

# Experimental study of asymmetric nuclear matter EOS from heavy-ion reactions with RIBF-SPIRIT

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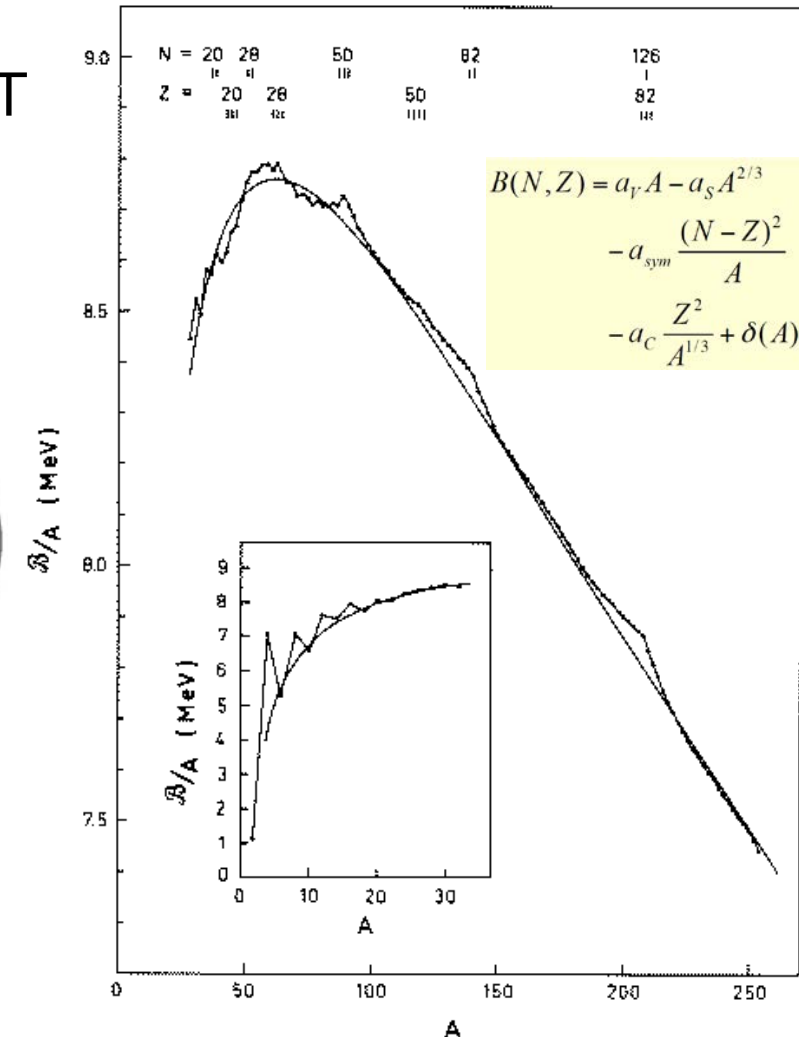
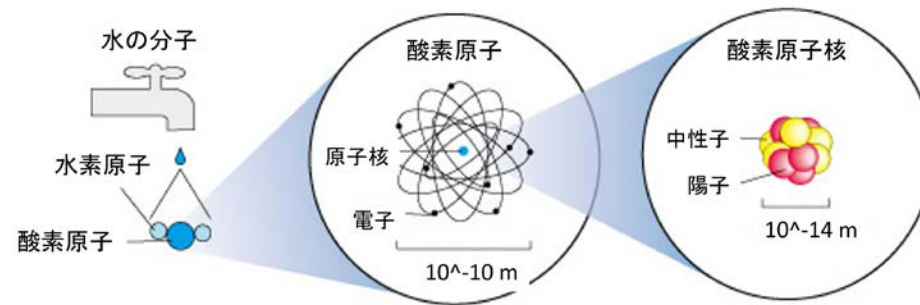
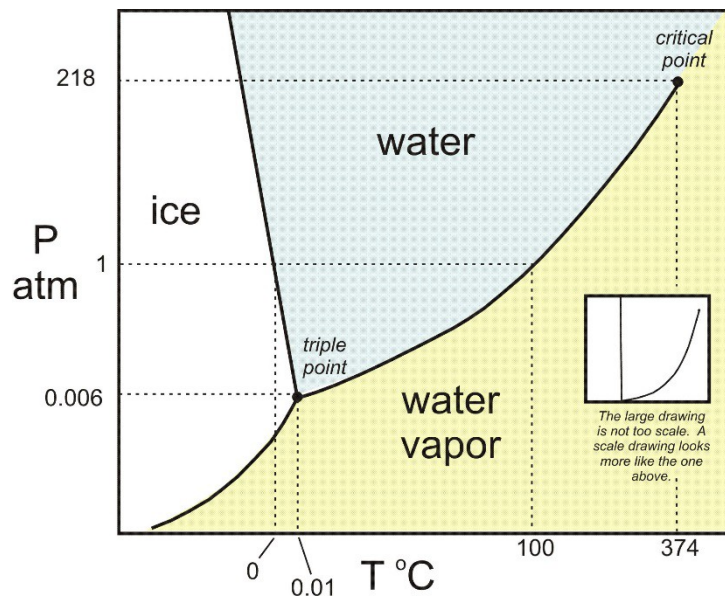
Workshop at the Tomonaga Center for the History of the Universe (TCHoU)

March 29, 2024

# Nuclear matter : many body system of nucleon

Bohr & Mottelson  
Nuclear Structure Vol.1

- Equation of State describes the relationship of thermodynamical quantity  $\leftrightarrow$  EoS of ideal gas:  $PV=nRT$
- Phase of diagram because of interaction between the molecules.



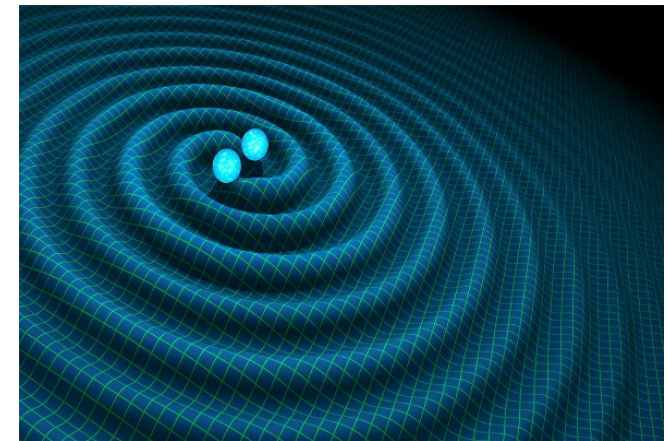
- Nuclear liquid drop model
- 1<sup>st</sup> order description of nuclear mass is succeeded. (Bethe-Weizsäcker Mass formula)

# Asymmetric nuclear matter EOS: Symmetry Energy term of nuclear EOS

- Equation of state of nuclear matter can be reconstructed by using the differential thermodynamic identity:

$$E(T, \rho, \delta) = E(T, \rho, \delta = 0) + E_{sym}(T, \rho) \delta^2 + O(\delta^4)$$
$$\delta = \frac{(\rho_n - \rho_p)}{\rho}$$

- The asymmetric term of nuclear EOS depends on  $\delta$
- Important term especially for astrophysics
  - Neutron star structure ( $T \sim 0$ )
    - Solar mass star with the radius of  $\sim 10$ km.
  - Supernovae process ( $T \sim O(10)$  MeV)
  - Neutron star merger/Gravitational wave

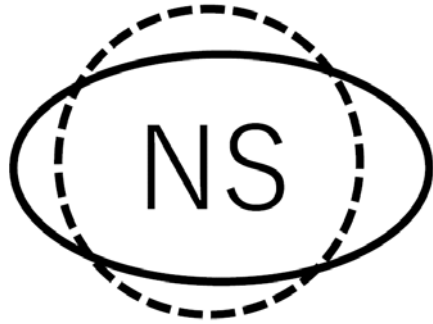


Visualization of a NS merger and the gravitational waves

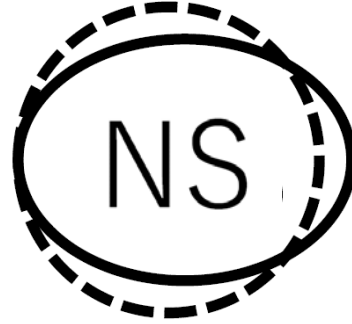
# Gravitational wave from neutron star merger

## Tidal deformation depends on nuclear EoS

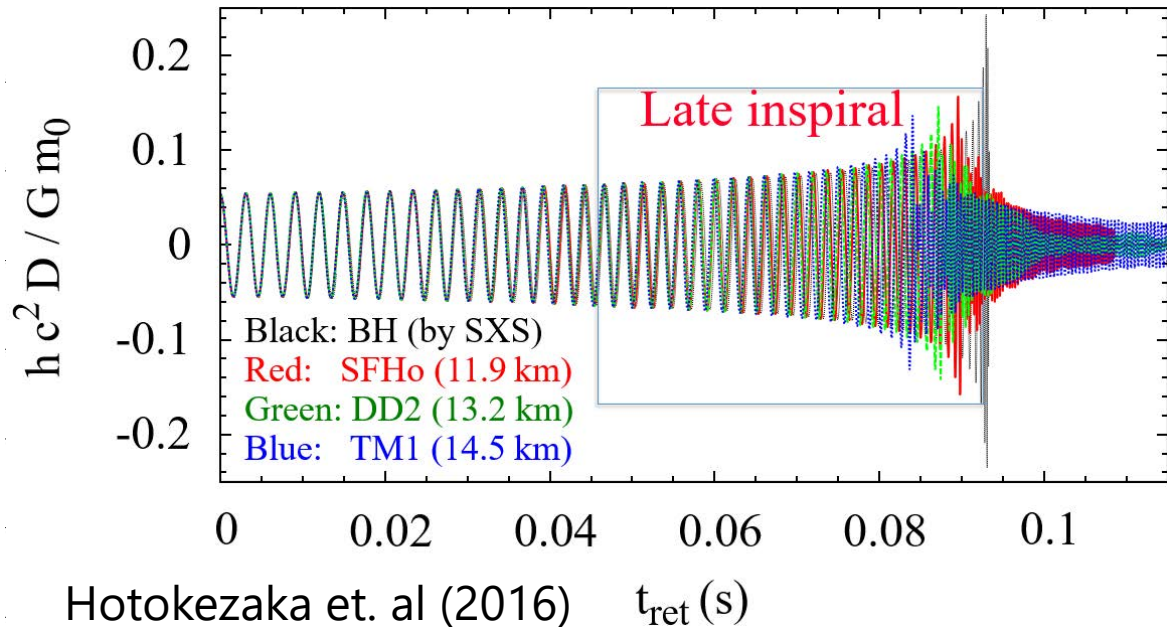
A. Bauswein, S. Goriely, and H.-T. Janka  
 APJ, 773, 21 (2013)



Soft → Easy to be deformed



Stiff → Small deformation



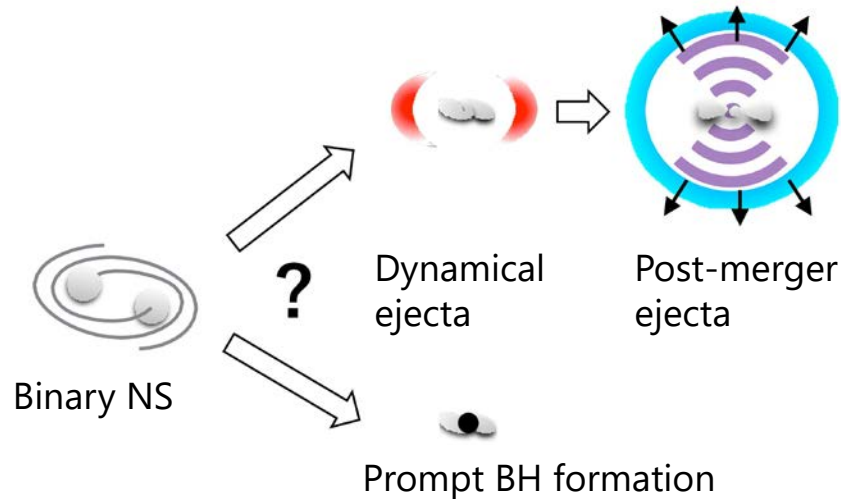
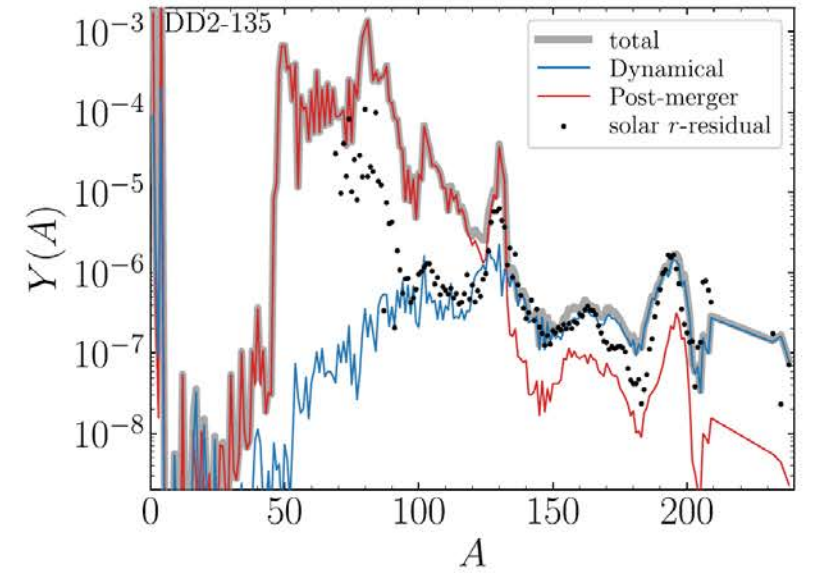
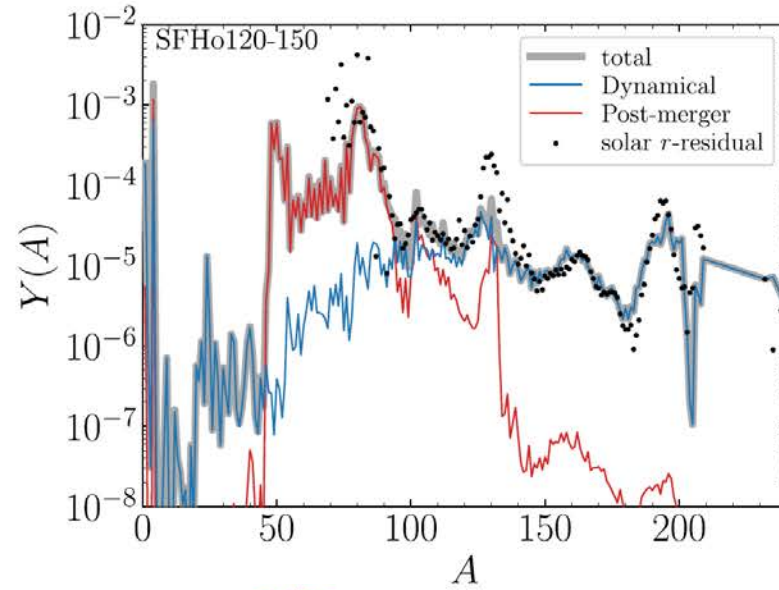
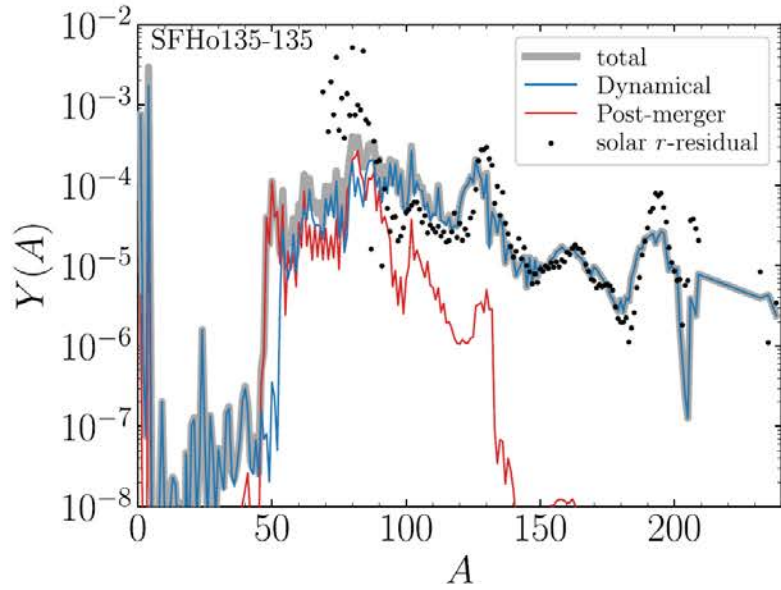
$$\Lambda = \frac{2}{3} k_2 \left( \frac{c^2 R}{GM} \right)^5 = \frac{64}{3} k_2 \left( \frac{R}{R_s} \right)^5$$

$\Lambda < 800$  (90% confidence)

GW170817 PRL 119 161101

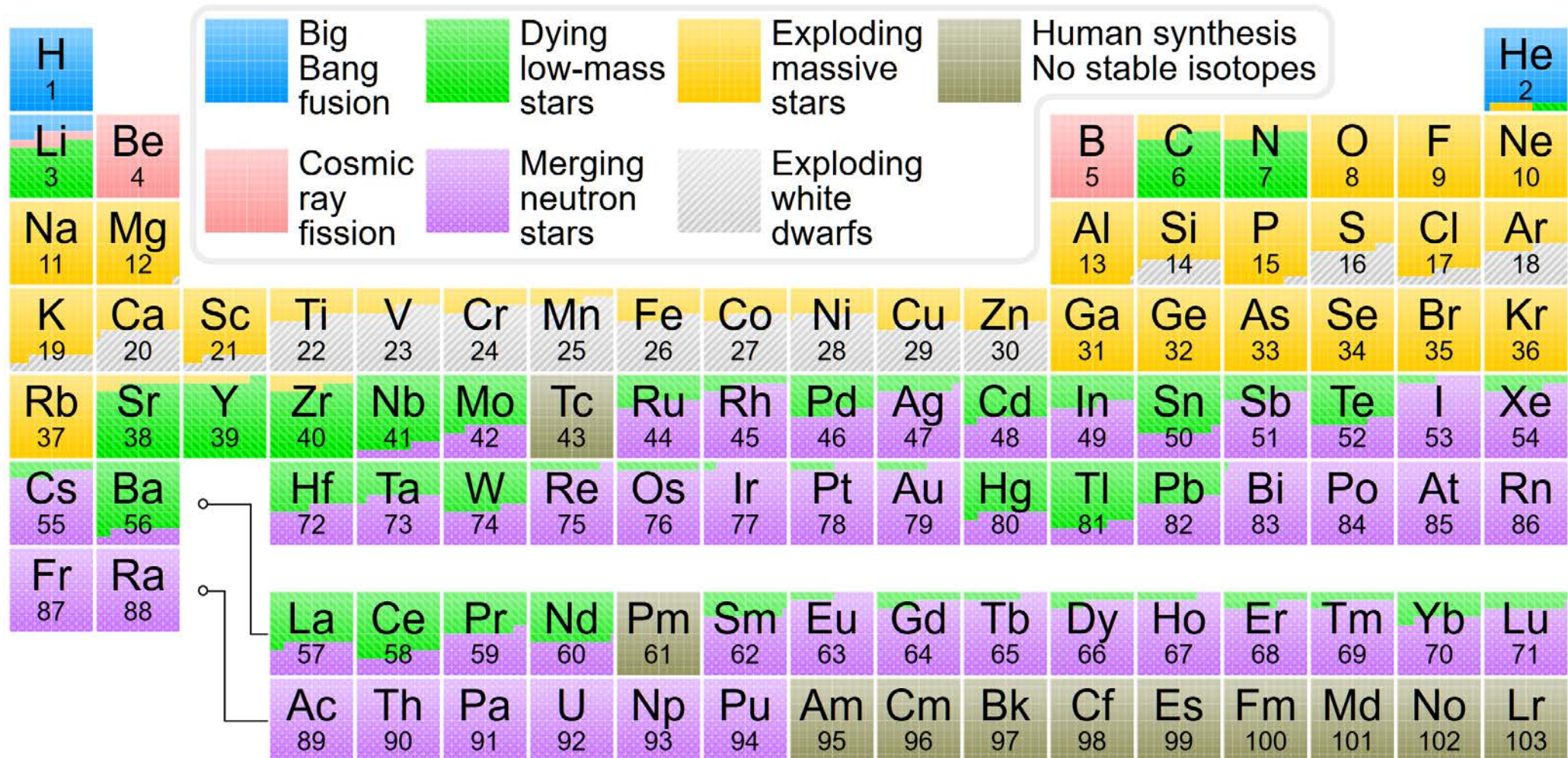


# Nuclear EoS is important also for the r-process nuclear synthesis in neutron star merger



Fujibayashi APJ 2023

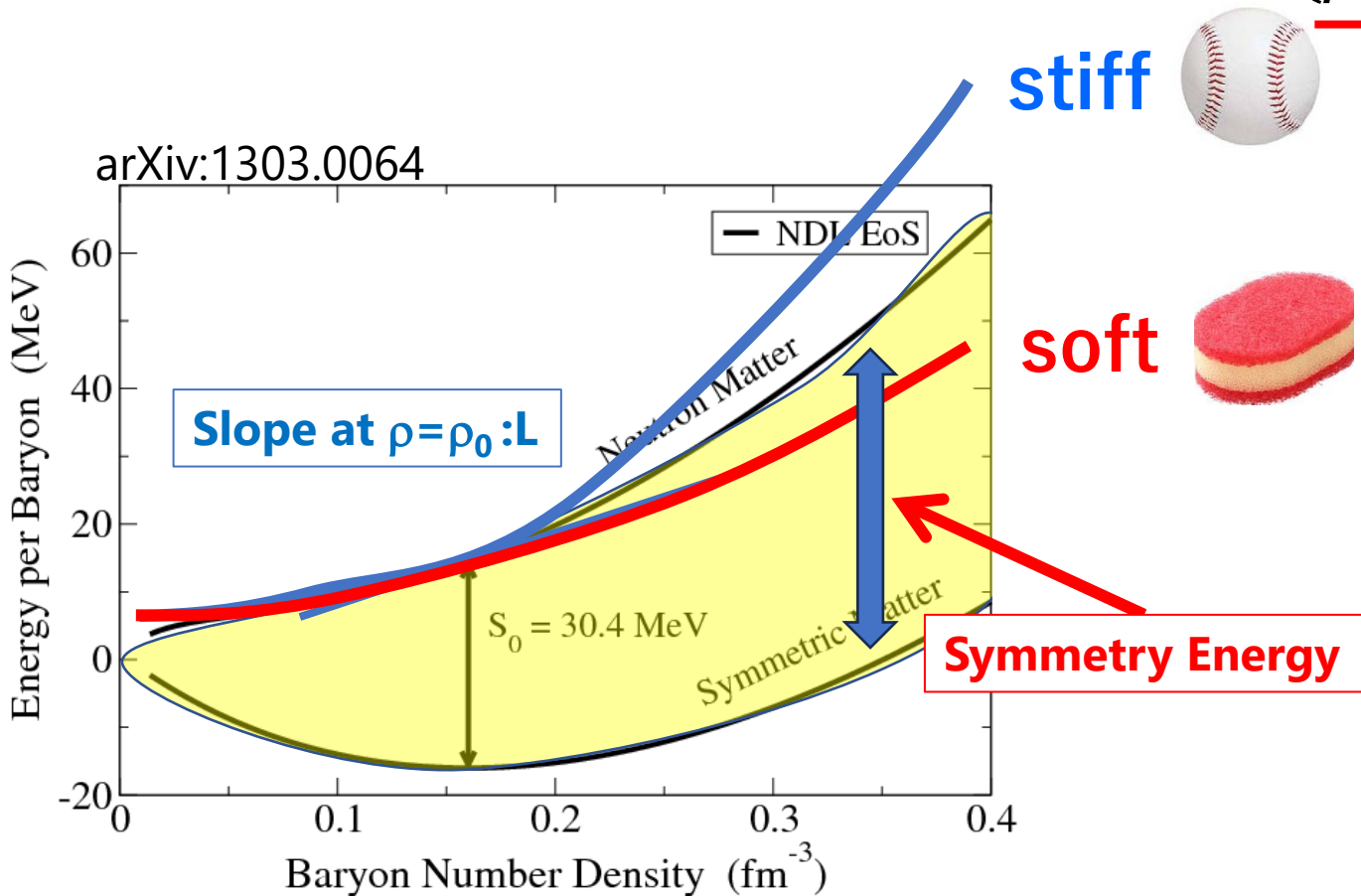
# Nuclear EoS is important also for the r-process nuclear synthesis in neutron star merger



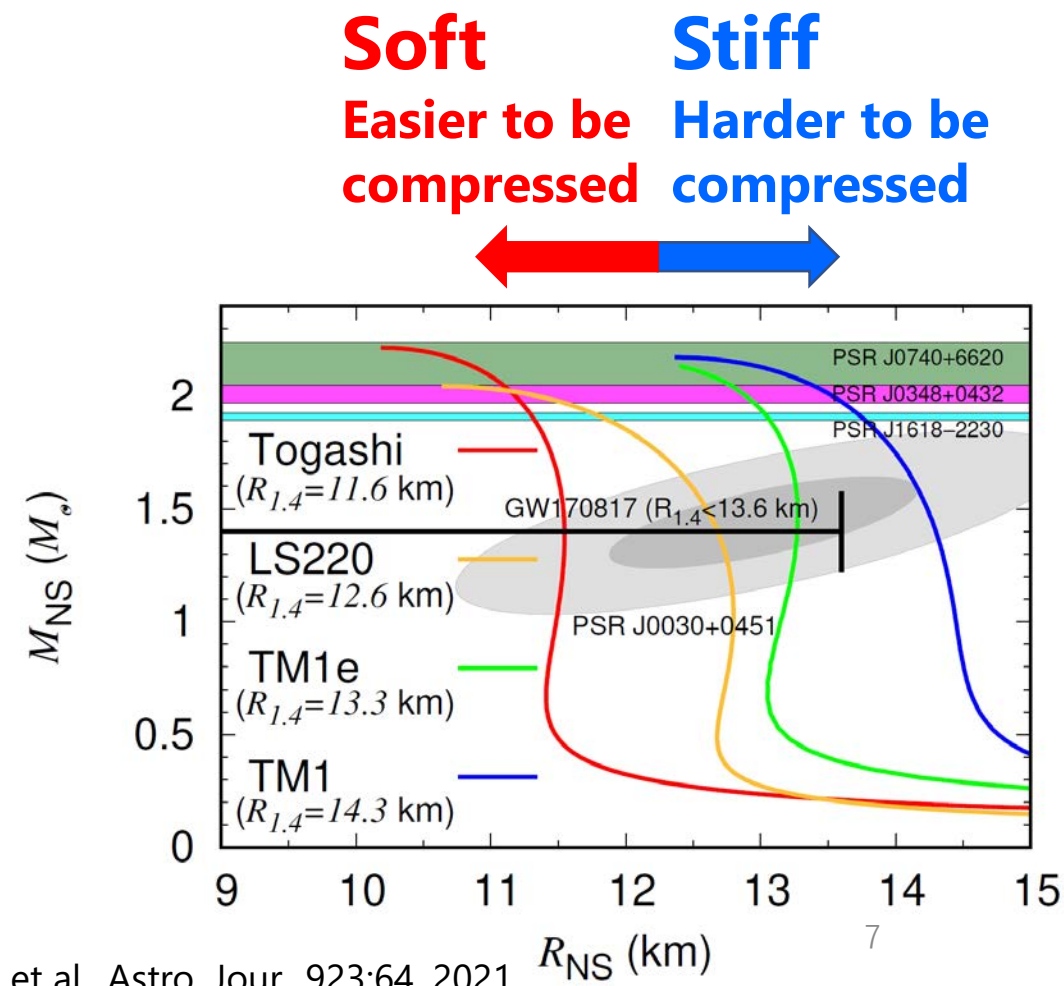
# Asymmetric nuclear matter EOS: Symmetry Energy term of nuclear EOS

$$E(T, \rho, \delta) = E(T, \rho, \delta = 0) + E_{sym}(T, \rho) \delta^2 + O(\delta^4)$$

$$\delta = (\rho_n - \rho_p) / \rho$$

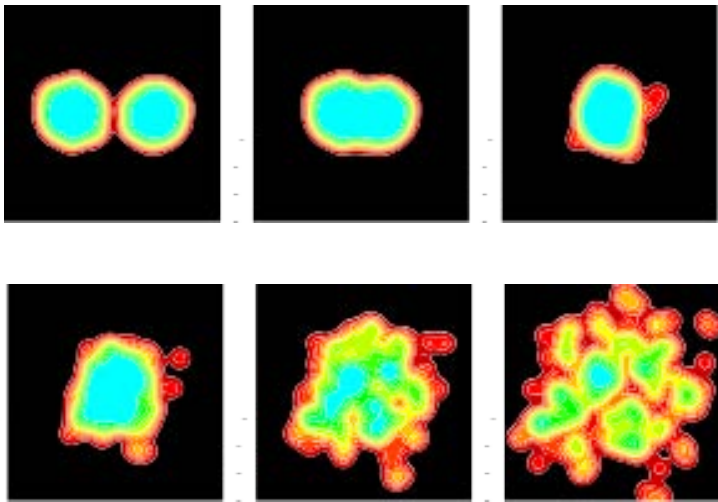


Parameter L is often referred to compare the SE as it can be obtained both from Astrophysics and nuclear physics.

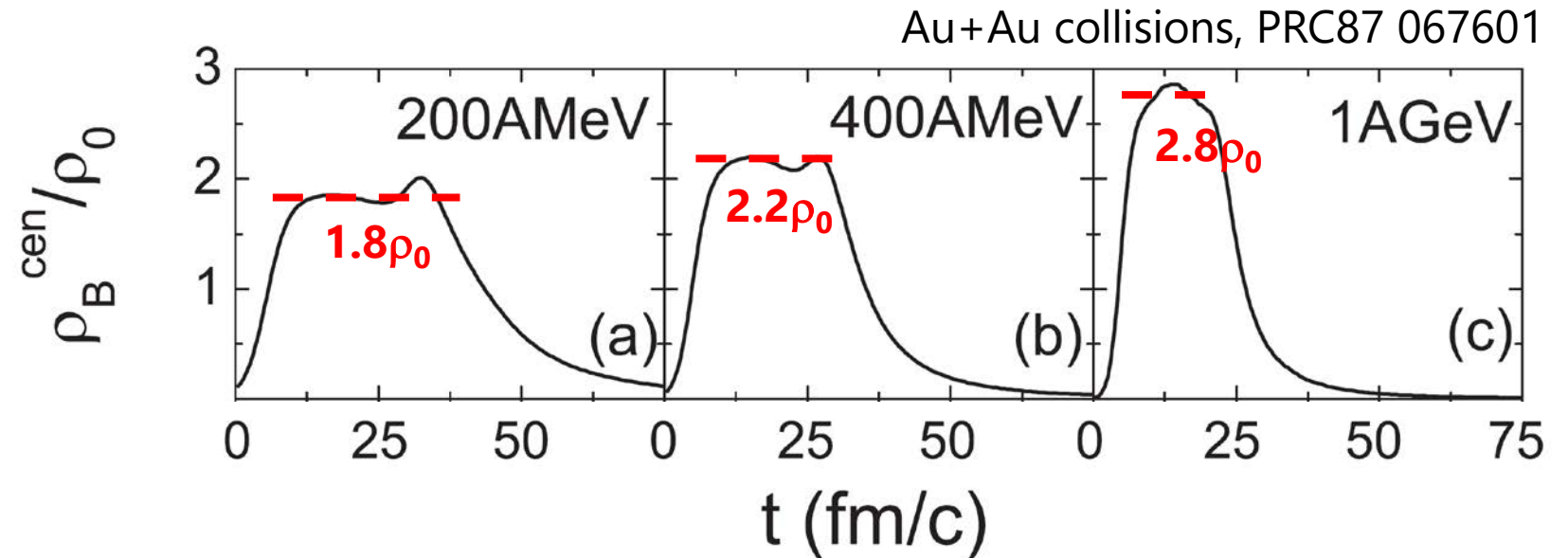


# Terrestrial experimental study of high dense matter nuclear symmetry energy → Heavy Ion Collision (HIC)

Sn+Sn @300MeV/u



Central density as a function of time.

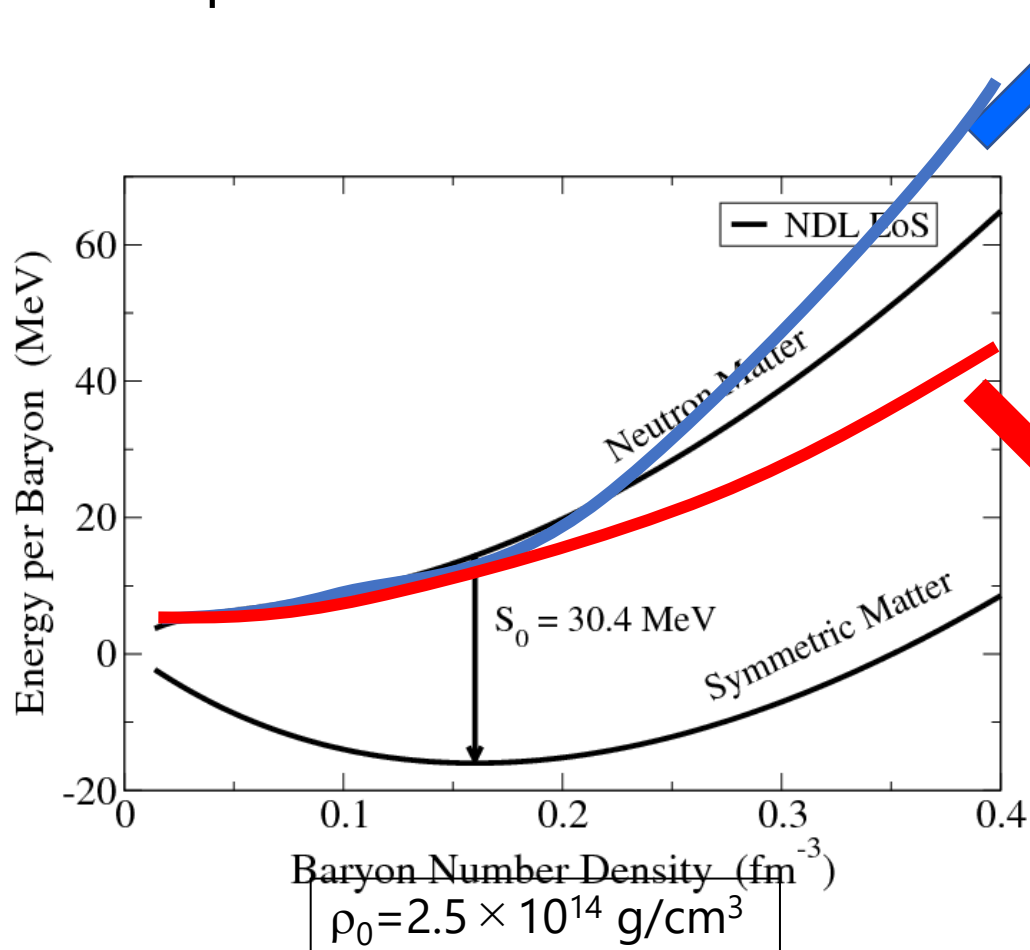


- Unique way to realize high dense matter in laboratory.
- Quite challenging to extract the information of high dense matter symmetry energy since we need the help of transport model.
  - Mixture of equilibrium and non-equilibrium state.



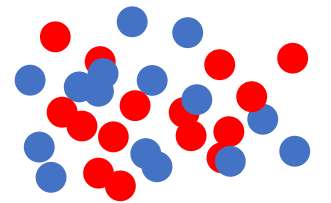
# Experimental observables from heavy ion collision to constrain the symmetry energy

- No direct observables, but contains the information of symmetry energy
- Symmetry energy  $\rightarrow$  appeared as pressure difference between neutron and proton



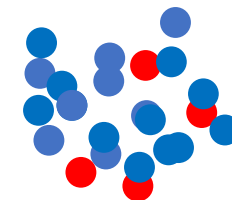
## Stiff symmetry energy (large L)

- $\rightarrow$  lower  $\rho_n/\rho_p$  in higher dense region
- $\rightarrow$  lower n/p in high  $\rho$



## Soft symmetry energy (small L)

- $\rightarrow$  larger  $\rho_n/\rho_p$  in higher dense region
- $\rightarrow$  larger n/p in high  $\rho$



# Experimental observables from heavy ion collision to constrain the symmetry energy

- No direct observables, but contains the information of symmetry energy
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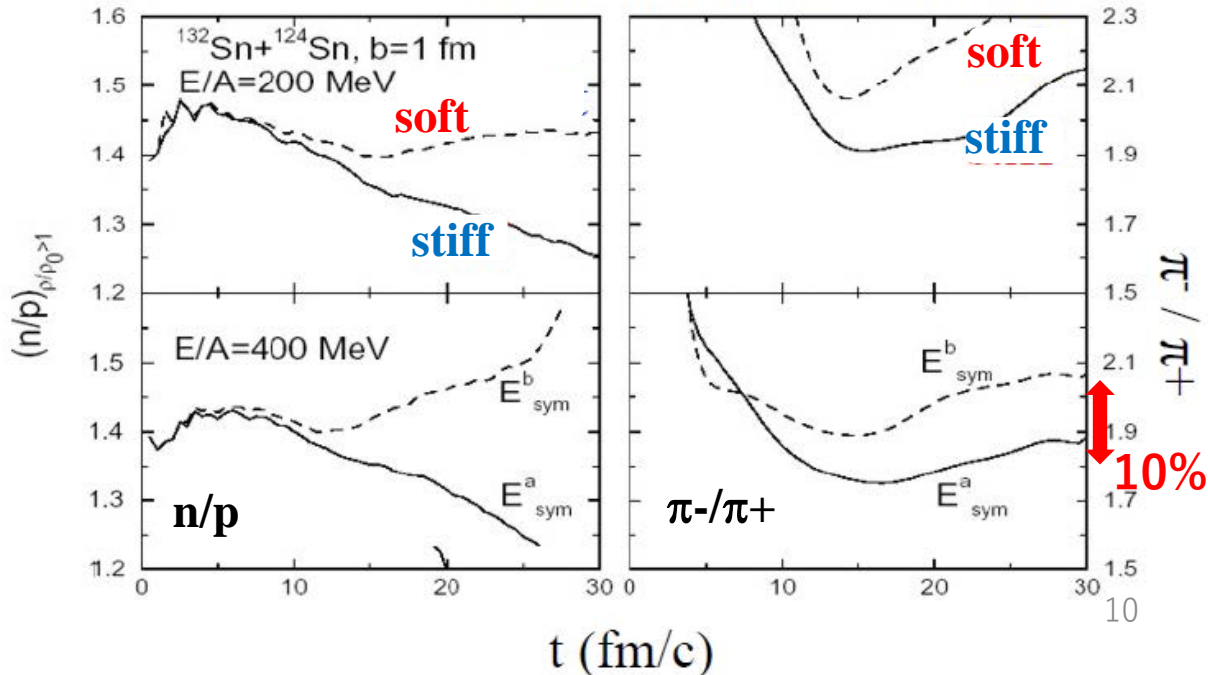
$\pi^-$  production (main reaction)



$\pi^+$  production (main)

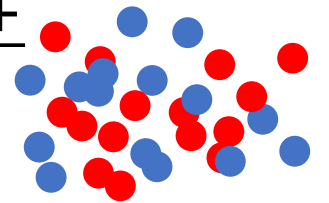


Li et al., Nucl.Phys. A734 (2004) 593.



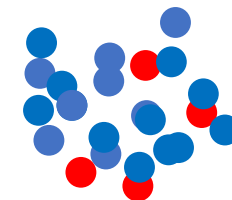
## Stiff symmetry energy (large L)

- $\rightarrow$  lower  $\rho_n/\rho_p$  in higher dense region
- $\rightarrow$  lower  $n/p$ , lower  $\pi^-/\pi^+$



## Soft symmetry energy (small L)

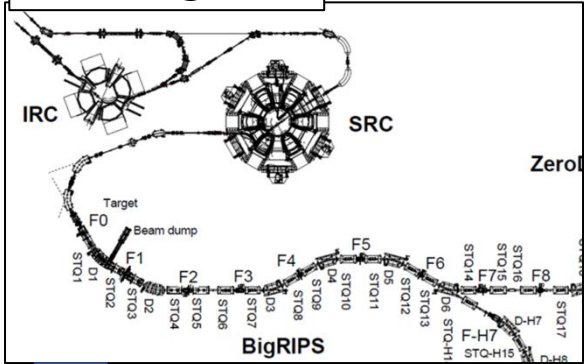
- $\rightarrow$  larger  $\rho_n/\rho_p$  in higher dense region
- $\rightarrow$  larger  $n/p$ , higher  $\pi^-/\pi^+$



# SPIRIT experiment: neutron rich Sn+Sn collision beam line+TPC+trigger+neutron detector



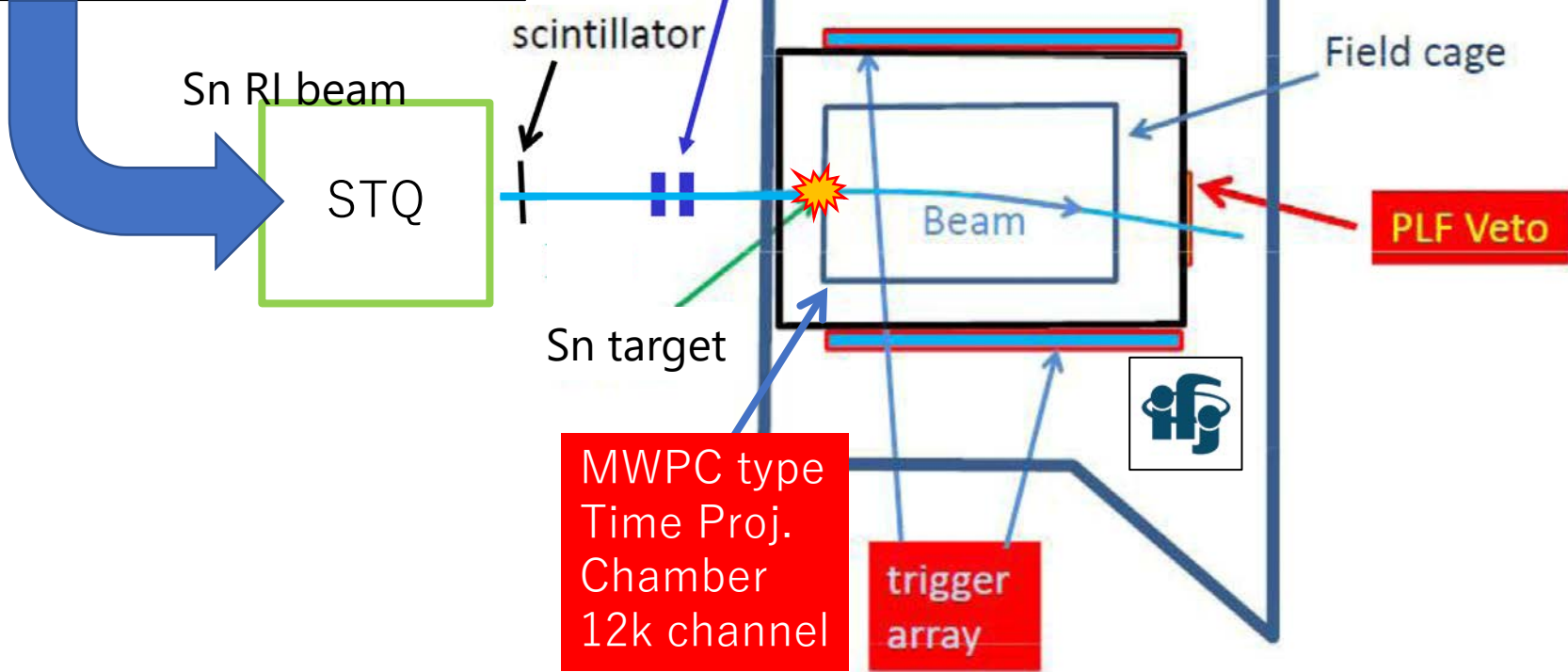
RIBF-BigRIPS Making neutron rich beam



Chamber in SAMURAI magnet  $B=0.5T$

Beam Tracker

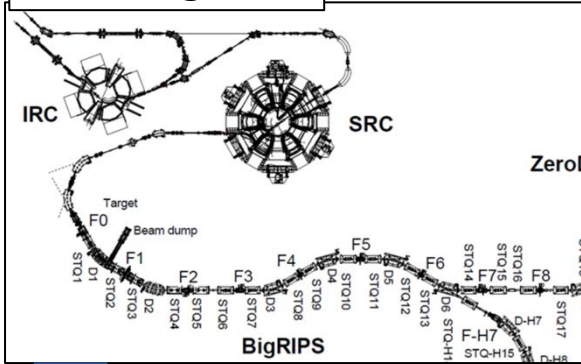
Neutron detector  
NeuLAND



# SPIRIT experiment: neutron rich Sn+Sn collision beam line+TPC+trigger+neutron detector



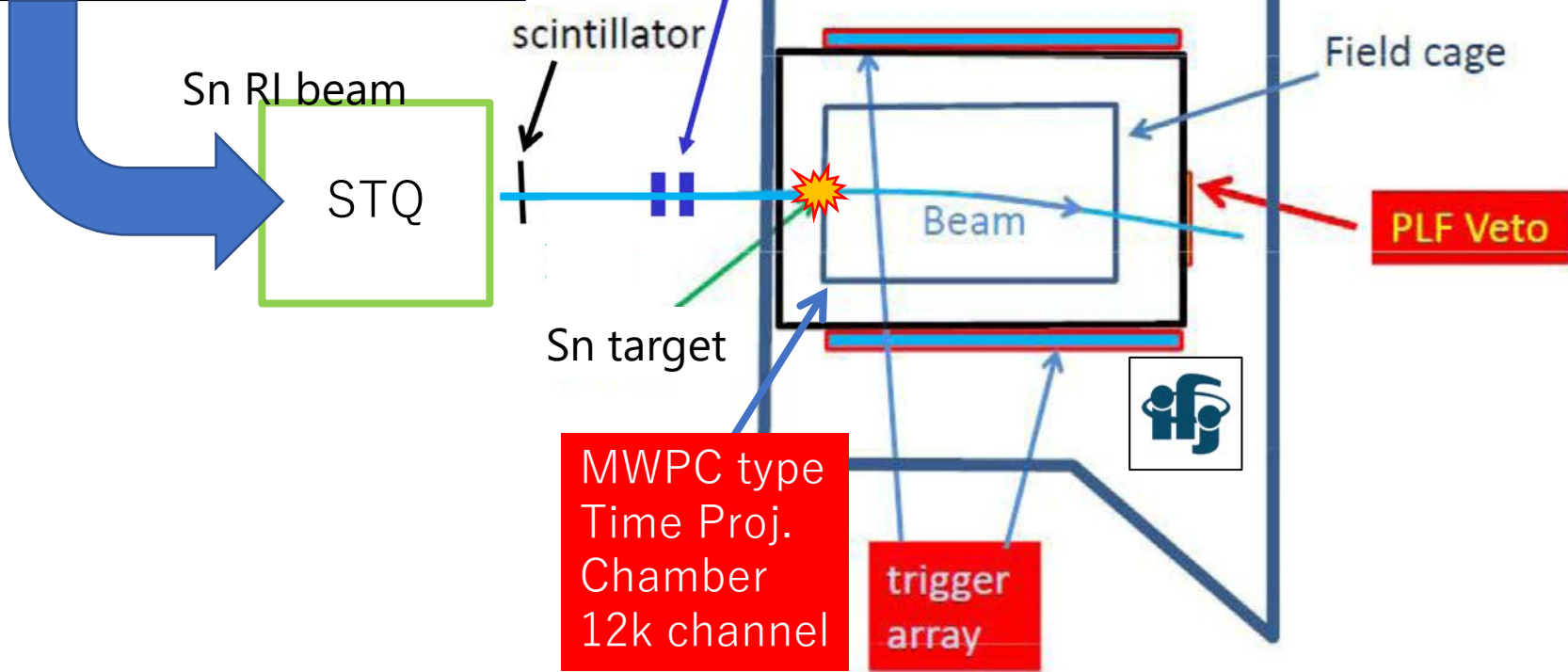
RIBF-BigRIPS Making neutron rich beam



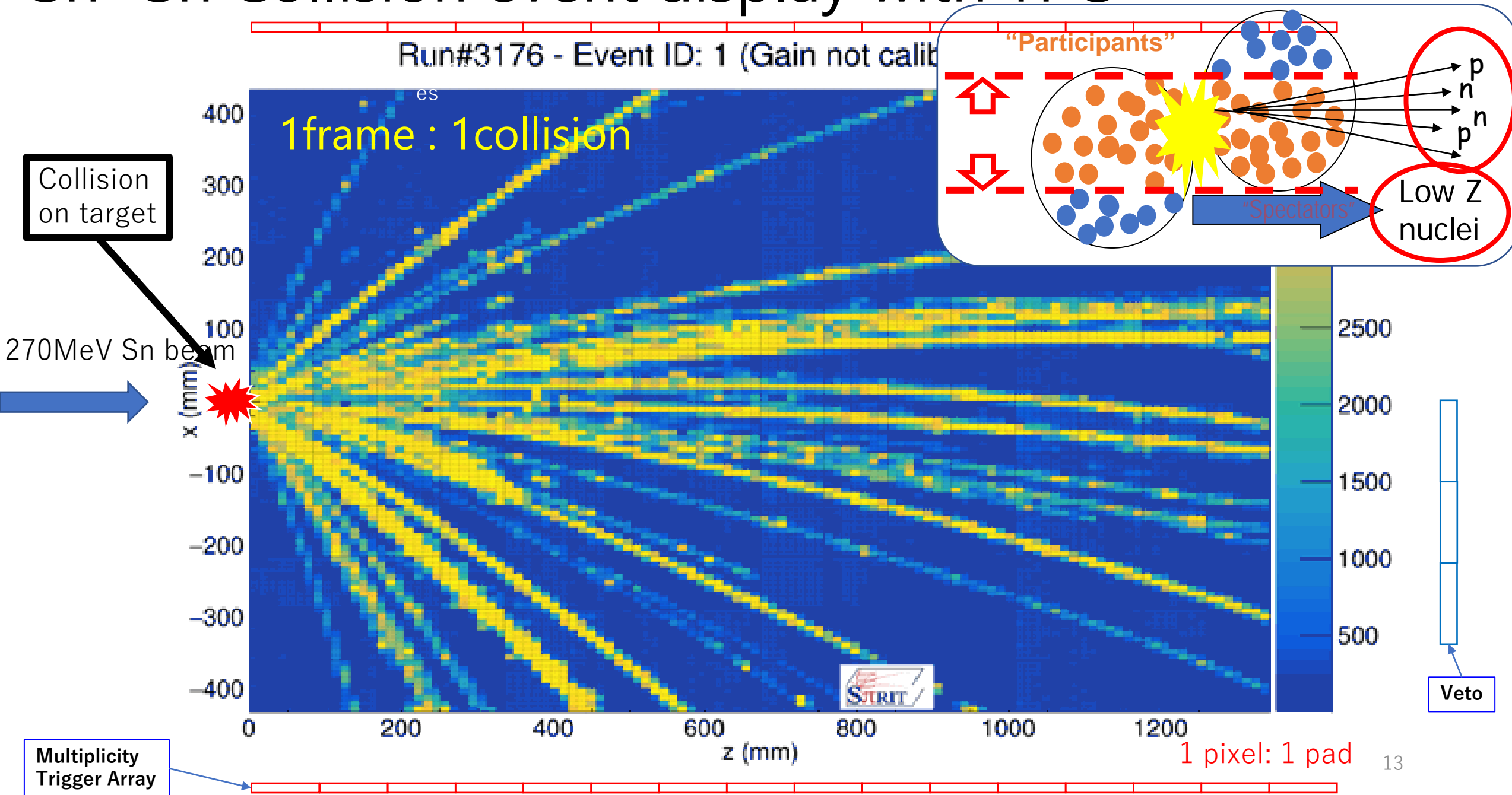
Chamber in SAMURAI magnet B=0.5T

Beam Tracker

Neutron Neutron detector  
5 sec./frame. Movie for ~2.5 hour.



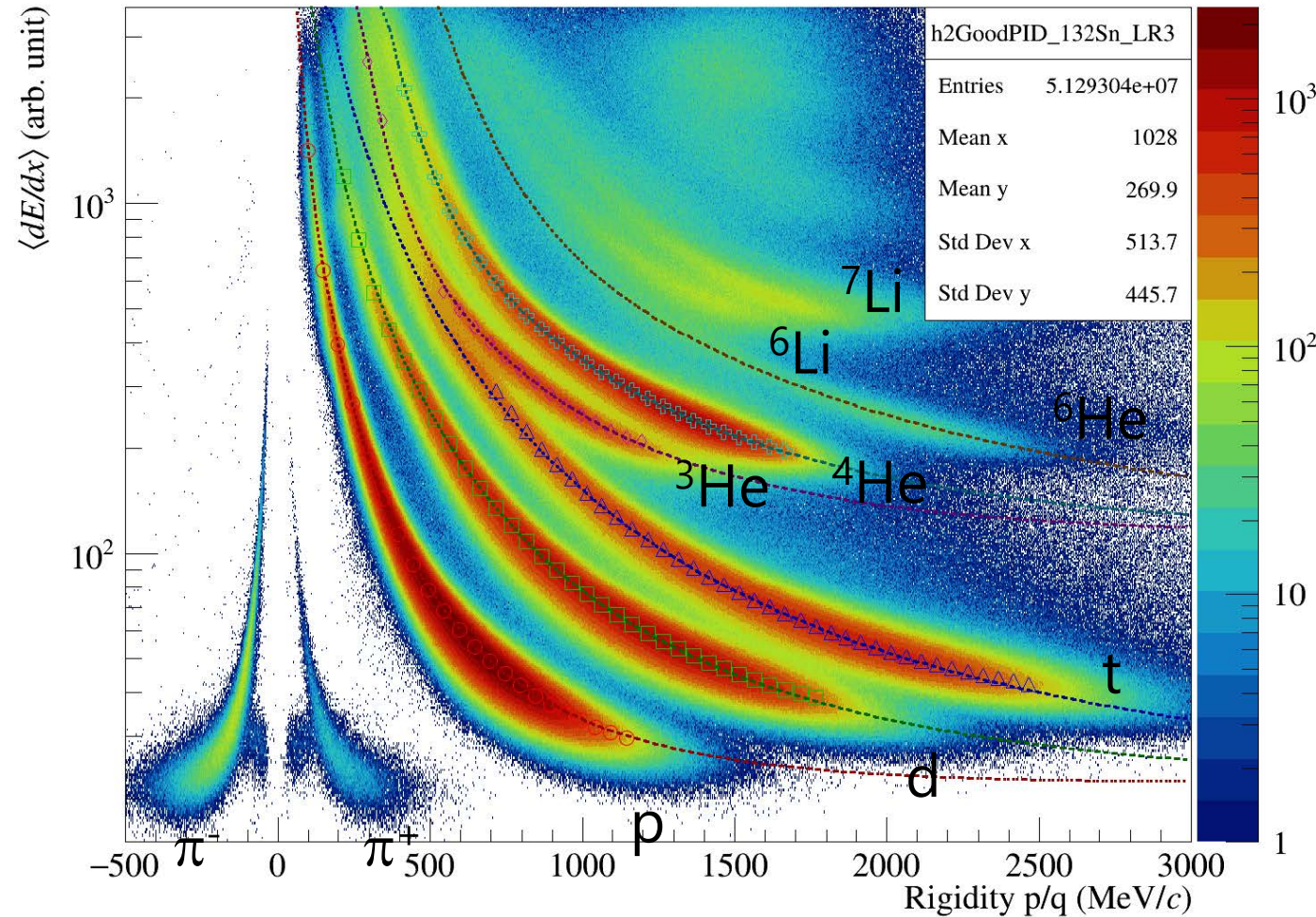
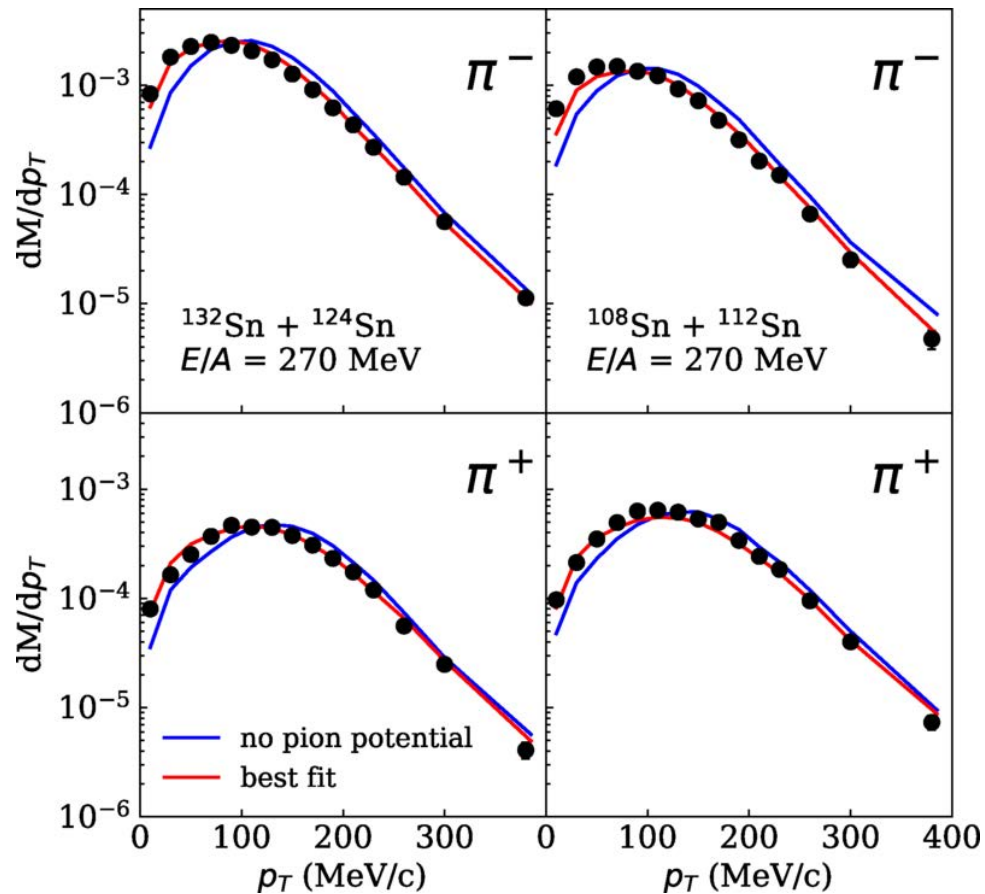
# Sn+Sn Collision event display with TPC



# Charged particle measurement with Time Projection Chamber

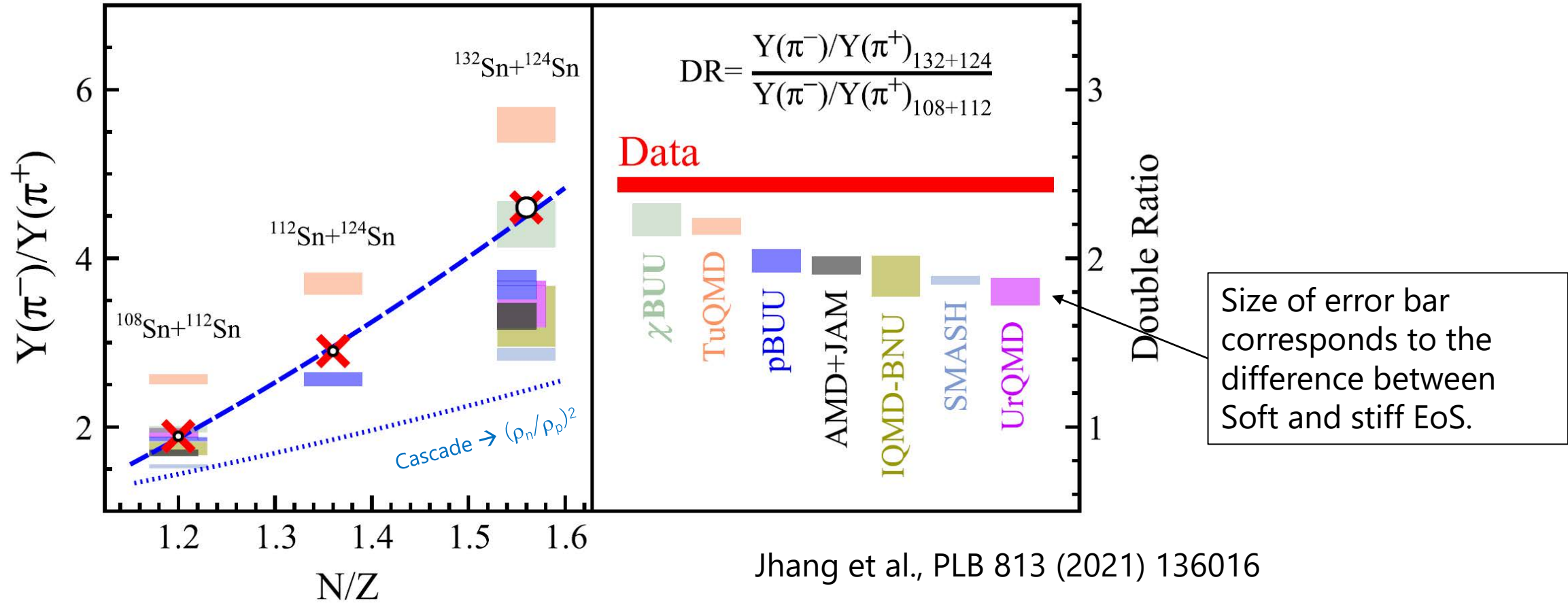
Measure all of particles produced in a HIC  
 Particle ID based on rigidity- $dE/dx$  ( $dE/dx \propto Z^2$ )  
 Rigidity  $\rightarrow$  particle momentum

TPC ParticleID for  $^{132}\text{Sn}+^{124}\text{Sn}$



# Result on pion multiplicity: pion ratio

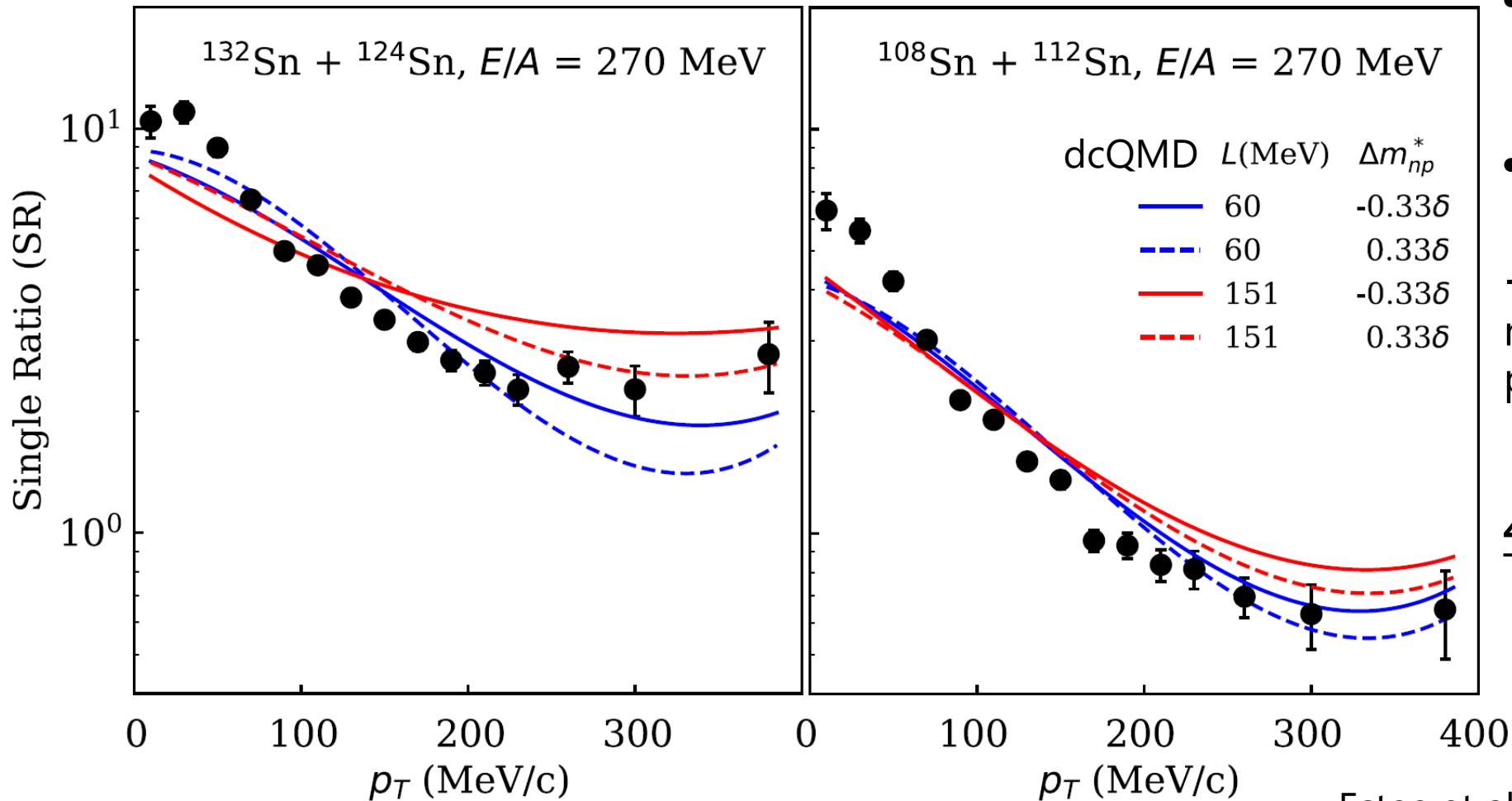
→ Large discrepancy among theoretical models



- Numerical calculation of HIC dynamics by using transport theory.
- Predictions with same EoS are supposed to be same → Larger discrepancy than experimental result.
- Different assumptions regarding the mean field potentials for  $\Delta$  baryons and pions can influence the pion multiplicities.

# High-momentum pion data: reduce the influence from the assumption for $\Delta$ /pion mean field potential

- Sensitivity to the isospin dependence of mean field dominates at high- $p_T$ .

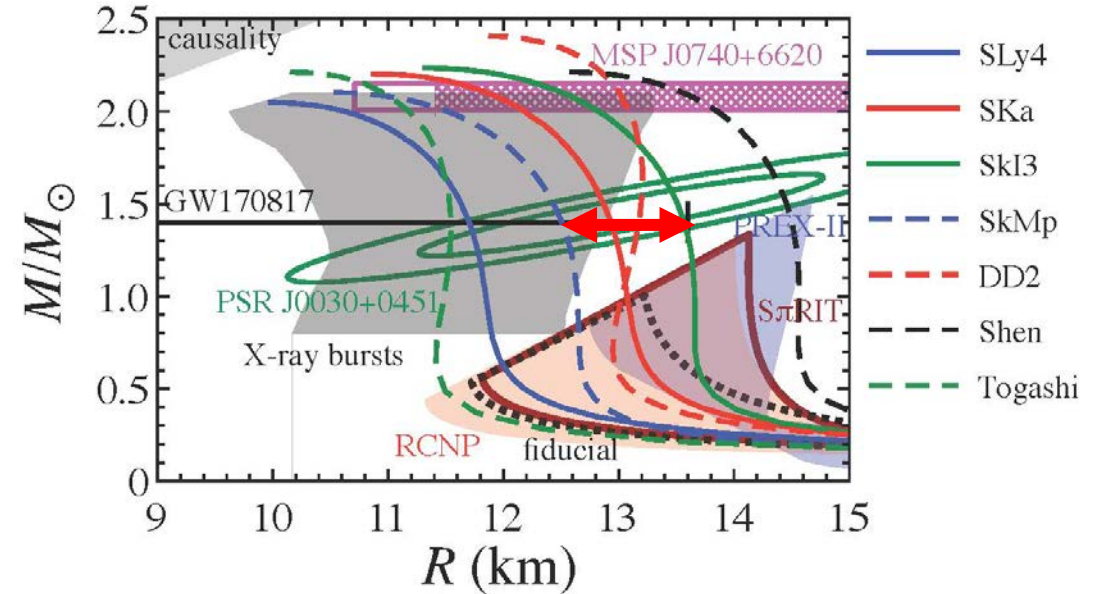
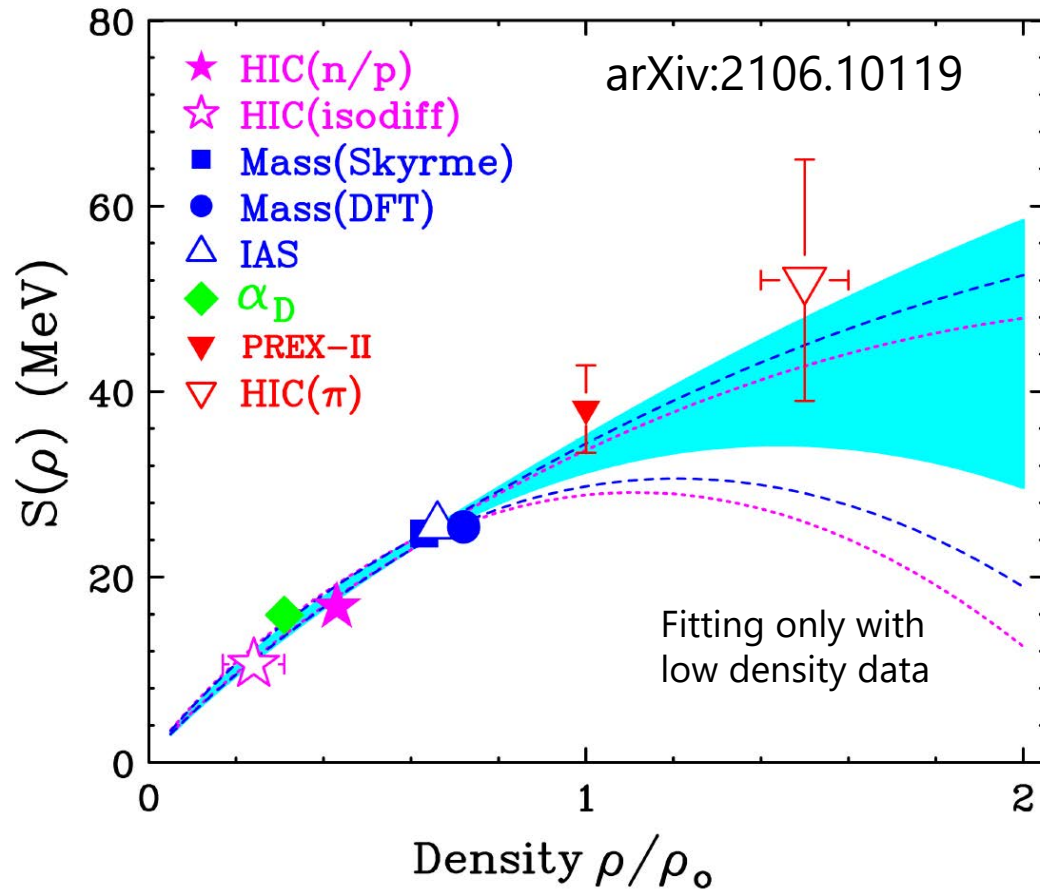


- Neutron rich system shows more sensitivity at high- $p_T$ .
- Calculation underestimate at low- $p_T$ .  
→ Coulomb effect and/or non-resonant pion production.

$$\underline{42 < L < 117}$$

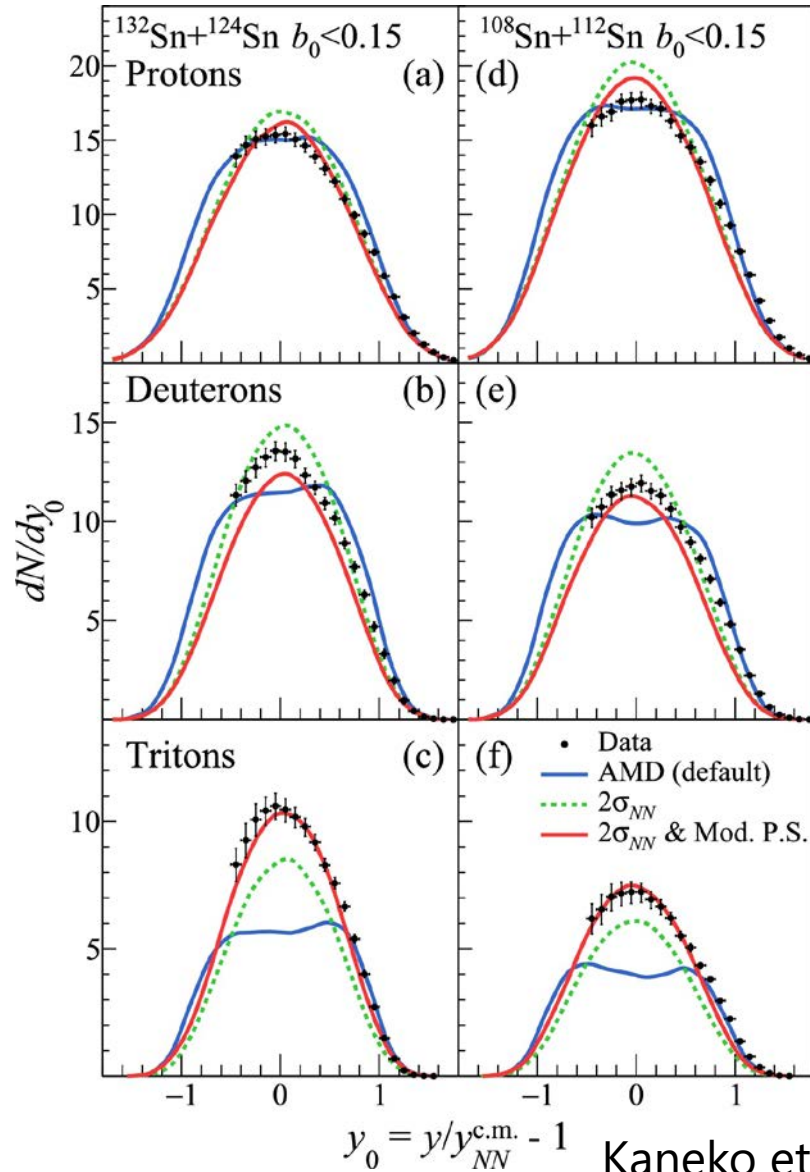


# Compilation of experimentally determined symmetry energy

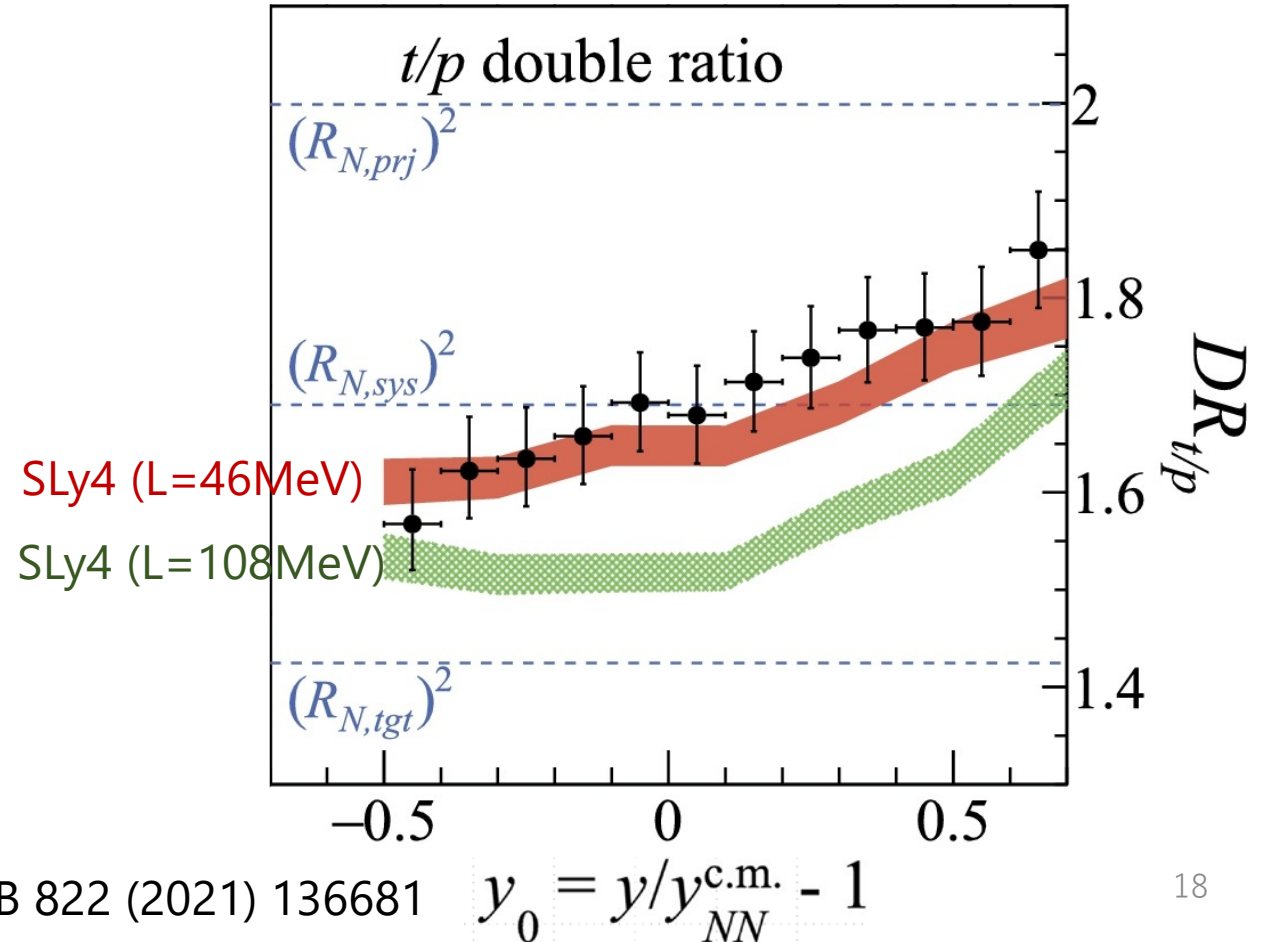


- Fitting with phenomenological formula:  $S_0 = (33.3 \pm 1.3)$  MeV,  $L = (59.6 \pm 22.1)$  MeV
  - suggests a radius for a 1.4 solar mass neutron star of  $13.1 \pm 0.6$  km

# Extra observable: p/d/t dN/dy

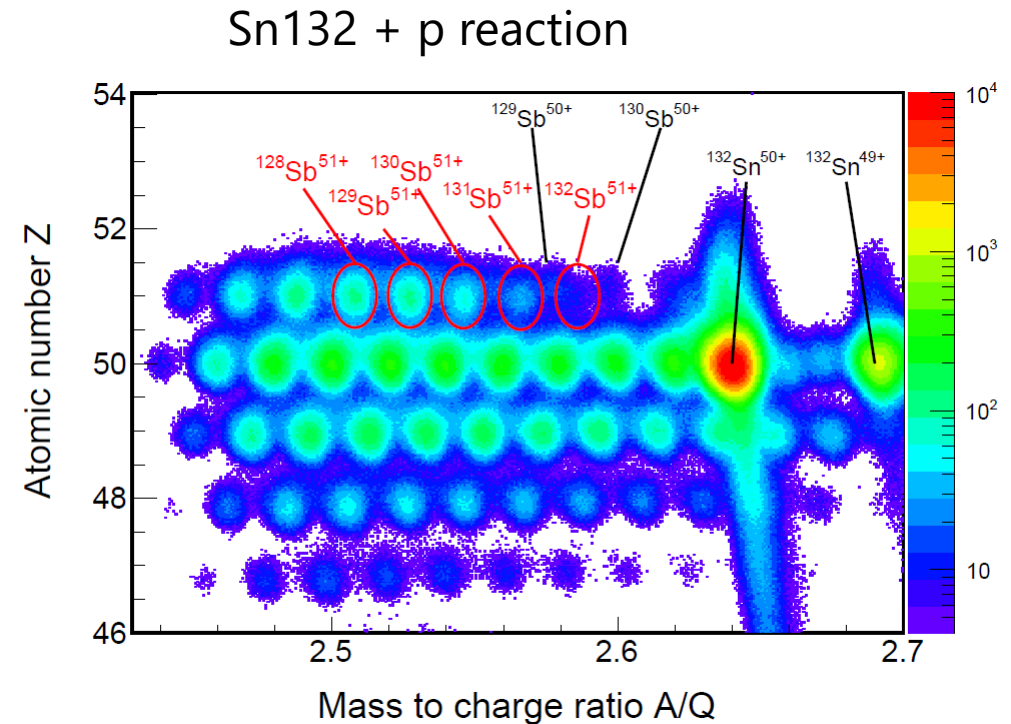


- Fundamental spectra to check the transport model.
- EoS dependence appears in triton production.
  - Triton easily produced in neutron rich matter.
- **Data favor  $L = 46\text{MeV}$  rather than  $L = 108\text{MeV}$ .**

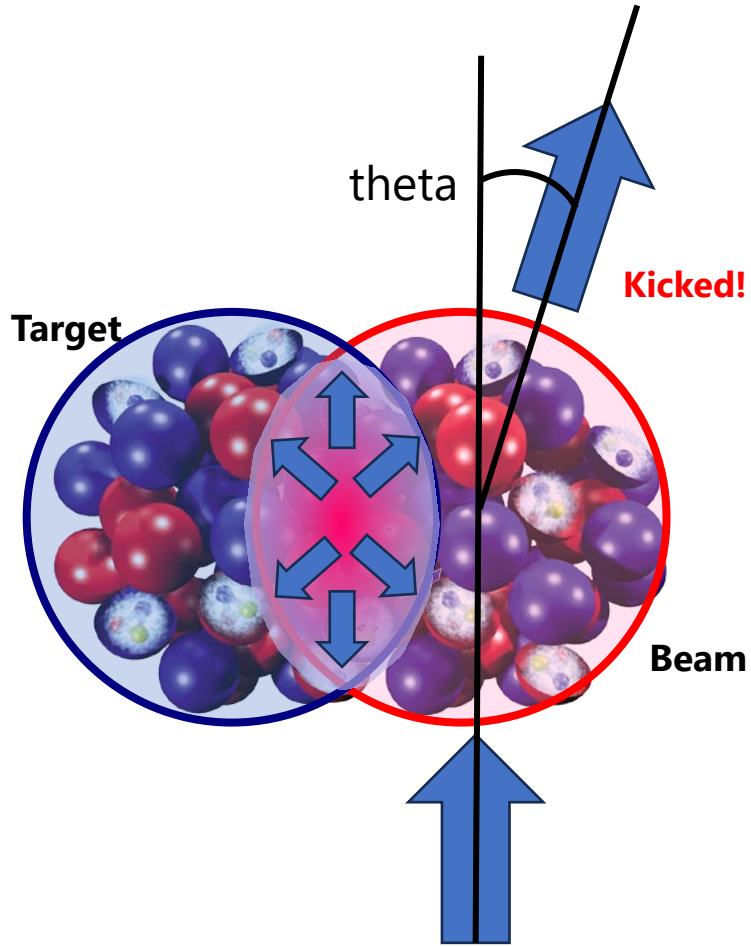


# Difference from Relativistic HIC

- Many body system composed of nucleons.
- Cluster state such as deuterium and alpha exists.
- x100 Longer collision time of  $\sim O(10\text{fm})$ .
- Less charged particles.
  - Track finding is simpler.
  - Worse reaction plane resolution.
- Possible to measure neutron production and its flow.
- Possible to identify spectator and to measure its kinematics.

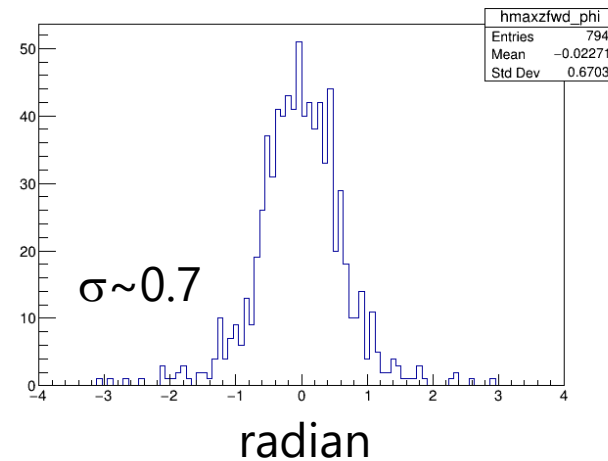


# Measurement of spectator for event characterization

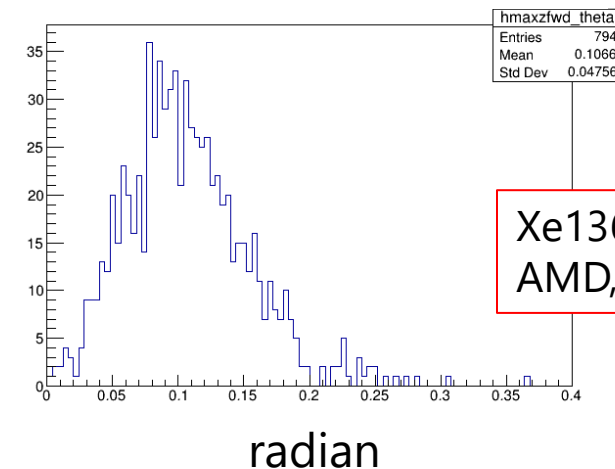


- Spectator would be useful for event characterization.
- According to AMD calculation:
  - It looks difficult to measure impact parameter through the measurement of spectator fragment.
  - Spectator information may deduce the reaction plane angle more precisely.
    - $\sigma(\Delta\phi)$  w/ participants: 1rad
    - $\sigma(\Delta\phi)$  w/ **spectator: 0.7 rad**

$\Delta\phi$ :  $\phi(\text{RP}) - \phi(\text{spectator})$   
of largest Z particle



theta of largest Z particle



Xe136+Sn124  
AMD, SLy4, b=8fm

# Summary

- Symmetry energy term of nuclear EoS is essential to understand the property of neutron star.
- Heavy RI collision experiment was conducted at RIKEN-RIBF to give constraint on EoS for high dense regime.
  - Spirit experiment
  - Charged pion and hydrogen production was measured.
- Delta baryon potential in dense matter is necessary to study pion production in HIC. → next step
- Proton/neutron measurement → next step for momentum dependence of U in matter.
- I am curious the universality of physics among the different hierarchy: nuclear matter and quark matter.
- Exotic hadron  $\leftrightarrow$  Exotic nuclei
- Halo state, Borromean, Strong E/B field ...