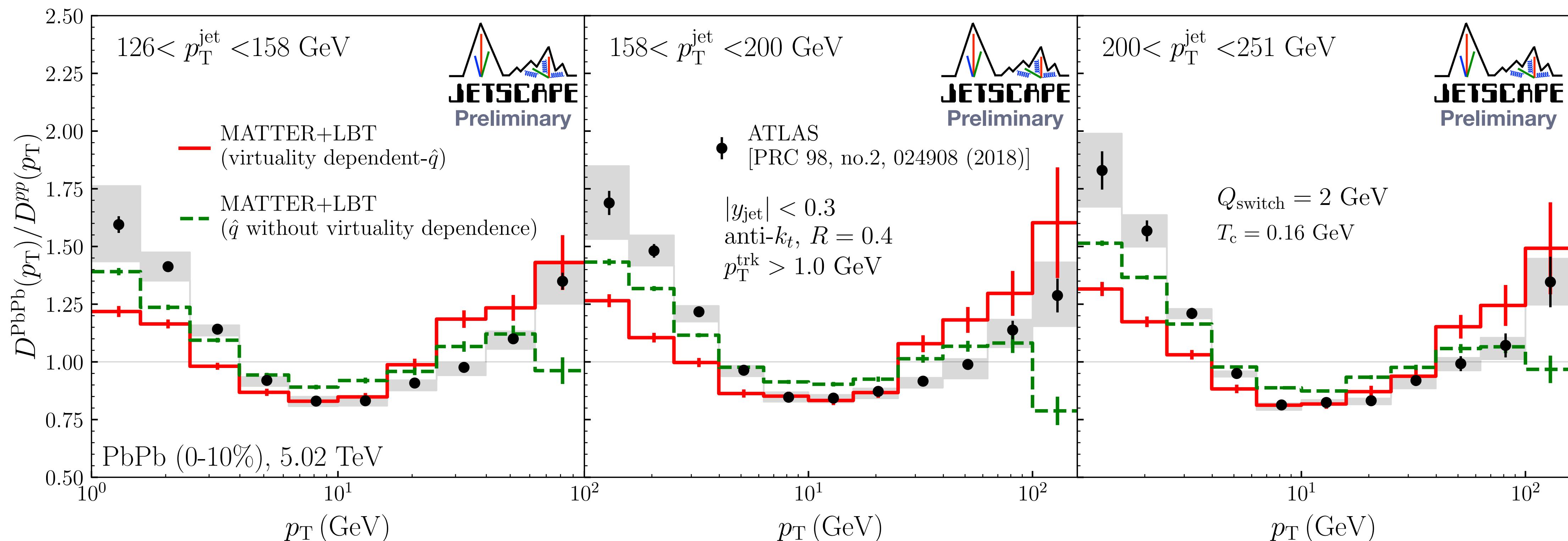
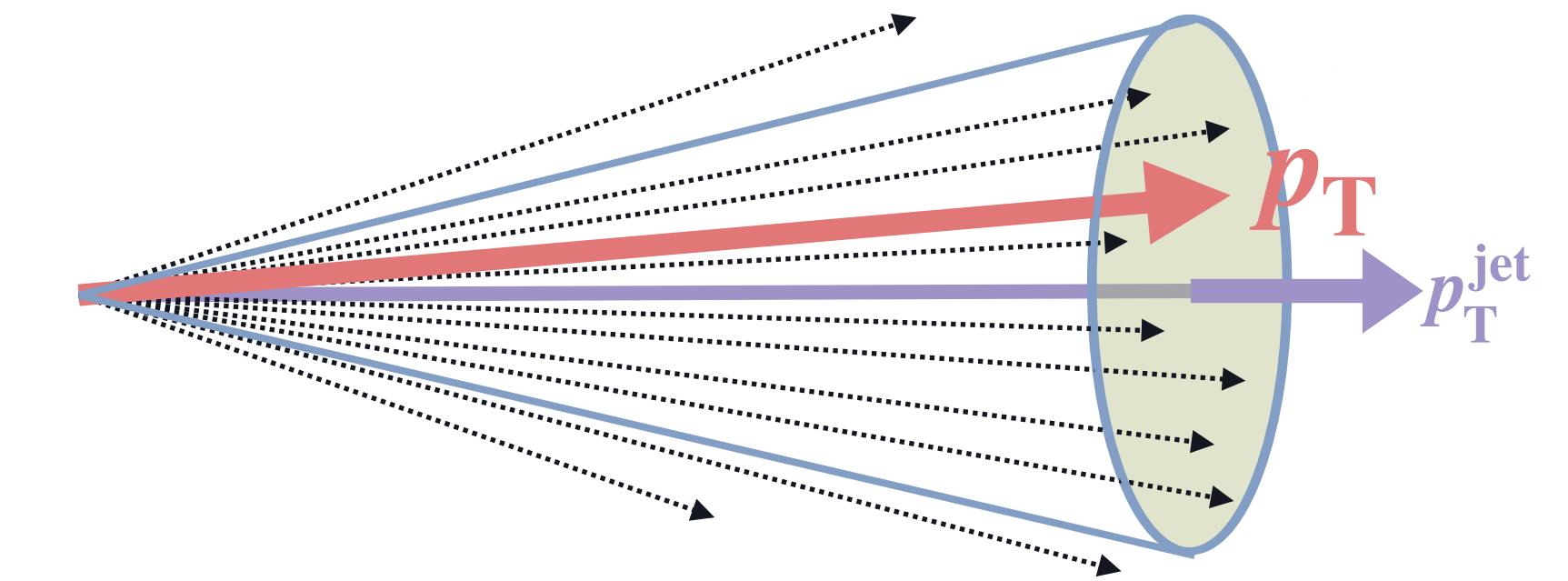
# Jet substructure

JERSCAPE (in preparation)

- **Jet Fragmentation Function**

- $p_T$  distribution of charged particle inside jets

$$D(p_T) = \frac{1}{N_{\text{jet}}} \sum_{\text{jet}} \left. \frac{dN_{\text{ch}}}{dp_T} \right|_{\text{in jet}}$$



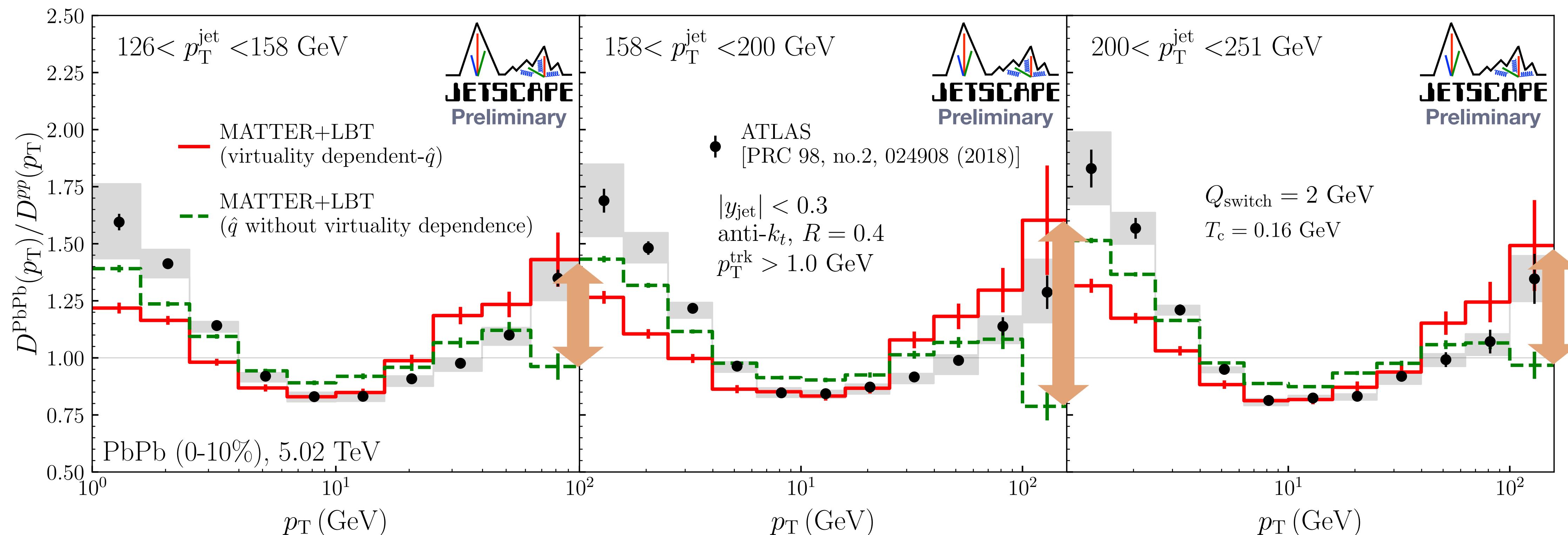
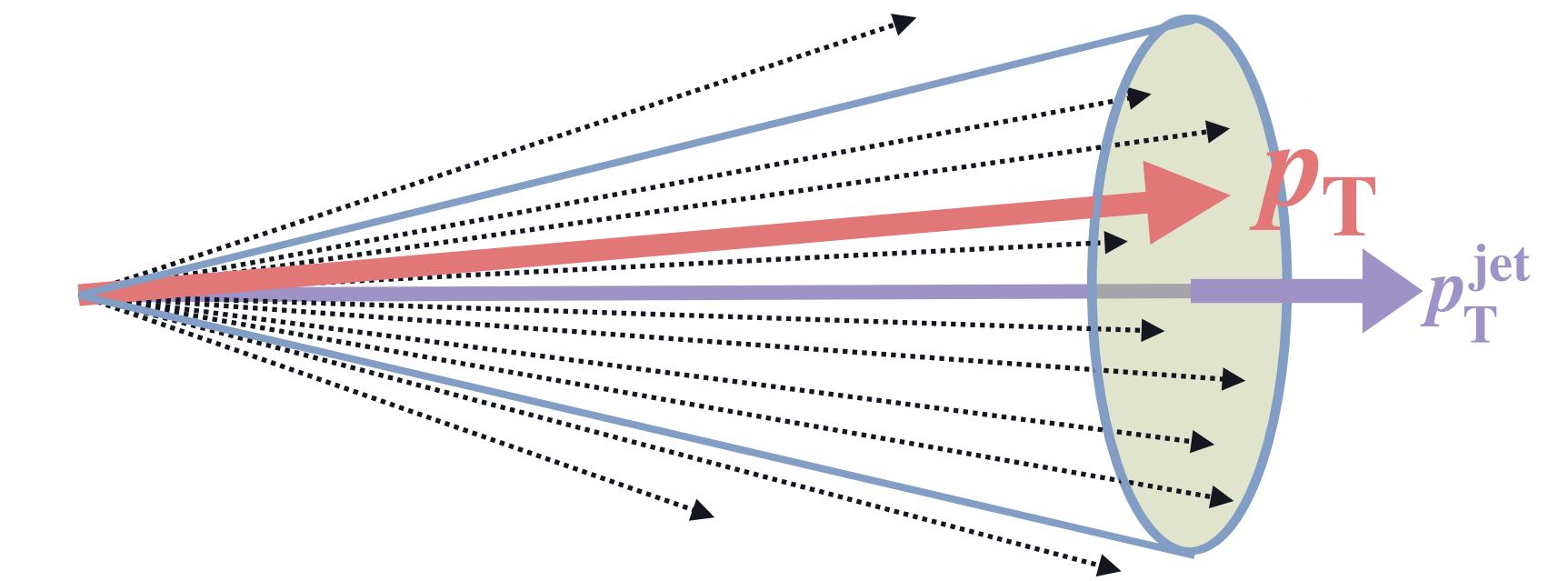
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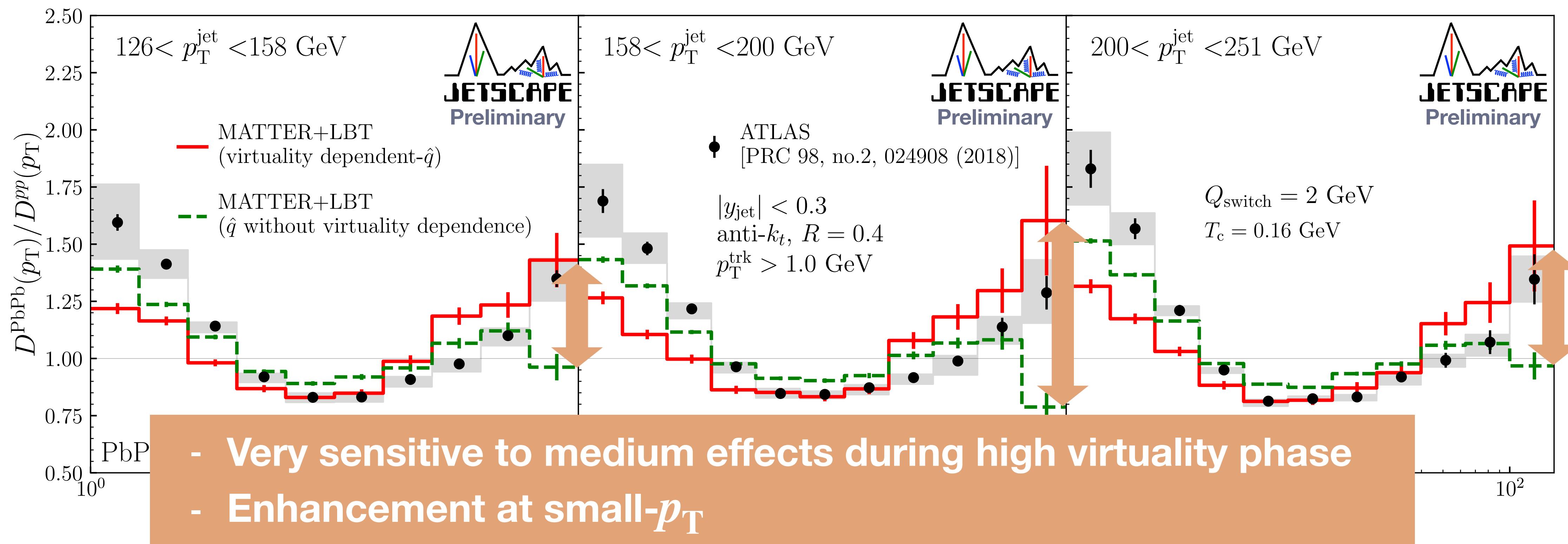
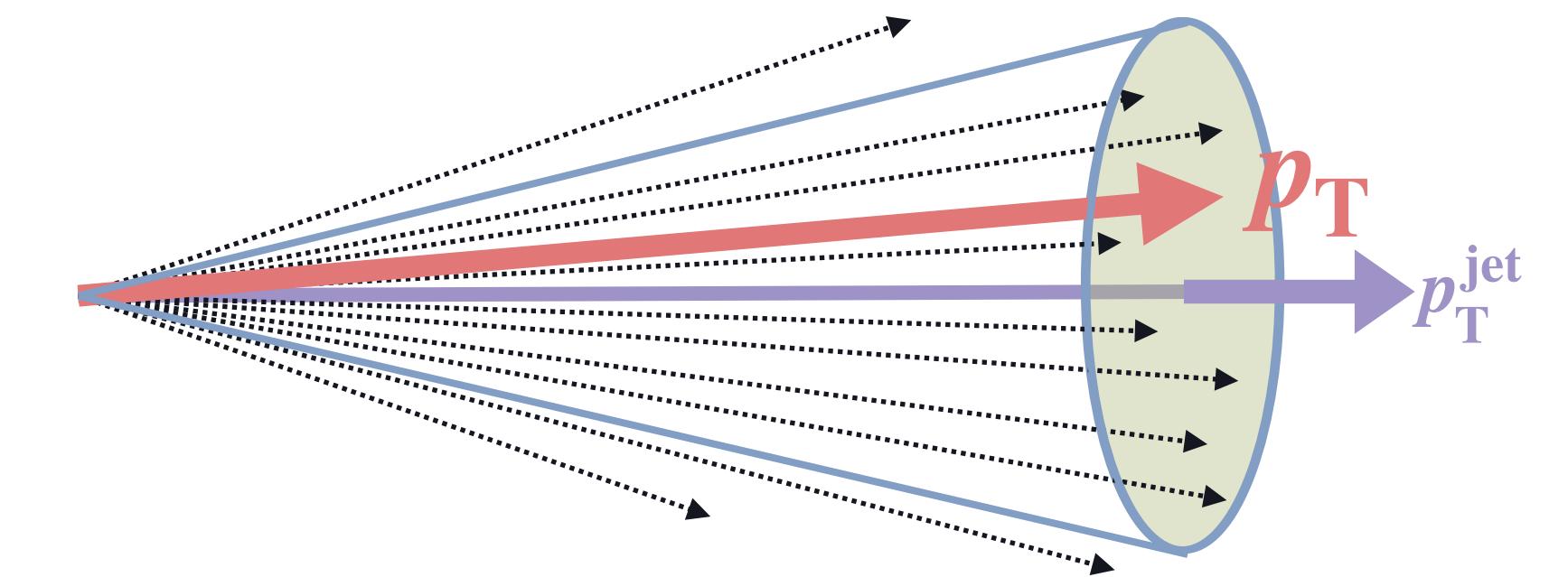
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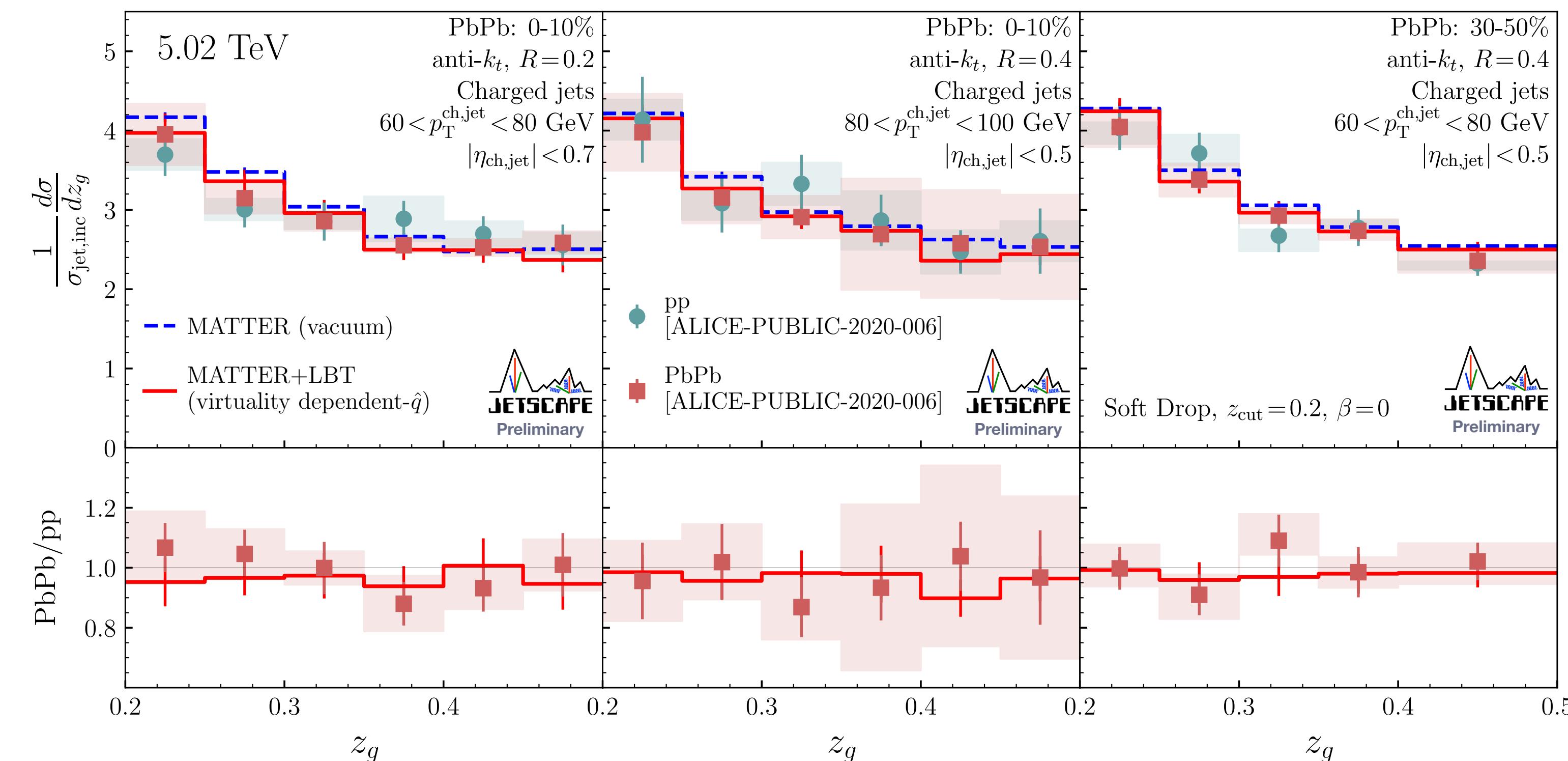
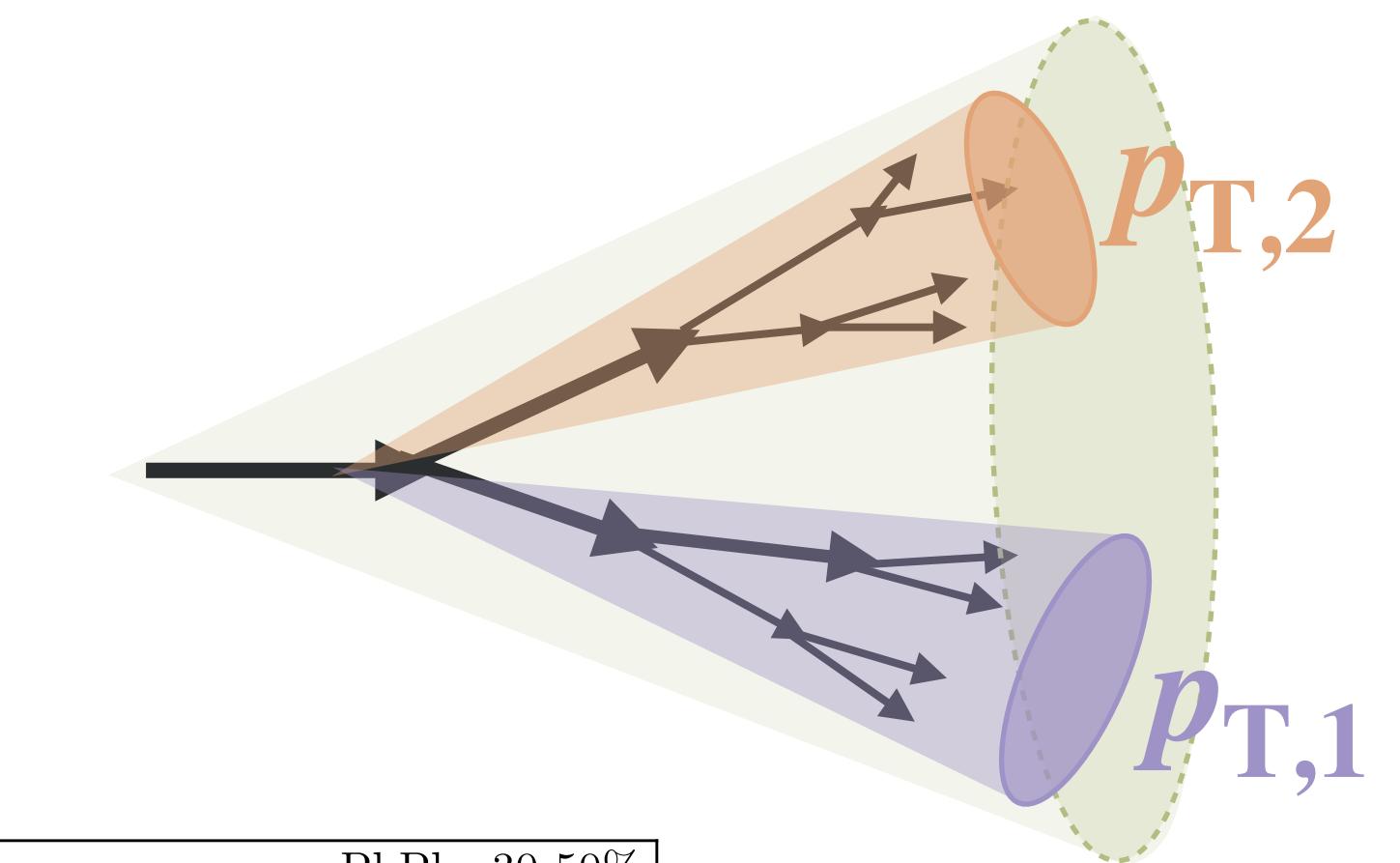
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- Momentum fraction in the hardest splitting of jet ( $z_g$ )

$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}}$$



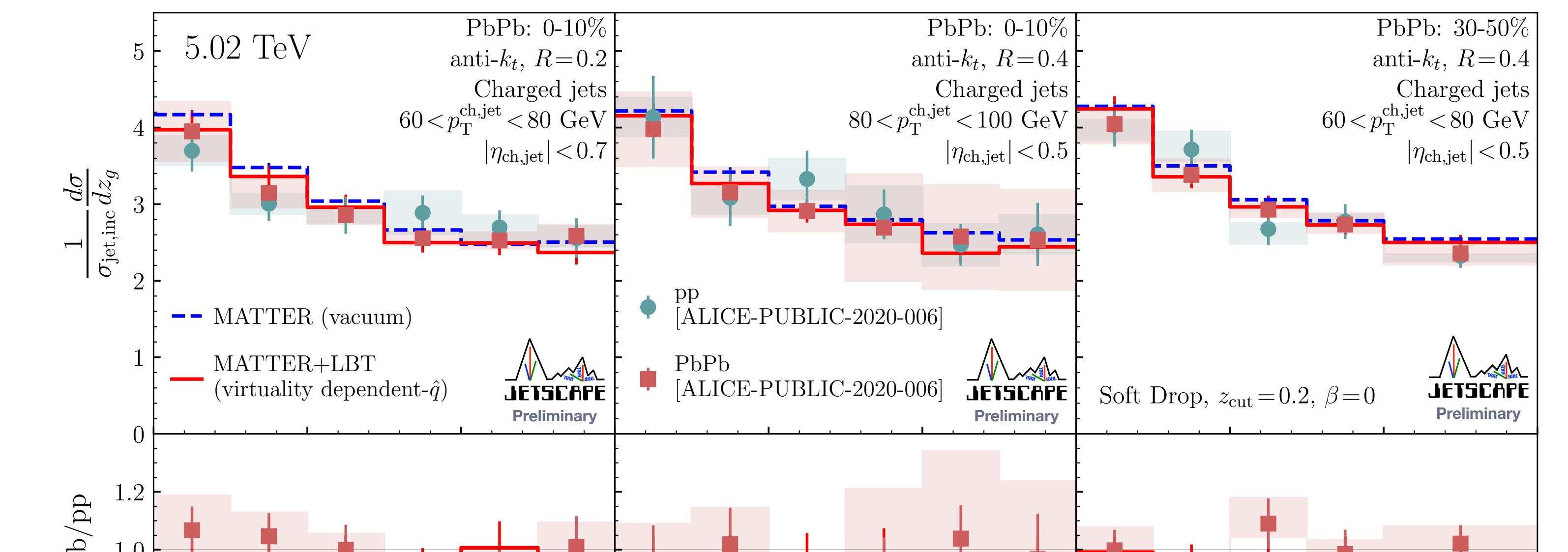
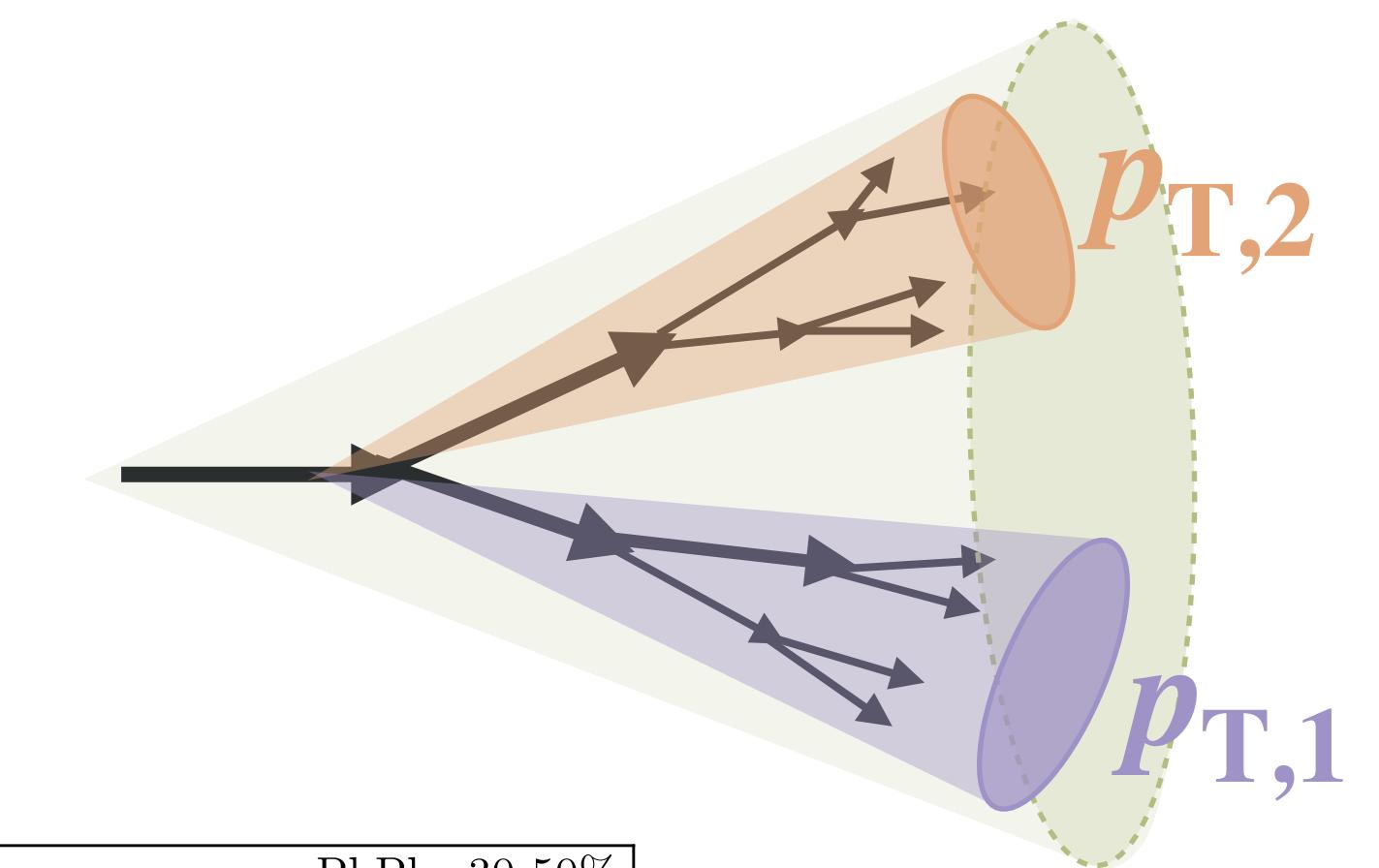
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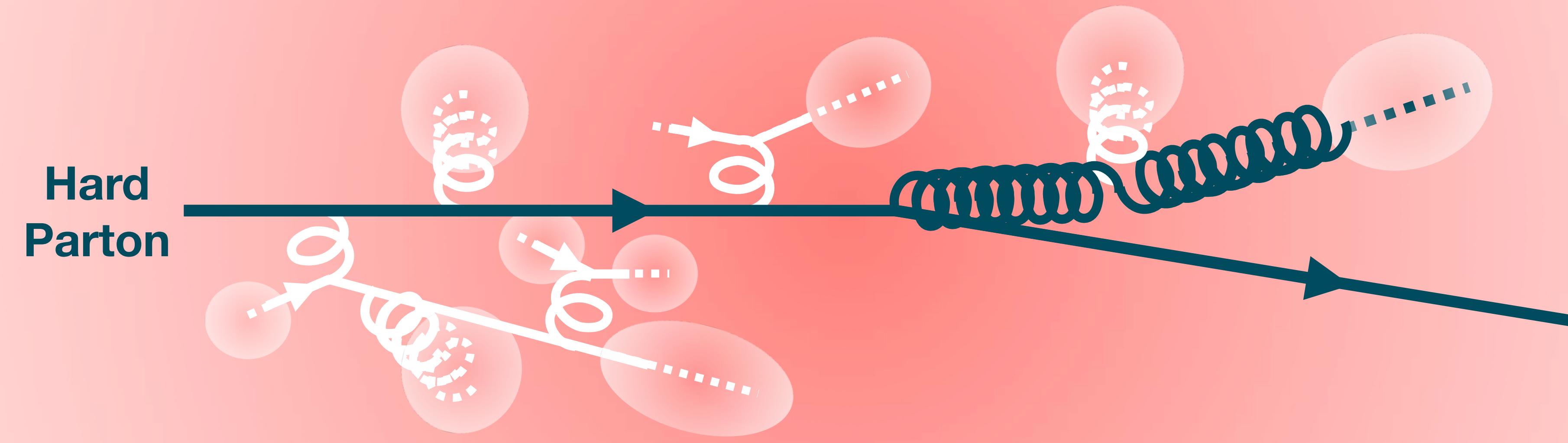
$$z_g = \frac{\min(p_{T,1}, p_{T,2})}{p_{T,1} + p_{T,2}}$$



- Good agreement with experimental data
- Almost no medium modification in hardest splittings

# Fluid + Jet Approach for Hydro Response

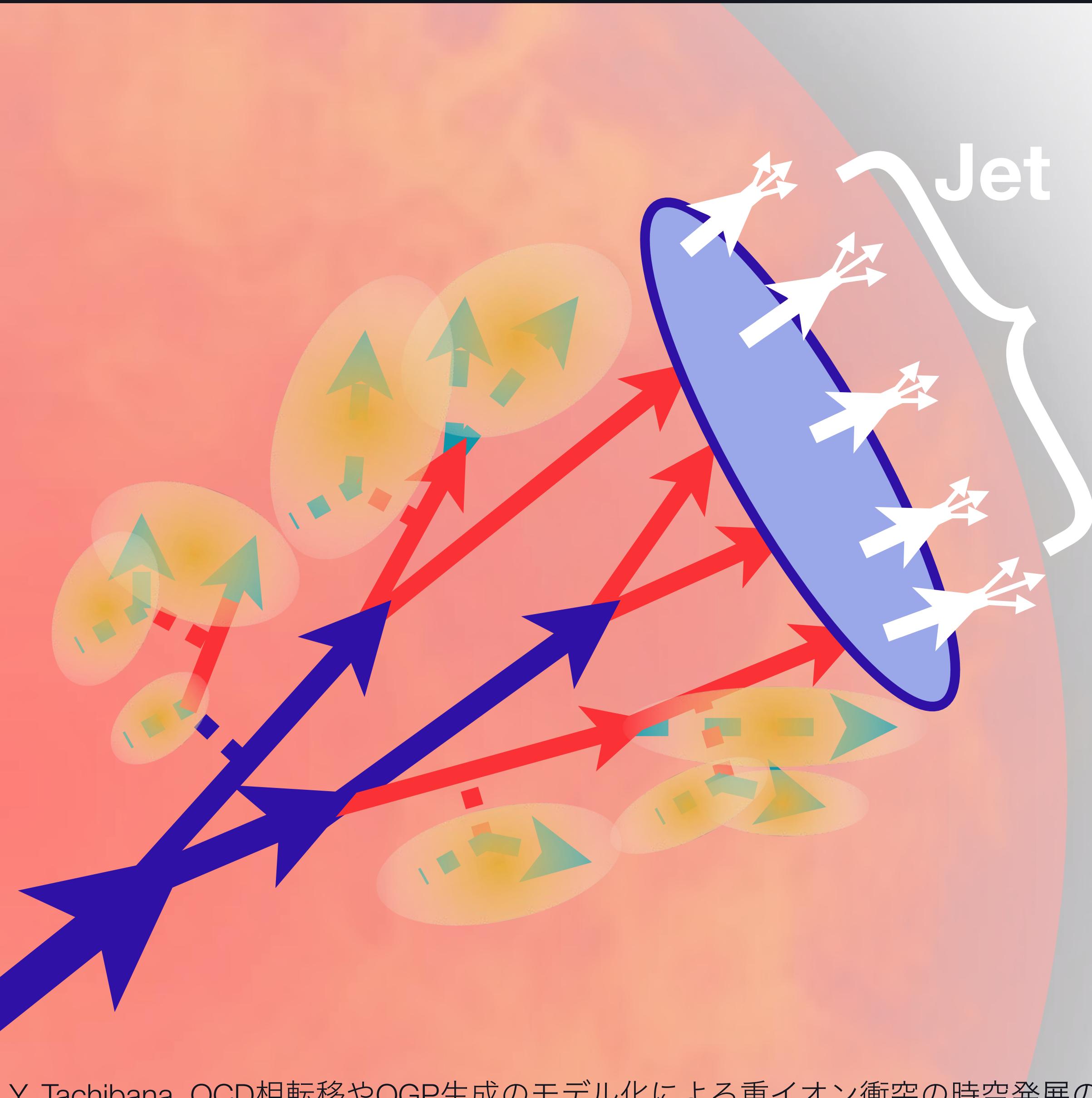
# Hydrodynamic Medium Response to Hard Partons



- **In-medium thermalization**

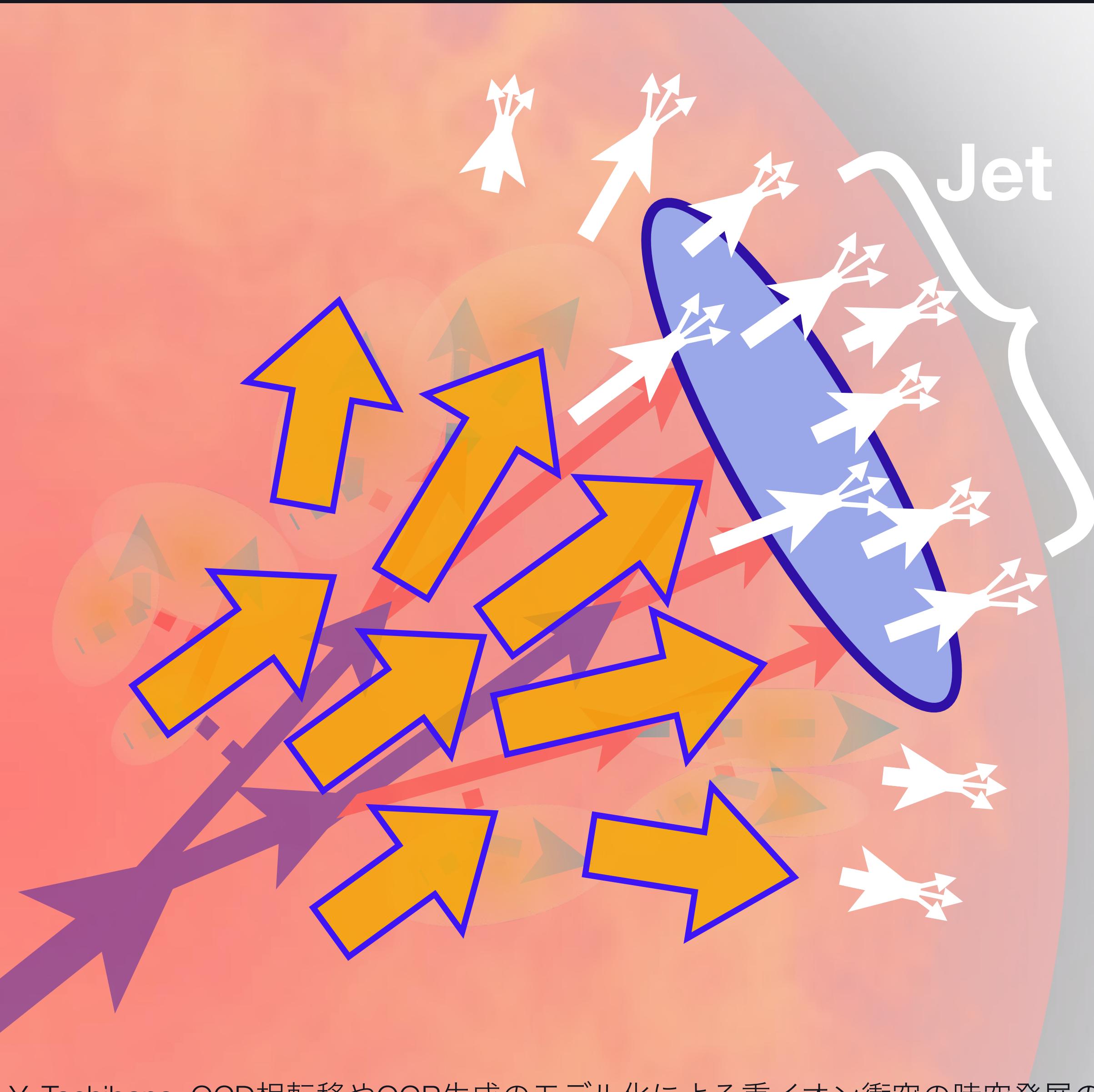
- Drop to typical scale of thermalized medium constituents ( $E \sim E_{\text{med}}$ )
- Transition to hydrodynamic transport → Hydrodynamic medium response

# Hydrodynamic Medium Response Effect on Jets



- **Jet-induced flow in medium**
  - Transport momentum deposited by jet
  - Modify particle emission around jet
- **Hydro medium response contribution**
  - Soft, spread out from jet
  - Jet-correlated, cannot be subtracted
  - Affect structures inside/around jet

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# Description of Hydro Medium Response to Jets

## ● Medium fluid evolution with energy-momentum deposition

Coupled Jet-Fluid (YT, N.-B. Chang, G.-Y. Qin), CoLBT-hydro (W. Chen, X.-N. Wang, W. Zhao,...)

EPOS3-HQ (I. Karpenko,...), JETSCAPE (JETSCAPE), Hybrid+Linearized Hydro (X. Yao, D. Pablos,...),

LEXUS+MUSIC (C.Shen, B. Schenke,...), DCCI2 (Y. Kanakubo, YT, T. Hirano,...), JAM (Y.Nara),...

- Hydrodynamic transport of jet energy-momentum via thermal partons
- Evolution together with the bulk QGP fluid

### Hydrodynamic equation with source term

$$\nabla_\mu T_{\text{med}}^{\mu\nu}(x) = J_{\text{jet}}^\nu(x)$$

Energy-momentum tensor  
of the QGP fluid

Energy and momentum  
deposited into the fluid

- Source term  $J_{\text{jet}}^\nu$  constructed from jet-shower evolution calculation
- Bulk part particle with hydro response obtained via the Cooper-Frye

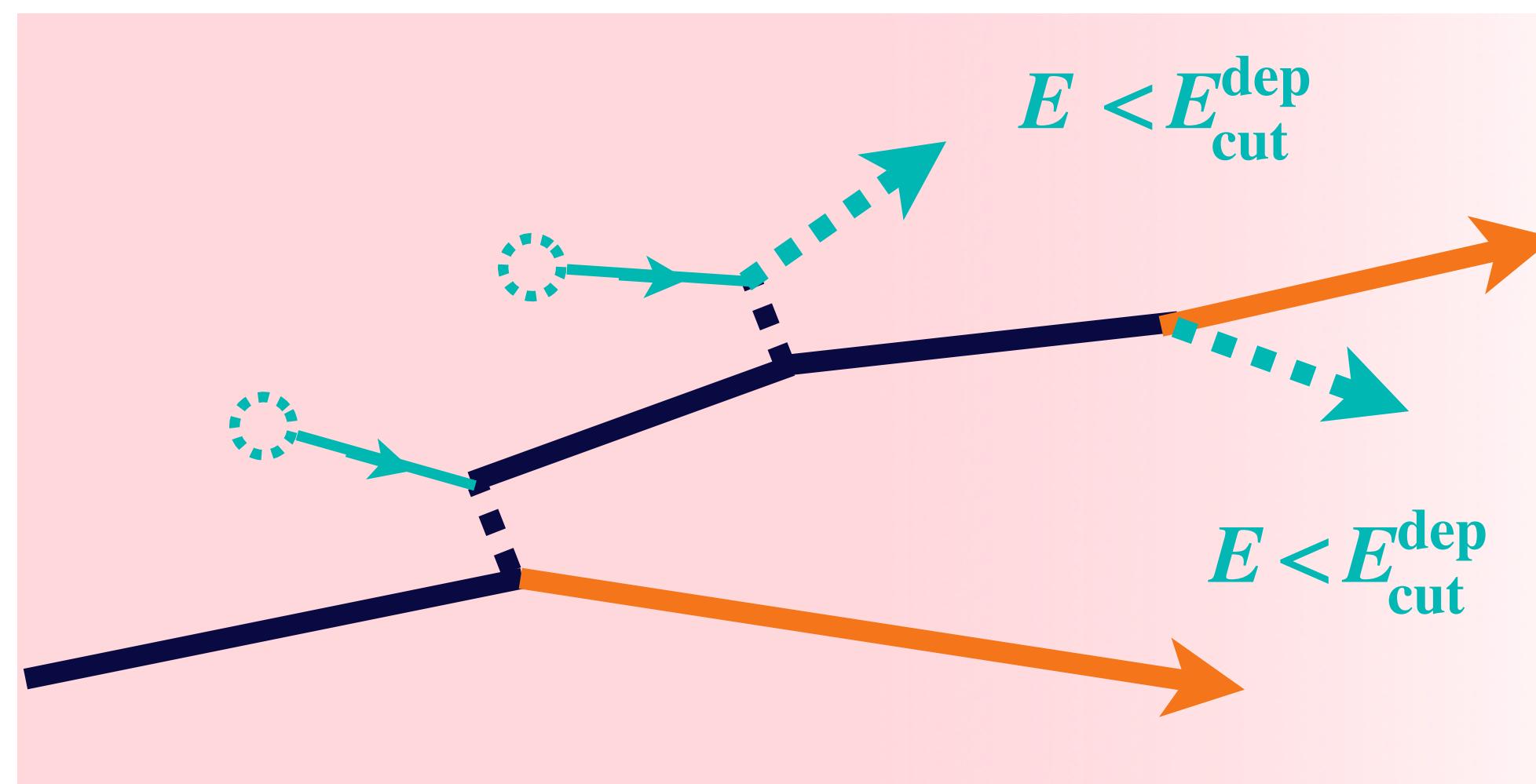
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YT, C. Shen and A. Majumder, arXiv:2001.08321

## ● Energy-momentum deposition

CoLBT-hydro (W. Chen, X.-N. Wang et al.)

- Soft partons
- Holes



$E_{\text{cut}}^{\text{dep}}$ : Energy scale for in-medium thermalization

## ● Causal source profile

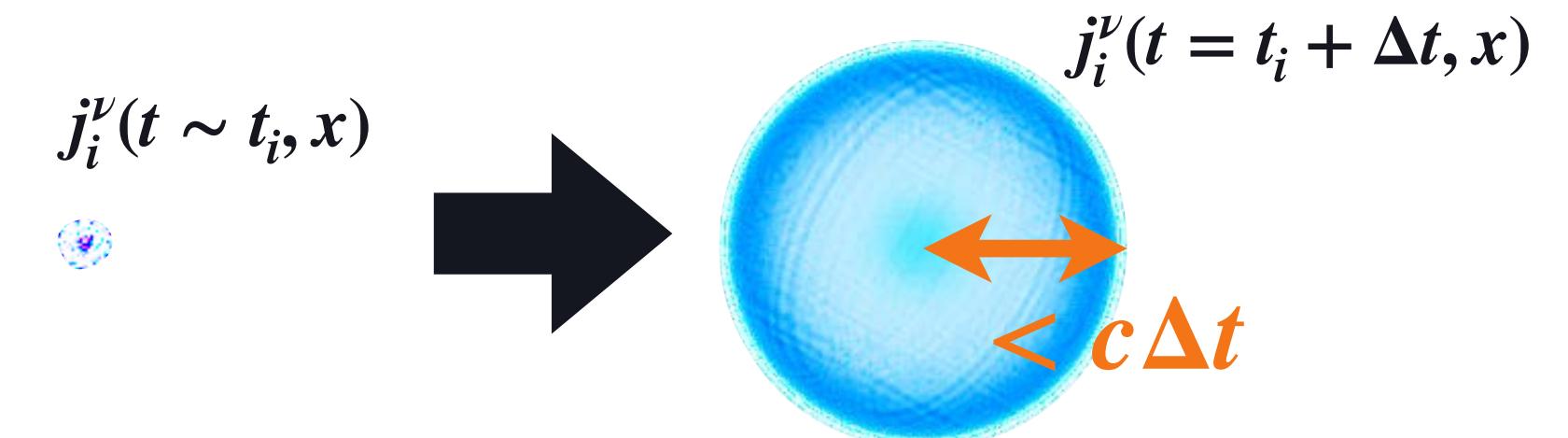
JETSCAPE (JETSCAPE)

- Relativistic diffusion equation

$$\left[ \frac{\partial}{\partial t} + \tau_{\text{diff}} \frac{\partial^2}{\partial t^2} - D_{\text{diff}} \nabla^2 \right] j^\nu(x) = 0$$

with initial condition

$$j^\nu(t = t_{\text{dep}}, \vec{x}) = p_{\text{dep}}^\nu \delta^{(3)}(\vec{x} - \vec{x}_{\text{dep}})$$



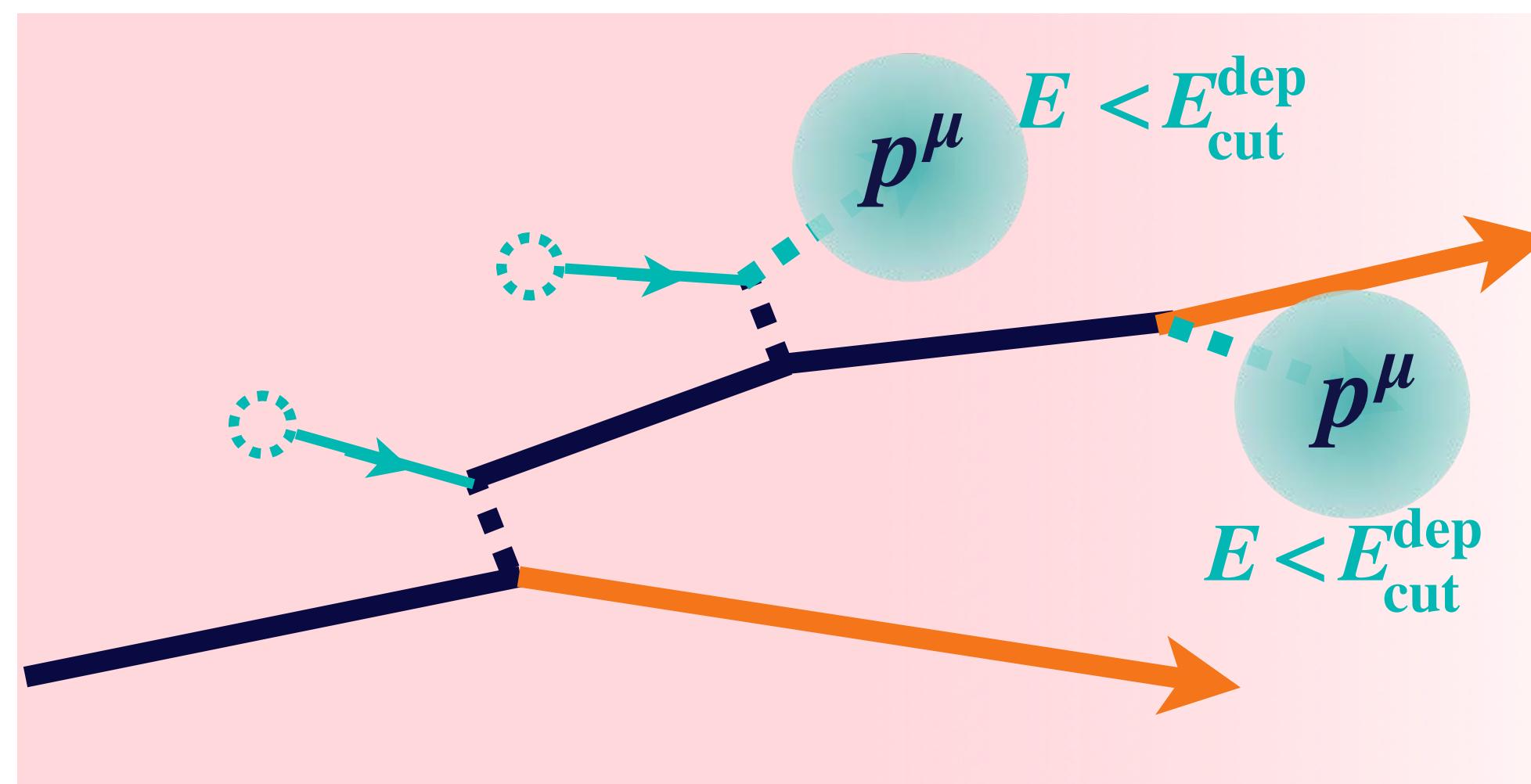
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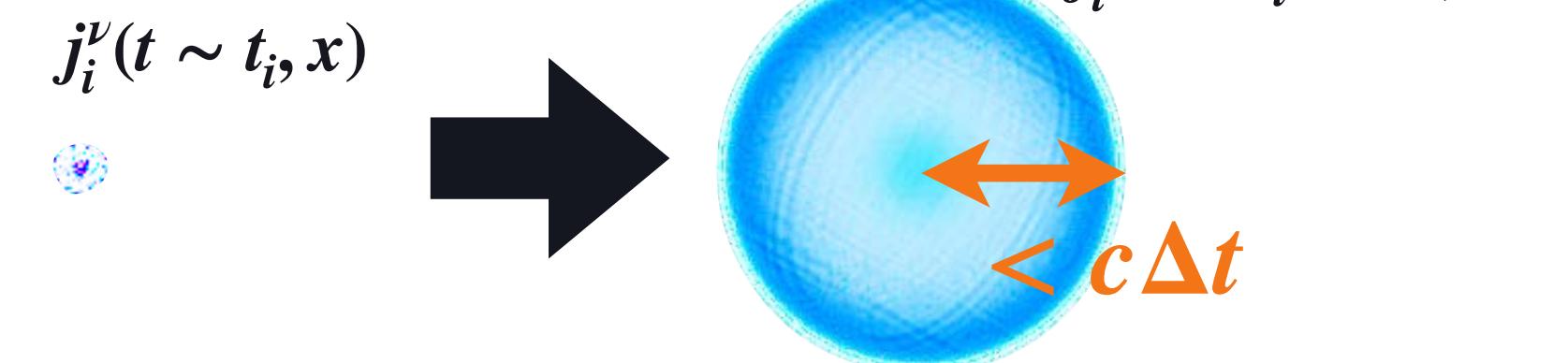
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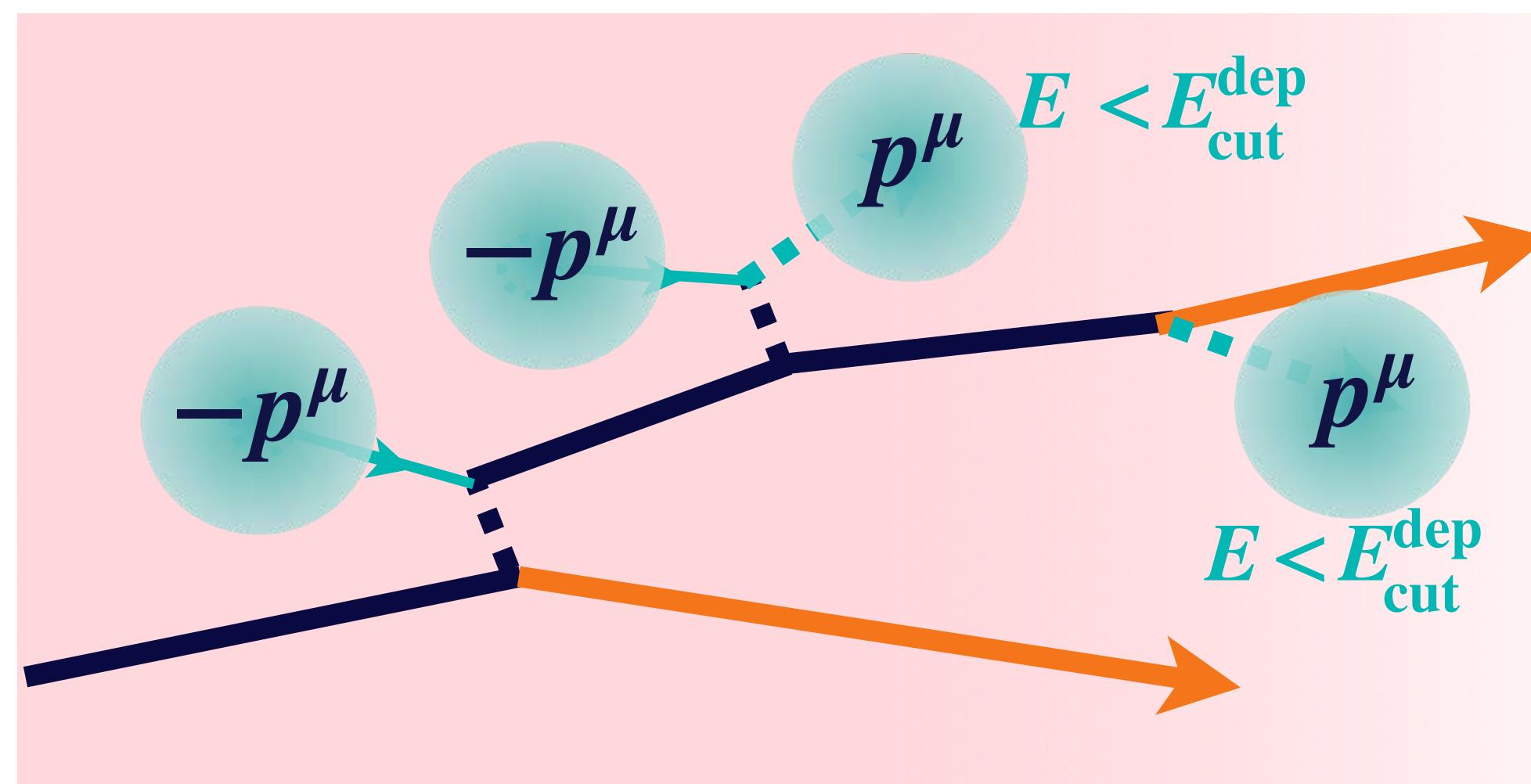
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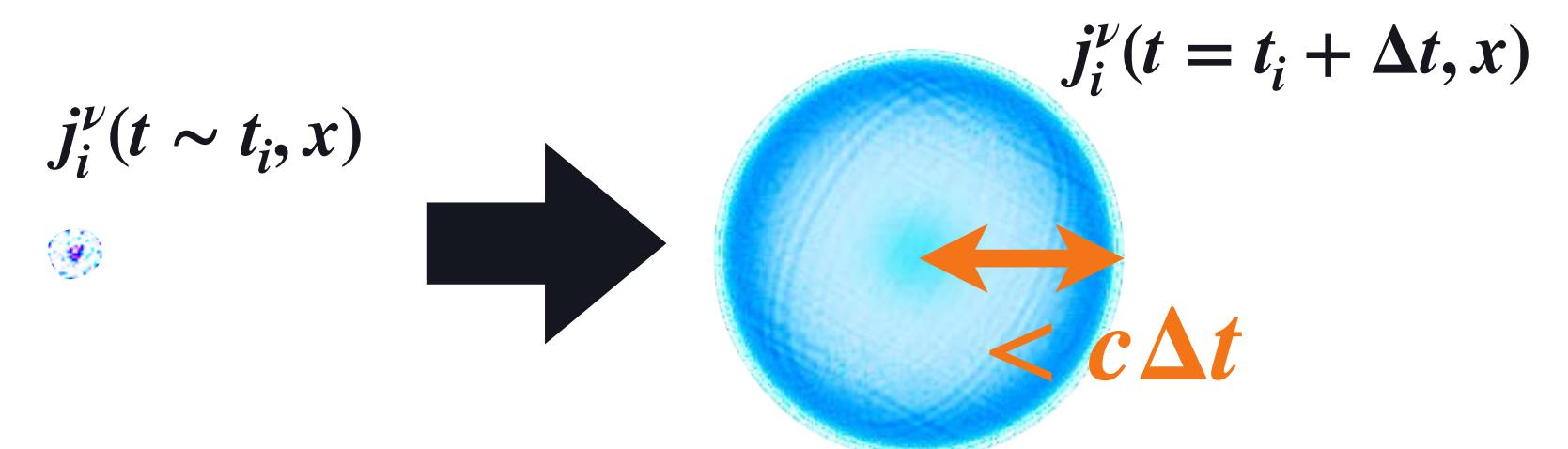
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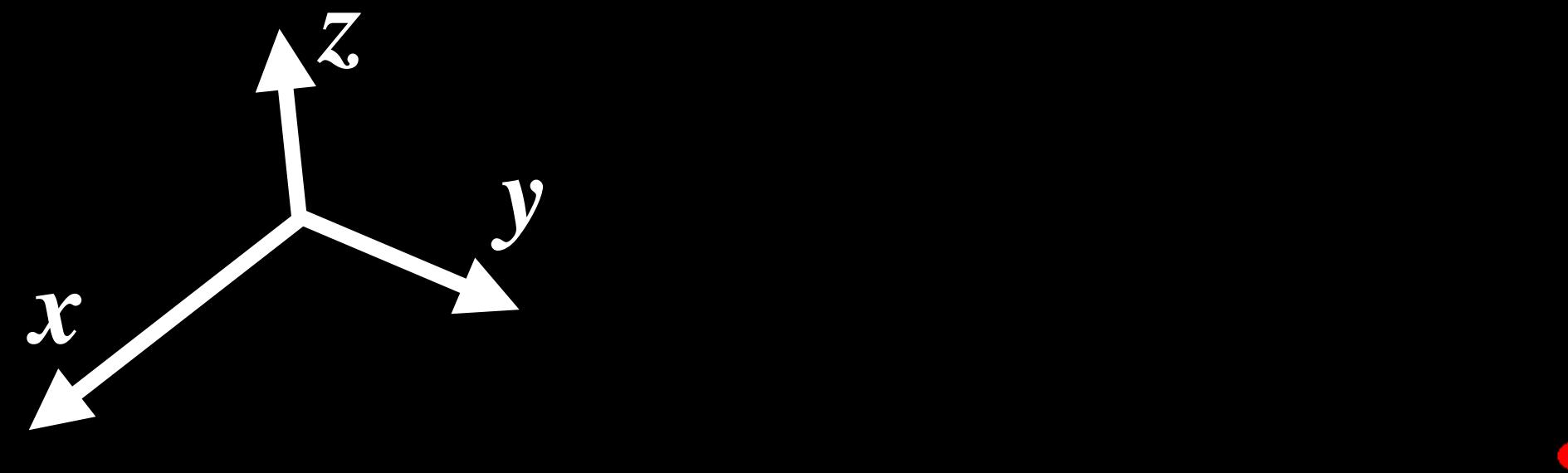
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# Evolution of Hydrodynamic Medium Response

MATTER + LBT + Causal Diff. + Ideal Hydro [Static Brick,  $T_{\text{brick}} = 250 \text{ MeV}$ ]  
YT, C. Shen, A. Majumder, arXiv:2001.08321

- Jet-Induced flow induced by a parton shower propagating in the  $x$  direction

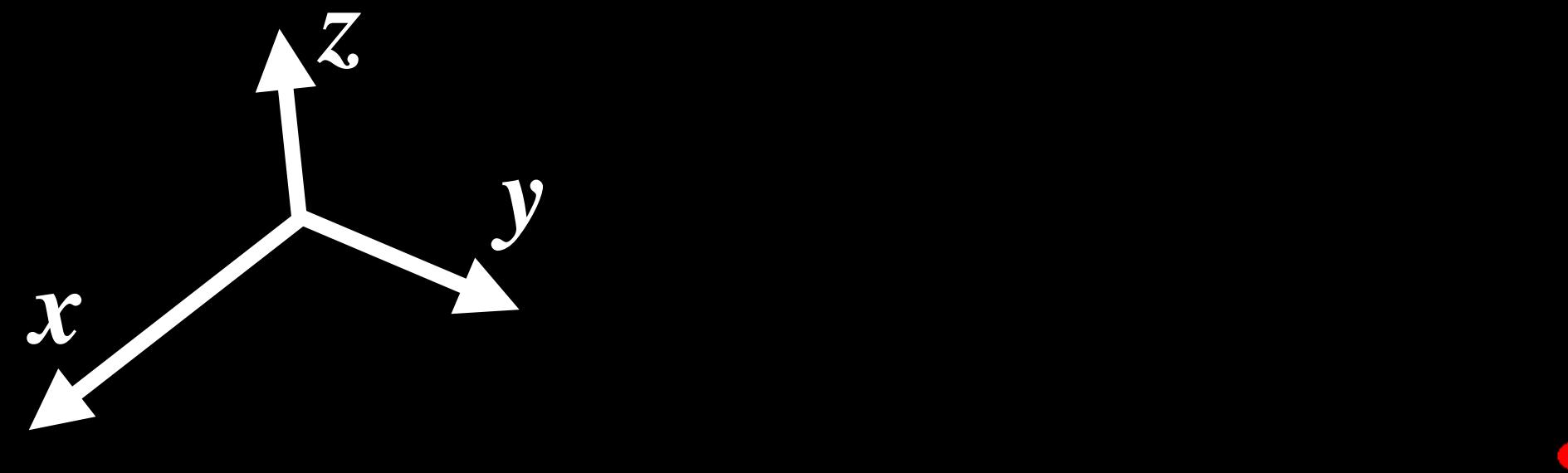


**Orange:** Region with  $T > 250 \text{ MeV}$   
**Blue:** Region with  $T < 250 \text{ MeV}$   
**Red:** Energetic Partons

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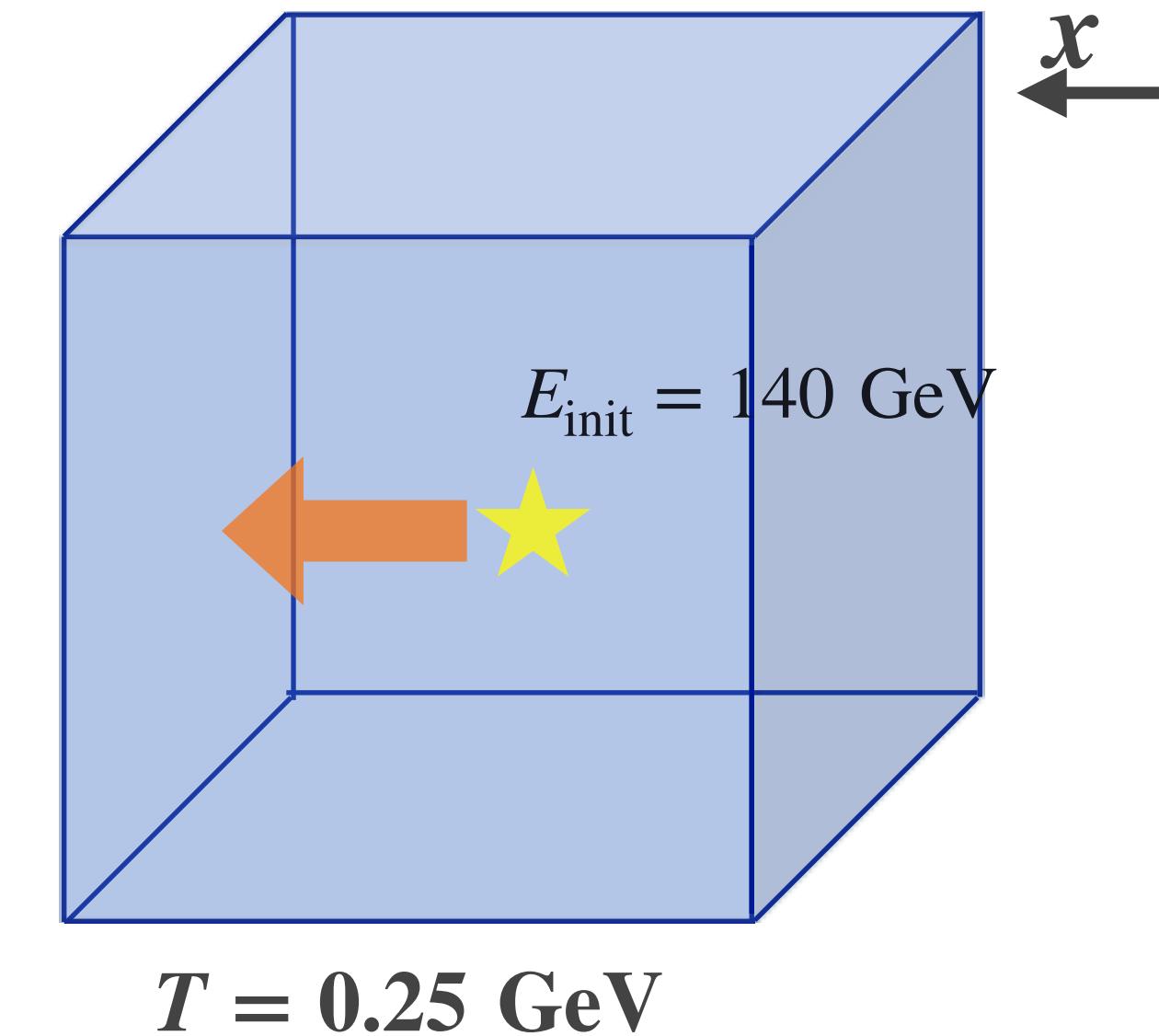
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# Recoil vs Recoil+Hydro response: Static brick case

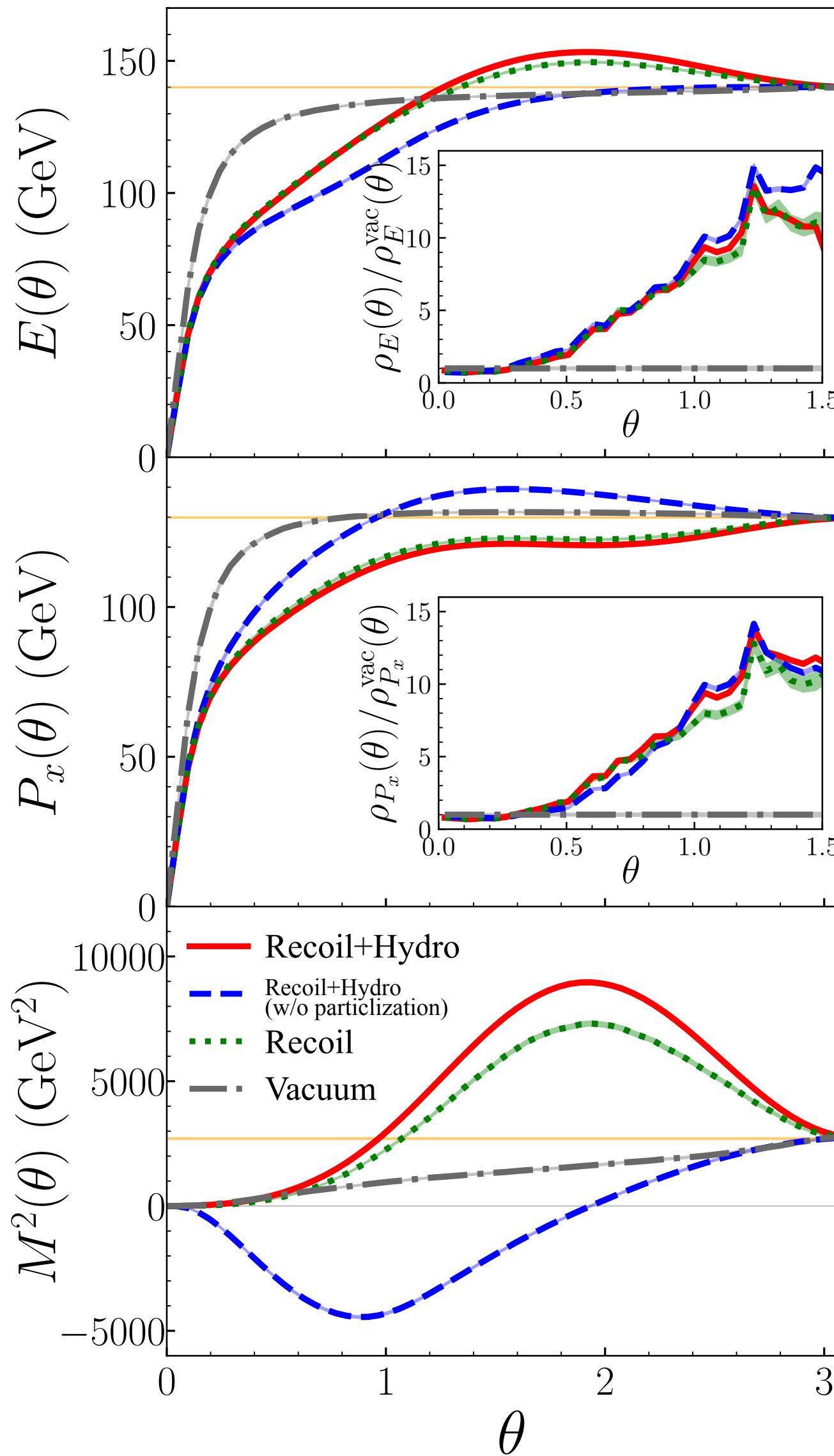
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- Jet propagation in medium with static uniform initial condition
- Energy loss by MATTER+LBT with recoils
- Medium evolves upto  $t = 10 \text{ fm}$

# Recoil vs Recoil+Hydro response: Static brick case

YT, C. Shen and A. Majumder, arXiv:2001.08321



## Angular structure of jet in brick

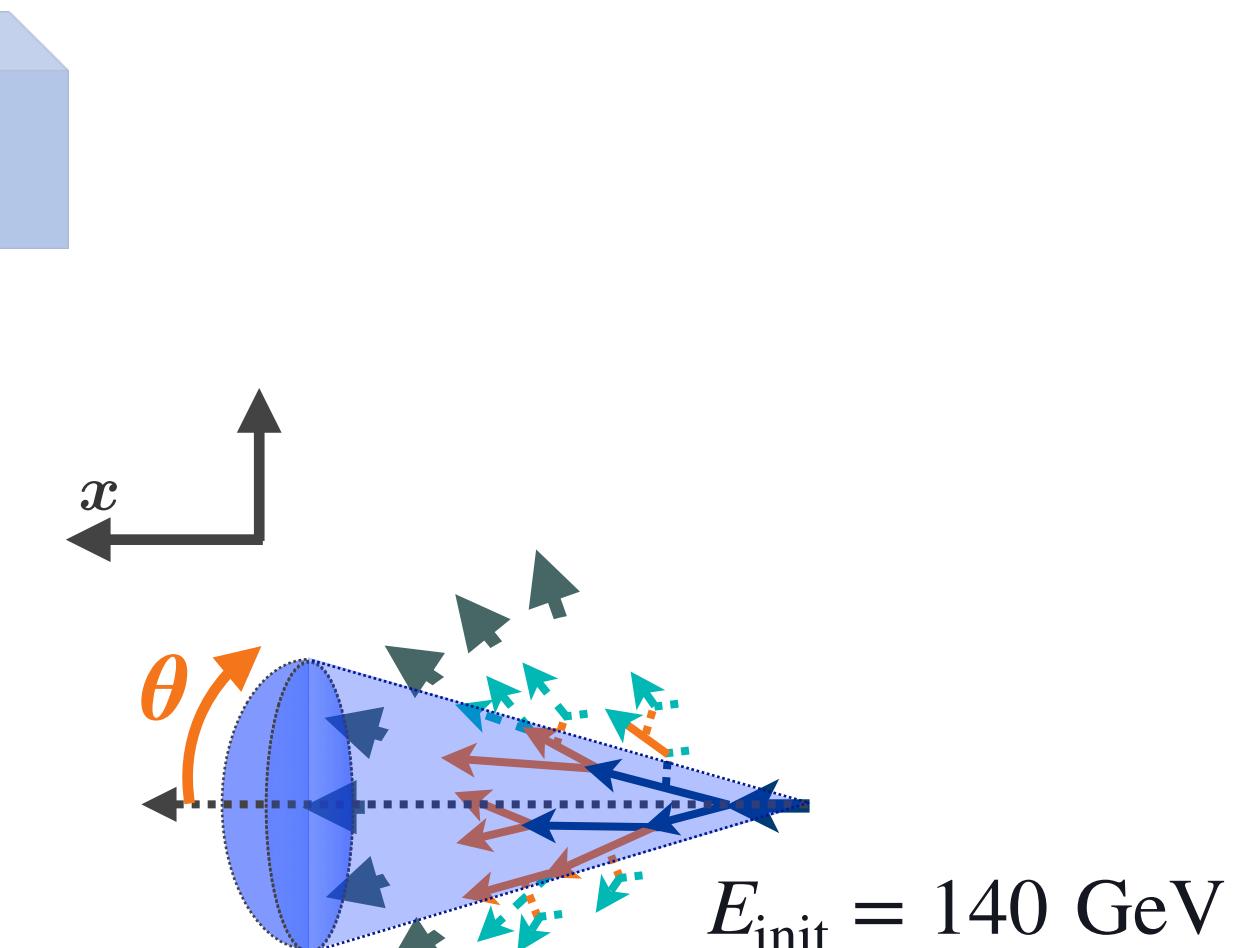
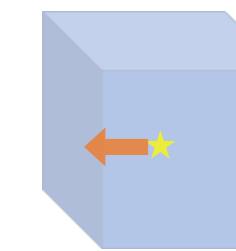
- Jet energy, momentum and mass

$$P^\mu(\theta) = \int_0^\theta d\theta' \frac{dP^\mu}{d\theta'}, \quad M^2(\theta) = P^\mu(\theta)P_\mu(\theta)$$

- Detailed substructure

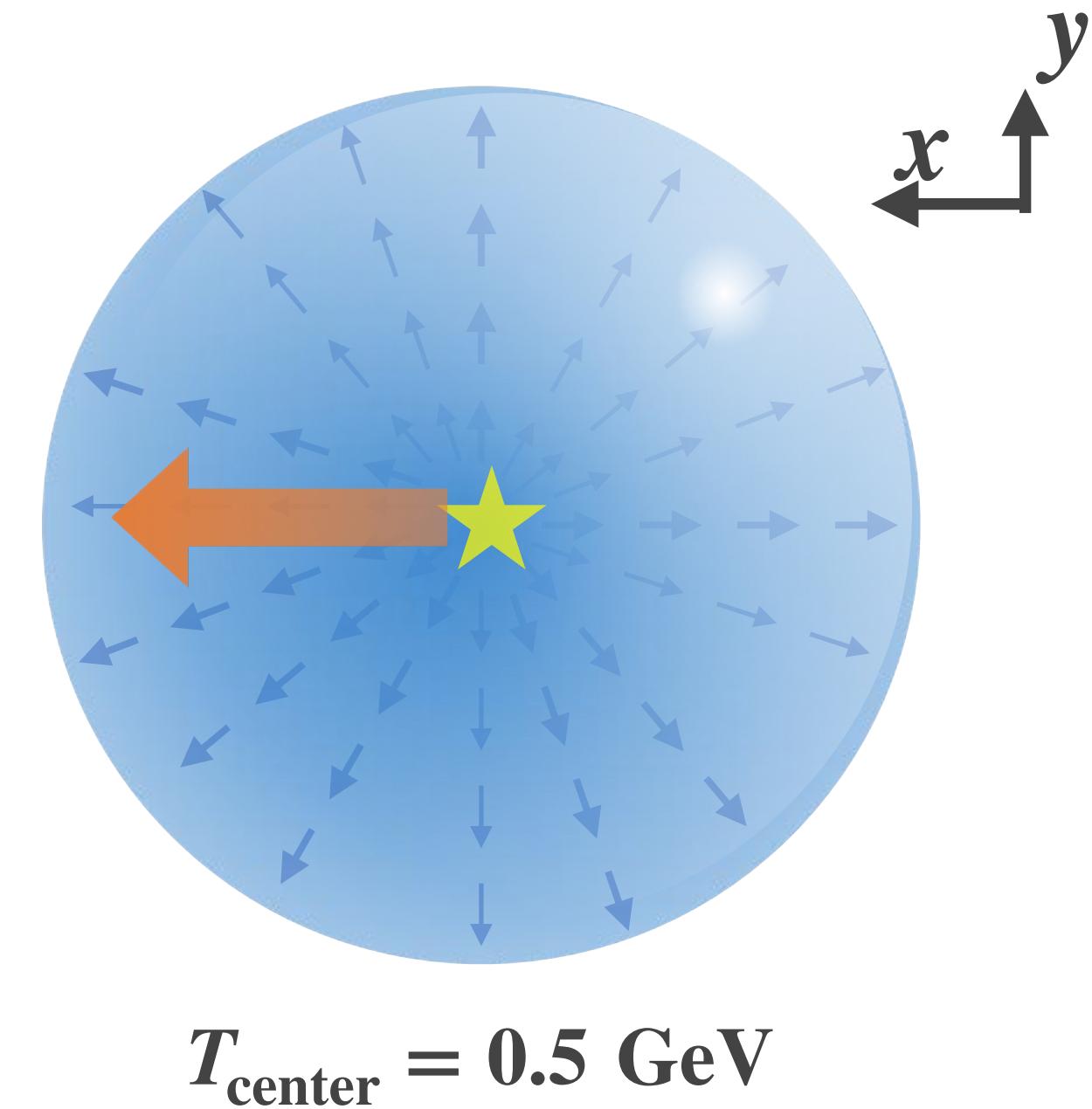
$$\rho_E(\theta) = \frac{1}{E(\theta=1)} \frac{dE}{d\theta}, \quad \rho_{P_x}(\theta) = \frac{1}{P_x(\theta=1)} \frac{dP_x}{d\theta}$$

- Backward suppression due to particilization (Recoil+Hydro)
- Backward suppression due to holes (Recoil)



# Recoil vs Recoil+Hydro response: Expanding medium case

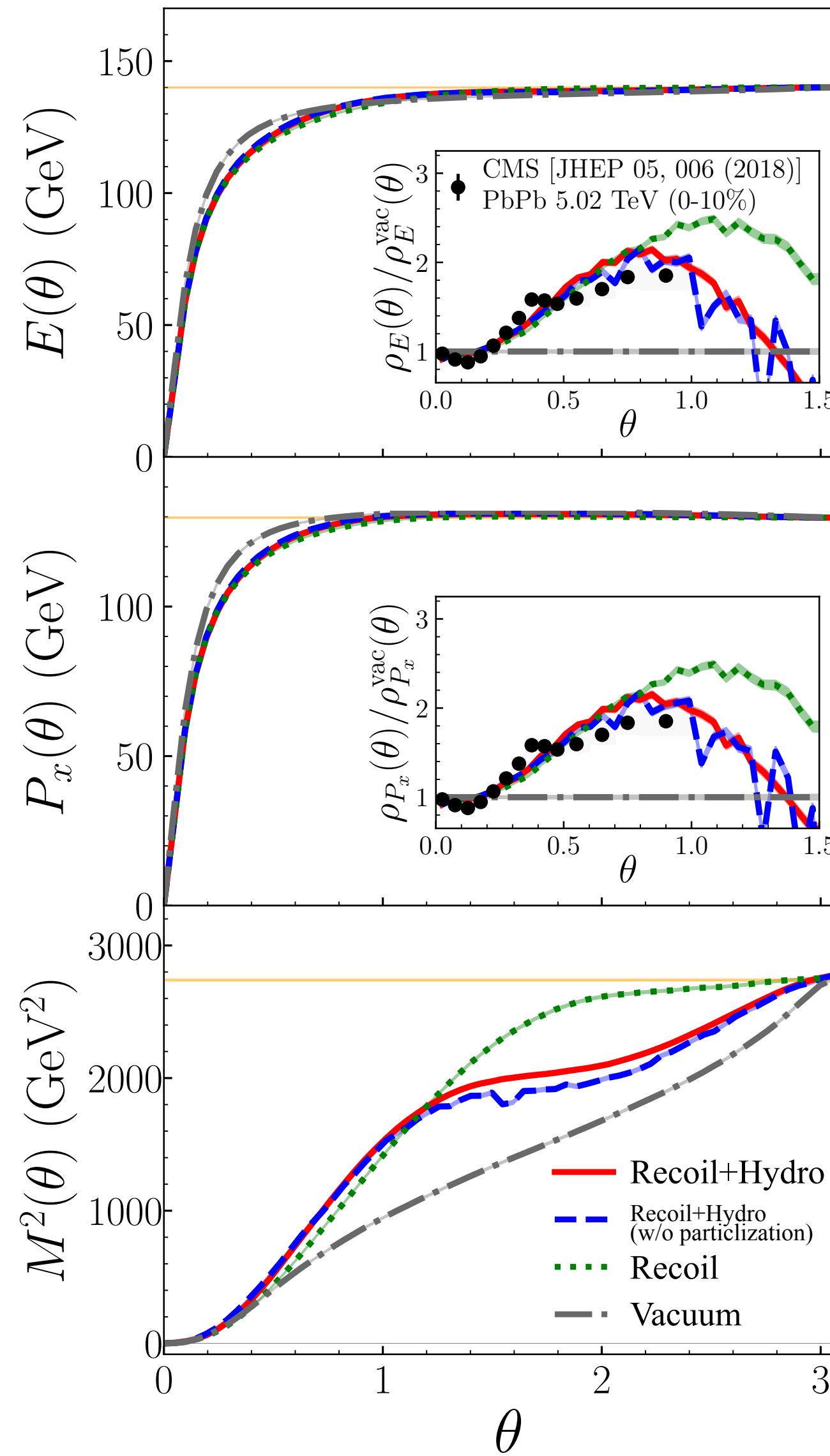
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- Jet propagation in medium with oblate 3-D Gaussian ( $\sigma_T = 1.5 \text{ fm}$ ,  $\sigma_z = 0.75 \text{ fm}$ )
- Medium size is chosen to reproduce the full simulation results
- Radial flow following the jet propagation

# Recoil vs Recoil+Hydro response: Expanding medium case

YT, C. Shen and A. Majumder, arXiv:2001.08321



- Angular structure of jet in oblate medium

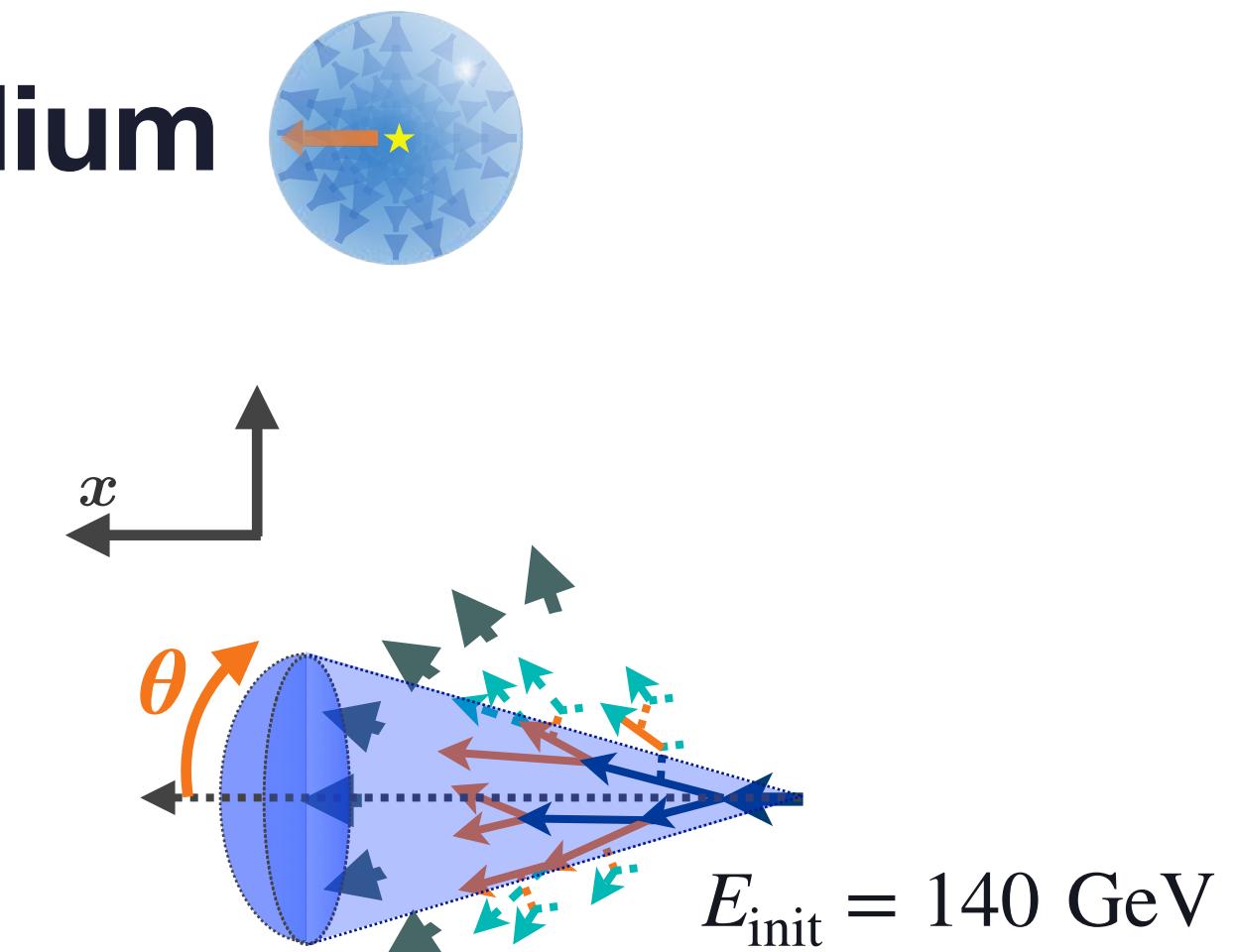
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$$P^\mu(\theta) = \int_0^\theta d\theta' \frac{dP^\mu}{d\theta'}, \quad M^2(\theta) = P^\mu(\theta)P_\mu(\theta)$$

- Detailed substructure

$$\rho_E(\theta) = \frac{1}{E(\theta=1)} \frac{dE}{d\theta}, \quad \rho_{P_x}(\theta) = \frac{1}{P_x(\theta=1)} \frac{dP_x}{d\theta}$$

- Collimation due to push by the radial flow
- Small effect of particlization (**Recoil+Hydro**)
- Clear difference at very large angle region ( $\theta > 1$ )



# Summary

## ● Jet evolution in JETSCAPE

- Multi-stage description by switching modules with virtuality
- Further extension by  $Q^2$ -dependence in jet quenching parameter  $\hat{q}$
- Simultaneous description of jet and high- $p_T$  particle energy loss in various  $\sqrt{s_{\text{NN}}}$
- Further systematic studies for jet substructure

## ● Hydrodynamic medium response

- Transport of thermalized jet energy and momentum
- Described by hydrodynamic equation with source terms
- Difference from recoils led by background flow

# Backup

# Causal Formulation for Source Term

YT, C. Shen and A. Majumder, arXiv:2001.08321

